Pump Performance Curves and Similarity Laws

Pump performance results are typically obtained from an experimental test of the given pump and are presented graphically for each performance parameter.

- Typical independent variable Q {usually gpm (liquids) or cfm (gases)}
- Typical dependent variables are

H – head pressure rise, in some cases ΔP

BHP – input power requirements (motor size)

- η pump efficiency
- These are graphed for fixed pump speed for each impeller diameter in a given family of pumps

Typical performance curves for a single impeller speed and diameter appear as



Fig. 11.6 Typical Centrifugal Pump Performance Curves at Fixed Pump Speed and diameter

These curves are observed to have the following characteristics:

- 1. h_p is approximately constant at low flow rate.
- 2. $h_p = 0$ at Q_{max} .

- 3. BHP is not equal to 0 at Q = 0.
- 4. BHP increases monotonically with the increase in Q.
- 5. $\eta_p = 0$ at Q = 0 and at Q_{max} .
- 6. Maximum pump efficiency occurs at <u>approximately</u> $Q^* = 0.6 Q_{max}$. This is the best efficiency point BEP. At any other operating point, efficiency is less, pump head can be higher or lower, and BHP can be higher or lower.
- 7. At the BEP, $Q = Q^*$, $h_p = h_p^*$, BHP = BHP*.

Measured Performance Data

Actual pump performance data will typically be presented graphically as shown in Fig. 11.7. Each graph will usually have curves representing the pump head vs. flow rate for two or more impeller diameters for a given class/model of pumps having a similar design. The graphs will also show curves of constant efficiency and constant pump power (BHP) for the impeller diameters shown. All curves will be for a fixed pump impeller speed.



Fig. 11.7 Measured performance curves for two models of a centrifugal water pump

How to Read Pump Performance Curves

Care must be taken to correctly read the performance data from pump curves. This should be done as follows:

- (1) For a given flow rate Q
- (2) Read vertically to a point on the pump head curve h for the impeller diameter D of interest.
- (3) All remaining parameters (efficiency & BHP) are read at this point; i.e., graphically interpolate between adjacent curves for BHP to obtain the pump power at this point.

Note that the resulting values are valid only for the conditions of these curves:

(1) pump model and design, (2) pump speed - N, (3) impeller size - D, (4) fluid (typically water)

Thus for the pump shown in Fig. 11.7a with an impeller diameter D = 32 in, we obtain the following performance at Q = 20,000 gpm:

Q = 20,000 gpm, D = 32 in, N = 1170 rpm H \cong 385 ft, BHP \cong 2300 bhp, $\eta_p \cong$ 86.3 %

Note that points that are not on an h vs. Q curve are not valid operating points. Thus for Fig. 11.7b, the conditions

$$Q = 22,000 \text{ gpm}, BHP = 1500 \text{ bhp}, hp = 250 \text{ ft}$$

do not correspond to a valid operating point because they do not fall on one of the given impeller diameter curves. However, for the same figure, the point

$$Q = 20,000$$
 gpm, BHP = 1250 bhp

is a valid point because it coincidentally also falls on the D = 38 in impeller curve at hp = 227 ft.

Net Positive Suction Head - NPSH

One additional parameter is typically shown on pump performance curves:

NPSH = head required at the pump inlet to keep the fluid from cavitating.

NPSH is defined as follows:

NPSH =
$$\frac{P_i}{\rho g} + \frac{V_i^2}{2g} - \frac{P_v}{\rho g}$$

where $P_i = pump$ inlet pressure

 P_v = vapor pressure of fluid

Considering the adjacent figure, write the energy equation between the fluid surface and the pump inlet to obtain the following:



NPSH =
$$\frac{P_{i}}{\rho g} + \frac{V_{i}^{2}}{2g} - \frac{P_{v}}{\rho g} = \frac{P_{a}}{\rho g} - Z_{i} - h_{f,a-i} - \frac{P_{v}}{\rho g}$$

For a pump installation with this configuration to operate as intended, the righthand-side of the above equation must be > the NPSH value for the operating flow rate for the pump.

Example:

A water supply tank and pump are connected as shown. $P_a = 13.6$ psia and the water is at $20 \degree C$ with $P_v = 0.34$ psia. The system has a friction loss of 4.34 ft. Will the NPSH of the pump of Fig. 11.7a at 20,000 gpm work?



Applying the previous equation we obtain

NPSH =
$$\frac{P_a}{\rho g} - Z_i - h_{f,a-i} - \frac{P_v}{\rho g}$$

NPSH = $\frac{(13.6 - 0.34) \text{lbf/in}^2 * 144 \text{ in}^2/\text{ft}^2}{62.4 \text{lbf/ft}^3} - (-10 \text{ ft}) - 4.34 \text{ ft}$

NPSH = 36.26 ft The pump will work because the system NPSH as shown in Fig. 11.7a is 30 ft which provides a 6.3 ft safety margin. Conversely, the pump could be located as close as 3.7 ft below the water surface and meet NPSH requirements.

Pump Similarity Laws

Application of the dimensional analysis procedures of Ch. V will yield the following three dimensionless performance parameters for centrifugal pumps:

Dimensionless flow coefficient:
$$C_Q = \frac{Q}{\omega D^3}$$

Dimensionless head coefficient: $C_H = \frac{gH}{\omega^2 D^2}$
Dimensionless power coefficient: $C_P = \frac{BHP}{\rho \omega^3 D^5}$

where ω is the pump speed in radians/time and other symbols are standard design and operating parameters with units that make the coefficients dimensionless.

How are these used?

These terms can be used to estimate design and performance changes between two pumps of similar design.

Stated in another way:

If pumps 1 and 2 are from the same geometric design family and are operating at similar kinematic and dynamic operating conditions, the flow rates, pump head, and pump power for the two pumps will be related according to the following expressions:

$\frac{\mathbf{Q}_2}{\mathbf{Q}_1} = \frac{\mathbf{N}_2}{\mathbf{N}_1} \left(\frac{\mathbf{D}_2}{\mathbf{D}_1}\right)^3$	Us de im
$\frac{\mathrm{H}_2}{\mathrm{H}_1} = \left(\frac{\mathrm{N}_2}{\mathrm{N}_1}\right)^2 \left(\frac{\mathrm{D}_2}{\mathrm{D}_1}\right)^2$	Us de im

Used to predict the new flow rate for a design change in pump speed N and impeller diameter D.

Used to predict the new pump head H for a design change in pump speed N and impeller diameter D.

BHP ₂	(ρ_2)	$(N_2)^2$	$\left(D_{2} \right)^{5}$	
$\overline{BHP_1} =$	$\left(\overline{\rho_1} \right)$	$\left(\overline{N_1}\right)$	$\left(\overline{D_1}\right)$	

Used to predict the new pump power BHP for a design change in fluid, ρ , pump speed N and impeller diameter D.

Example

It is desired to modify the operating conditions for the 38 in diameter impeller pump of Fig. 11.7b to a new pump speed of 900 rpm and a larger impeller diameter of 40 in.

Determine the new pump head and power for the new pump speed at the BEP.



For the D = 38 in impeller of Fig. 11.7b operating at 710 rpm, we read the best efficiency point (BEP) values as

$$Q^* = 20,000 \text{ gpm}, H^* = 225 \text{ ft}, BHP^* = 1250 \text{ hp}$$

Applying the similarity laws for $N_2 = 900$ rpm and $D_2 = D_1 = 38$ in, we obtain

$$\frac{Q_2}{Q_1} = \frac{N_2}{N_1} \left(\frac{D_2}{D_1}\right)^3 = \frac{900}{710} \left(\frac{40}{38}\right)^3 = 1.478$$

$$Q_2 = 20,000*1.478 = 29,570 \text{ gpm} \quad \text{ans.}$$

$$\frac{H_2}{H_1} = \left(\frac{N_2}{N_1}\right)^2 \left(\frac{D_2}{D_1}\right)^2 = \left(\frac{900}{710}\right)^2 \left(\frac{40}{38}\right)^2 = 1.78$$

$$H_2 = 225*1.78 = 400.5 \text{ ft} \quad \text{ans.}$$

$$\frac{BHP_2}{BHP_1} = \left(\frac{\rho_2}{\rho_1}\right) \left(\frac{N_2}{N_1}\right)^3 \left(\frac{D_2}{D_1}\right)^5 = (1) \left(\frac{900}{710}\right)^3 \left(\frac{40}{38}\right)^5 = 2.632$$

$$BHP2 = 3290 \text{ hp} \quad \text{ans.}$$

Thus, even small changes in the speed and size of a pump can result in significant changes in flow rate, head, and power.

It is noted that every point on the original 38 in diameter performance curve exhibits a similar translation to a new operating condition.

The similarity laws are obviously useful to predict changes in the performance characteristics of an existing pump or to estimate the performance of a modified pump design prior to the construction of a prototype.

Matching a Pump to System Characteristics

The typical design/sizing requirement for a pump is to select a pump which has a pump head which matches the required system head at the design/operating flow rate for the piping system.

Key Point

$$h_p = h_{sys}$$
 at Q_{des} .

It is noted that pump selection should occur such that the operating point of the selected pump should occur on the pump curve near or at the BEP.

From the energy equation in Ch. VI, the system head is typically expressed as

$$h_{sys} = \frac{P_2 - P_1}{\rho g} + \frac{V_2^2 - V_1^2}{2g} + Z_2 - Z_1 + \left\{ f \frac{L}{D} + \sum K_i \right\} \frac{V^2}{2g}$$

Thus, the selection of a pump for a piping system design should result in a pump for which the pump head h_p at the design flow rate Q_{des} is equal (or very close) to the head requirements h_{sys} of the piping system at the same flow rate, and this should occur at or near the point of maximum efficiency for the chosen pump.



Other operating and performance requirements (such as NPSH) and cost are obviously also a part of the selection criteria for a pump.