

CHAPTER 8: Measurement Relationships

8.6 Surface Area of a Sphere

Surface Area of a Sphere

The formula for the surface area of a sphere with radius r is $SA = 4\pi r^2$.

If you know the surface area of a sphere, you can determine the radius r , of a sphere.

Example:

a) A spherical storage tank has a radius of 8 m.
Find the surface area of the tank.

b) A can of paint covers 20 m^2 and costs \$30.
How much will it cost to paint the tank?

c) A new tank will be built with a surface area of 2000 m^2 . What radius will be required?

Solution:

$$\begin{aligned} \text{a) } SA &= 4\pi r^2 \\ &= 4 \times \pi \times 8^2 \\ &= 804.2 \text{ m}^2 \end{aligned}$$

The surface area of the tank is 804.2 m^2 .

$$\text{b) } \frac{804.2}{20} = 40.2$$

The city will need to buy 41 cans of paint.

The cost will be $41 \times 30 = \$1230$.

$$\begin{aligned} \text{c) } SA &= 4\pi r^2 \\ 2000 &= 4\pi r^2 \\ \frac{2000}{4\pi} &= \frac{4\pi r^2}{4\pi} \\ 159.2 &= r^2 \\ 12.6 \text{ m} &= r \end{aligned}$$

The new tank requires a radius of 12.6 m.



Practice:

1. a) The envelope of a hot air balloon can be approximated with a sphere with a radius of 12 m. Find the area of Dacron required to make the balloon.

b) Balloon quality Dacron sells for $\$5/\text{m}^2$. How much does it cost to buy the Dacron for the balloon?

c) A smaller balloon has a surface area of 1000 m^2 . What is the radius of this balloon?



Answers:

1. a) 1809.6 m^2 b) $\$9047.79$ c) 8.9 m