## Assignment 18: Separable Differential Equations (7.2) Name Please provide a handwritten response.

1a. The separable differential equation $y^{\prime}=\frac{x^{2}+\sqrt{x}}{\boldsymbol{e}^{2 y}+y-\sin \boldsymbol{y}}$ is written as $\int\left(e^{2 y}+y-\sin y\right) d y=\int\left(x^{2}+\sqrt{x}\right) d x$ with the variables separated. Integrate $\int\left(e^{\wedge}(2 y)+y-\sin (y), y\right)$ and store the result as $g(y)$. Integrate $\int\left(x^{\wedge} 2+\sqrt{x}, x\right)$ and store the result as $\boldsymbol{h}(\boldsymbol{x})$. Now form $\boldsymbol{g}(\boldsymbol{y})=\boldsymbol{h}(\boldsymbol{x})+\boldsymbol{c}$ and record your result below.

1b. You can form an IVP (Initial Value Problem) by adding the initial condition $\boldsymbol{y}(\mathbf{1 . 5})=\mathbf{1}$ to the differential equation in 1a. Evaluate $\boldsymbol{g}(\boldsymbol{y})=\boldsymbol{h}(\boldsymbol{x})+\boldsymbol{c}$ at $\boldsymbol{y}(\mathbf{1 . 5})=\mathbf{1}$ by entering $\boldsymbol{g}(\boldsymbol{y})=\boldsymbol{h}(\boldsymbol{x})+\boldsymbol{c} \mid \boldsymbol{x}=\mathbf{1 . 5}$ and $\boldsymbol{y}=\mathbf{1}$ and record the result below. Use the solve command to solve the resulting equation for $\boldsymbol{c}$ and record the result below.

Rewrite the general solution substituting the above value for $\boldsymbol{c}$ (add $\mid \boldsymbol{c}=$ $\qquad$ to the above result) and record the solution below.

1c. It would be impossible to solve this particular solution for $y$. To graph this solution you can graph it as you graphed the implicit function in Assignment 9. Put the IVP in $\downarrow \mathbf{Y}$ as $z 1(x, y)=\left(e^{\wedge}(2 y)\right) / 2+y^{\wedge} 2 / 2+\cos (y)-\left(x^{\wedge} 3\right) / 3-\left(2 x^{\wedge}(3 / 2)\right) / 3-2.385$ (on the Voyage 200 enter this expression as $\boldsymbol{y 1}$ and deselect $\boldsymbol{y 1} \mathbf{1}$ ). Set the WINDOW to $\mathbf{0} \leq x \leq 5,-6 \leq y \leq 2$ before starting. Record your results on the graph below.


TI-89


Voyage 200

1d. If there were no initial condition attached to the differential equation, then you could create a family of particular solutions by letting $c$ range, say, from -2 to 2 . These solutions could then be graphed on the same axes showing how the solutions vary with $c$. Plot $z 1=e^{\wedge}(2 y) / 2+y^{\wedge} 2 / 2+\cos y-x^{\wedge} 3 / 3-\left(2 x^{\wedge}(3 / 2) / 3\right)+c$ with $c=-2,0,2$ (on the Voyage 200 enter the expression in $\boldsymbol{y 1}$, deselect $\boldsymbol{y} \mathbf{1}$ and run the impgraph program). First use $\boldsymbol{c}=\mathbf{- 2}$ and save the picture as dif1 for comparison. Regraph the expression with $\boldsymbol{c}=\mathbf{0}$ and compare with the picture. Sketch the graphs obtained when $\boldsymbol{c}=-\mathbf{2 , 0} 2$ on the same set of axes below.


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