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1 2 3 4 5 6 7 8 9 10 024 16 15 14 13 12 11 10 09 08 07

# **Contents**

### CHAPTER 1

<b>Foldables</b>			
Vocat	Vocabulary Builder		
1-1	Variables and Expressions 4		
1-2	Order of Operations		
1-3	Open Sentences		
1-4	Identity and Equality Properties 11		
1-5	The Distributive Property 13		
1-6	Commutative and Associative		
	Properties 15		
1-7	Logical Reasoning and		
	Counterexamples 17		
1-8	Number Systems 19		
1-9	Functions and Graphs 22		
<b>Study Guide</b>			

### CHAPTER 2

Foldables		
Vocabulary Builder		
2-1	Writing Equations	
2-2	Solving Equations by Using	
	Addition and Subtraction 35	
2-3	Solving Equations by Using	
	Multiplications and Division 37	
2-4	Solving Multi-Step Equations 40	
2-5	Solving Equations with the	
	Variable on Each Side 43	
2-6	Ratios and Proportions 45	
2-7	Percent of Change 48	
2-8	Solving Equations and Formulas 50	
2-9	Weighted Averages 53	
<b>Study Guide</b>		

### CHAPTER 3

<b>Foldables</b>		
Vocabulary Builder		
3-1		
3-2	Representing Functions 65	
3-3	Linear Functions 67	
3-4	Arithmetic Sequences 70	
3-5	Proportional and Nonproportional	
	Relationships 72	
<b>Study Guide</b>		

### CHAPTER 4

_		
Foldables		
Vocabulary Builder		
4-1	Rate of Change and Slope 82	
4-2	Slope and Direct Variation	
4-3	Graphing Equations in	
	Slope-Intercept Form 88	
4-4	Writing Equations in	
	Slope-Intercept Form 91	
4-5	Writing Equations in	
	Point-Slope Form	
4-6	Statistics: Scatter Plots and	
	Lines of Fit	
4-7	Geometry: Parallel and	
	Perpendicular Lines	
<b>Study Guide</b>		
-		

### CHAPTER 5

Foldables		
Vocabulary Builder		106
5-1	Graphing Systems of Equations	108
5-2	Substitution	110
5-3	Elimination Using Addition and	
	Subtraction	113
5-4	Elimination Using	
	Multiplication	115
5-5	Applying Systems of Linear	
	Equations	117
Study Guide		120

### CHAPTER 6

Foldables		
Vocabulary Builder		
6-1	Solving Inequalities by Addition	
	and Subtraction 127	
6-2	Solving Inequalities by	
	Multiplication and Division 129	
6-3	Solving Multi-Step Inequalities 131	
6-4	Solving Compound Inequalities 133	
6-5	Solving Open Sentences Involving	
	Absolute Value 136	
6-6	Solving Inequalities Involving	
	Absolute Value 138	
6-7	Graphing Inequalities in	
	Two Variables 140	
6-8	Graphing Systems of Inequalities 143	
<b>Study Guide</b> 146		

# **Contents**

### CHAPTER 7

<b>Foldables</b>		
Vocabulary Builder		
7-1	Multiplying Monomials	154
7-2	Dividing Monomials	157
7-3	Polynomials	159
7-4	Adding and Subtracting	
	Polynomials	162
7-5	Multiplying a Polynomial by a	
	Monomial	164
7-6	Multiplying Polynomials	166
7-7	Special Products	169
<b>Study Guide</b> 17		

### CHAPTER 8

Foldables		
Vocabulary Builder		176
8-1	Monomials and Factoring	178
8-2	Factoring Using the Distributive	
	Property	180
8-3	Factoring Trinomials	
	$ax^2 + bx + c$ :	182
8-4	Factoring Trinomials	
	$ax^2 + bx + c$ :	184
8-5	Factoring Differences of	
	Squares	187
8-6	Perfects Squares and Factoring	189
<b>Study Guide</b> 19		

### CHAPTER 9

<b>Foldables</b>		
Vocabulary Builder 198		
9-1	Graphing Quadratic Functions 200	
9-2	Solving Quadratic Equations by	
	Graphing 205	
9-3	Solving Quadratic Equations by	
	Completing the Square 208	
9-4	Solving Quadratic Equations by	
	Using the Quadratic Formula 211	
9-5	Exponential Functions 214	
9-6	Growth and Decay 217	
<b>Study Guide</b>		

### CHAPTER 10

Foldables.224Vocabulary Builder.225		
<b>10-1</b> Simplifying Radical Expressions. 227		
<b>10-2</b> Operations with Radical		
Expressions 230		
<b>10-3</b> Radical Equations		
<b>10-4</b> The Pythagorean Theorem 234		
<b>10-5</b> The Distance Formula		
<b>10-6</b> Similar Triangles 239		
<b>Study Guide</b> 242		

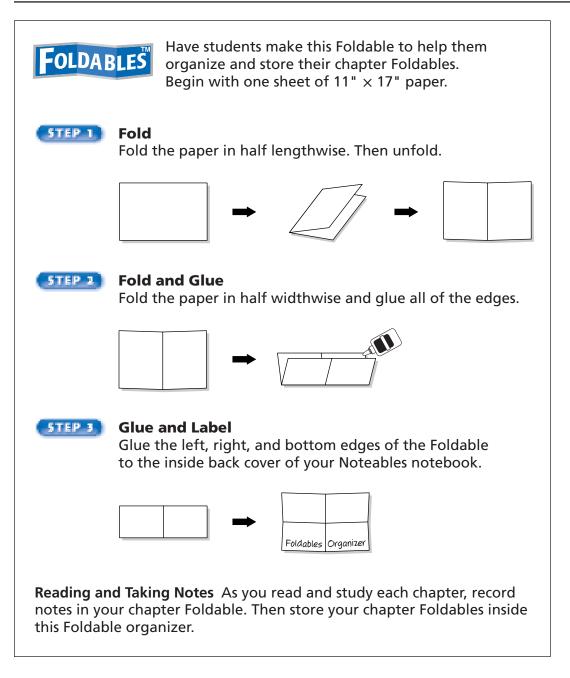
### CHAPTER 11

Foldables		
Vocabulary Builder		
11-1	Inverse Variation.	249
11-2	Rational Expressions	251
11-3	Multiplying Rational	
	Expressions	253
11-4	Dividing Rational Expressions	255
11-5	Dividing Polynomials	258
11-6	Rational Expressions with Like	
	Denominators	260
11-7	Rational Expressions with Unlike	
	Denominators	262
11-8	Mixed Expressions and Complex	
	Fractions	265
11-9	Solving Rational Equations	267
<b>Study Guide</b> 271		

### CHAPTER 12

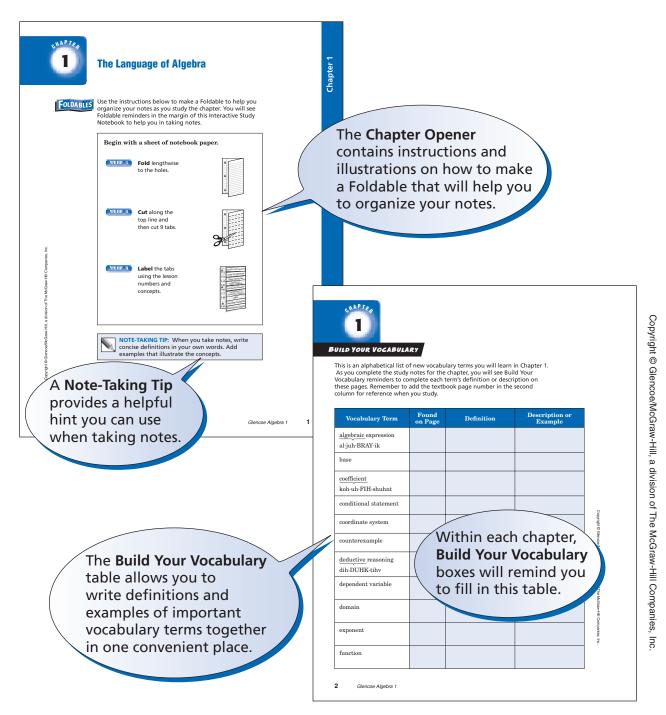
<b>Foldables</b>		
Vocabulary Builder 278		
12-1	Sampling and Bias 280	
12-2	Counting Outcomes	
12-3	Permutations and	
	Combinations	
12-4	Probability of Compound	
	Events	
12-5	Probability Distributions 289	
12-6	Probability Simulations 291	
<b>Study Guide</b>		

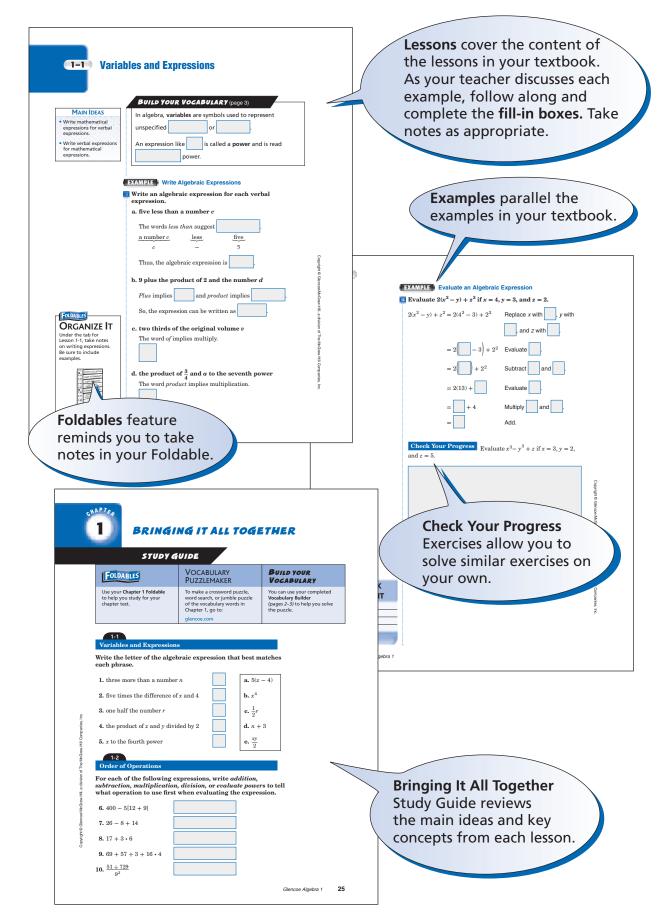
# **Organizing Your Foldables**



# Using Your Noteables Interactive Study Notebook

This note-taking guide is designed to help you succeed in *Algebra 1*. Each chapter includes:





# NOTE-TAKING TIPS

Your notes are a reminder of what you learned in class. Taking good notes can help you succeed in mathematics. The following tips will help you take better classroom notes.

- Before class, ask what your teacher will be discussing in class. Review mentally what you already know about the concept.
- Be an active listener. Focus on what your teacher is saying. Listen for important concepts. Pay attention to words, examples, and/or diagrams your teacher emphasizes.
- Write your notes as clear and concise as possible. The following symbols and abbreviations may be helpful in your note-taking.

Word or Phrase	Symbol or Abbreviation	Word or Phrase	Symbol or Abbreviation
for example	e.g.	not equal	¥
such as	i.e.	approximately	*
with	w/	therefore	<i>.</i>
without	w/o	versus	VS
and	+	angle	۷

- Use a symbol such as a star (\*) or an asterisk (\*) to emphasize important concepts. Place a question mark (?) next to anything that you do not understand.
- Ask questions and participate in class discussion.
- Draw and label pictures or diagrams to help clarify a concept.
- When working out an example, write what you are doing to solve the problem next to each step. Be sure to use your own words.
- Review your notes as soon as possible after class. During this time, organize and summarize new concepts and clarify misunderstandings.

### **Note-Taking Don'ts**

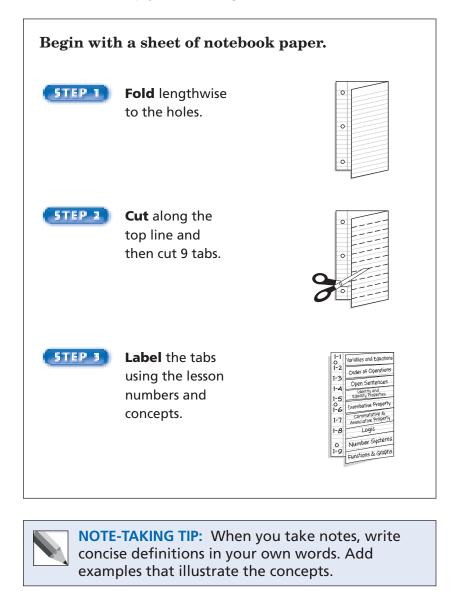
- Don't write every word. Concentrate on the main ideas and concepts.
- **Don't** use someone else's notes as they may not make sense.
- Don't doodle. It distracts you from listening actively.
- Don't lose focus or you will become lost in your note-taking.



# **The Language of Algebra**



Use the instructions below to make a Foldable to help you organize your notes as you study the chapter. You will see Foldable reminders in the margin of this Interactive Study Notebook to help you in taking notes.





BUILD YOUR VOCABULARY

This is an alphabetical list of new vocabulary terms you will learn in Chapter 1. As you complete the study notes for the chapter, you will see Build Your Vocabulary reminders to complete each term's definition or description on these pages. Remember to add the textbook page number in the second column for reference when you study.

Vocabulary Term	Found on Page	Definition	Description or Example
algebraic expression			
al·juh·BRAY·ik			
base			
coefficient			
koh·uh·FIH·shuhnt			
conditional statement			
coordinate system			
counterexample			
deductive reasoning			
dih·DUHK·tihv			
dependent variable			
domain			
exponent			
function			

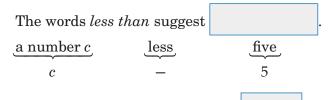
Vocabulary Term	Found on Page	Definition	Description or Example
hypothesis			
hy·PAH·thuh·suhs			
independent variable			
inequality			
integer			
irrational numbers			
like terms			
multiplicative inverses			
open sentence			
order of operations			
perfect square			
principal square root			
rational approximation			
real numbers			
reciprocal			
solution set			

# **1–1** Variables and Expressions

	Build Your VocaBulary (page 3)
l bal	In algebra, <b>variables</b> are symbols used to represent unspecified or .
sions	An expression like is called a <b>power</b> and is read
	power.

### EXAMPLE Write Algebraic Expressions

- Write an algebraic expression for each verbal expression.
  - a. five less than a number *c*



Thus, the algebraic expression is

- **b.** 9 plus the product of 2 and the number d
  - *Plus* implies

and *product* implies

So, the expression can be written as

### c. two thirds of the original volume v

The word of implies multiply.

d. the product of  $\frac{3}{4}$  and *a* to the seventh power The word *product* implies multiplication.



### MAIN IDEAS

- Write mathematica expressions for verb expressions.
- Write verbal express for mathematical expressions.

4

FOLDABLES

examples.

Under the tab for

Organize It

Lesson 1-1, take notes on writing expressions. Be sure to include

> ariables and Equati Order of Operation Open Sentences

umber Sys ins & Gras

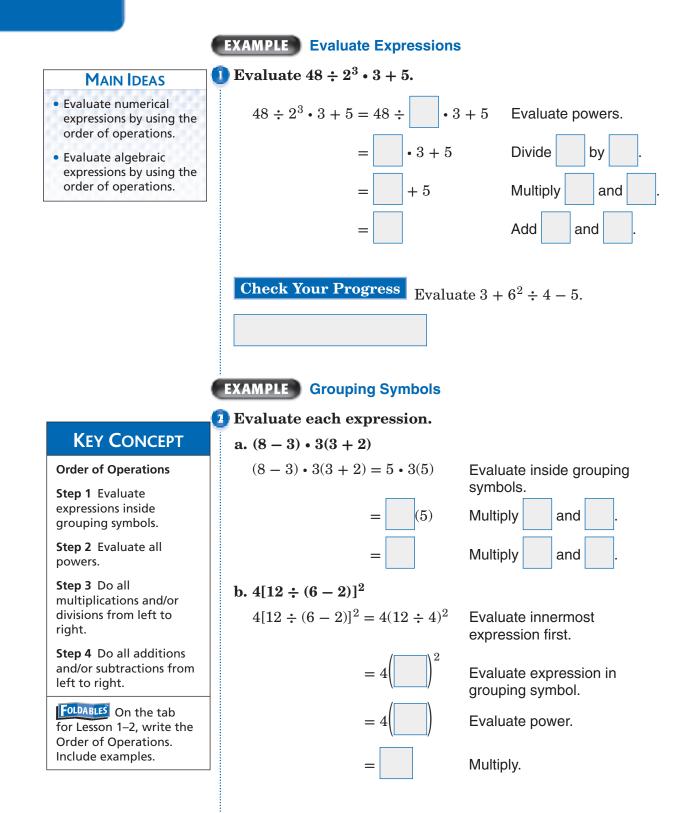
Glencoe Algebra 1

	Check Your Progress Write an algebraic expression		
	for each verbal expression.		
	<b>a.</b> nine more than a number <i>h</i>		
	<b>b.</b> the difference of 6 and 4 times a number $x$		
	<b>c.</b> one half the size of the original perimeter <i>p</i>		
	c. one han the size of the original permeter p		
	<b>d.</b> the product of 6 and <i>x</i> to the fifth power		
(	EXAMPLE Evaluate Powers		
	D Evaluate 3 <sup>4</sup> .		
	$3^4 = 3 \cdot 3 \cdot 3 \cdot 3$ Use as a factor times.		
	Multiply		
	= Multiply.		
	<b>Check Your Progress</b> Evaluate the expression 5 <sup>4</sup> .		
•	EXAMPLE Write Verbal Expressions		
	Write a verbal expression for each algebraic expression.		
	a. $\frac{8x^2}{5}$		
	the quotient of 8 times and		
	b. $y^5 - 16y$		
	the difference of and		
Homework			
ASSIGNMENT	<b>Check Your Progress</b> Write a verbal expression for		
Page(s):	each algebraic expression.		
Exercises:	<b>a.</b> $7a^4$ <b>b.</b> $x^2 + 3$		
( )			

1-1

### **Order of Operations**

1-2



**1-2**  
**c.** 
$$\frac{2^{5}-6\cdot 2}{3^{3}-5\cdot 3-2} = 4 = 4 + 3$$

$$\frac{2^{5}-6\cdot 2}{3^{3}-5\cdot 3-2} = 4 = 4 + 3$$

$$\frac{2^{5}-6\cdot 2}{3^{3}-5\cdot 3-2} = 4 = 4 + 3$$

$$\frac{2^{5}-6\cdot 2}{3^{3}-5\cdot 3-2} = 4 = 4 + 3$$

$$\frac{2^{5}-6\cdot 2}{3^{3}-5\cdot 3-2} = 4 = 4 + 3$$

$$\frac{2^{5}-6\cdot 2}{3^{3}-5\cdot 3-2} = 4 + 3$$

$$\frac{2^{5}-6\cdot 3-2}{3^{3}-5\cdot 3-2} = 4 + 3$$

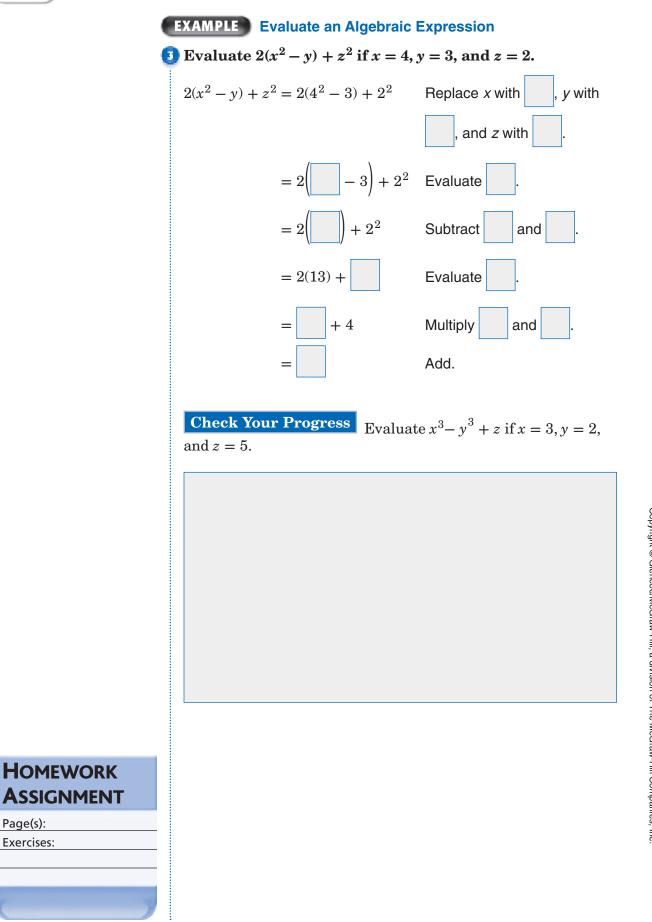
$$\frac{2^{5}-6\cdot 3-2}{3^{3}-5\cdot 3-2} = 4 + 3$$

$$\frac{2^{5}-6\cdot 3-2}{3^{3}-5\cdot 3-2} = 4 + 3$$

$$\frac{2^{5}-6\cdot 3-2}{3^{5}-5\cdot 3-2} = 4 + 3$$

$$\frac{2^{5}-6\cdot 3-2}{3^{5}-5\cdot 3-2} = 4 + 3$$





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Page(s): Exercises:

## 1-3

## **Open Sentences**

in a

### MAIN IDEAS

- Solve open sentence equations.
- Solve open sentence inequalities.

### BUILD YOUR VOCABULARY (pages 2-3)

The process of finding a value for a variable that results

sentence is called **solving the open sentence**.

A sentence that contains an sign is called an equation.

A set of numbers from which replacements for a

may be chosen is called a replacement set.

### EXAMPLE Use a Replacement Set to Solve an Equation

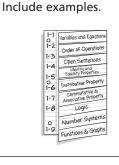
**1** Find the solution set for 3(8 - b) = 6 if the replacement set is  $\{2, 3, 4, 5, 6\}$ .

Replace *b* in 3(8 - b) = 6 with each value in the replacement set.

а	3(8-b)=6	True or False?
2	$3(8-2) \stackrel{?}{=} 6 \rightarrow 18 \neq 6$	
3	$3(8-3) \stackrel{?}{=} 6 \rightarrow 15 \neq 6$	
4	$3(8-4) \stackrel{?}{=} 6 \rightarrow 12 \neq 6$	
5	$3(8-5) \stackrel{?}{=} 6 \rightarrow 9 \neq 6$	
6	$3(8-6) \stackrel{?}{=} 6 \rightarrow 6 = 6$	

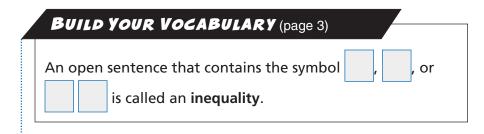
The solution set is

**Check Your Progress** Find the solution set for the equation 6c - 5 = 7 if the replacement set is  $\{0, 1, 2, 3, 4\}$ .



FOLDABLES

**ORGANIZE IT** Under the tab for Lesson 1-3, explain how to solve open sentence equations and inequalities.



### EXAMPLE

FISHING Carlos needs \$35 or more for a fishing trip. He already bought a ticket for the charter boat for \$13. Does Carlos need to save \$20, \$21, \$22, or \$23 to have enough money for the fishing trip? Find the solution set for  $s + 13 \ge 35$  if the replacement set is {20, 21, 22, 23}.

Replace s in  $s + 13 \ge 35$  with each value in the replacement set.

s	<i>s</i> + 13 ≥ 35	True or False?
20	$20 + 13 \ge 35 \longrightarrow 33 \ge 35?$	
21	$21 + 13 \ge 35 \longrightarrow 34 \ge 35?$	
22	$22 + 13 \ge 35 \rightarrow 35 \ge 35$	
23	$23 + 13 \ge 35 \rightarrow 36 \ge 35$	

The solution set for  $s + 13 \ge 35$  is \_\_\_\_\_\_. Carlos needs to save at least \$22 or \$23 for the fishing trip.

**Check Your Progress SHOPPING** Maleka needs \$75 or more for a shopping trip. She already bought a sweater for \$22. Does Maleka need to save \$51, \$52, \$53, or \$54 to have enough money for the shopping trip? Find the solution set for  $s + 23 \ge 75$  if the replacement set is  $\{51, 52, 53, 54\}$ .

- ${\bf A}$  {51, 52}; Maleka needs to save at least \$51 or \$52 for the shopping trip.
- **B** {53, 54}; Maleka needs to save at least \$53 or \$54 for the shopping trip.
- ${\bf C}$  {55}; Maleka needs to save at least \$55 for the shopping trip.
- ${\bf D}$  {35}; Maleka needs to save at least \$35 for the shopping trip.

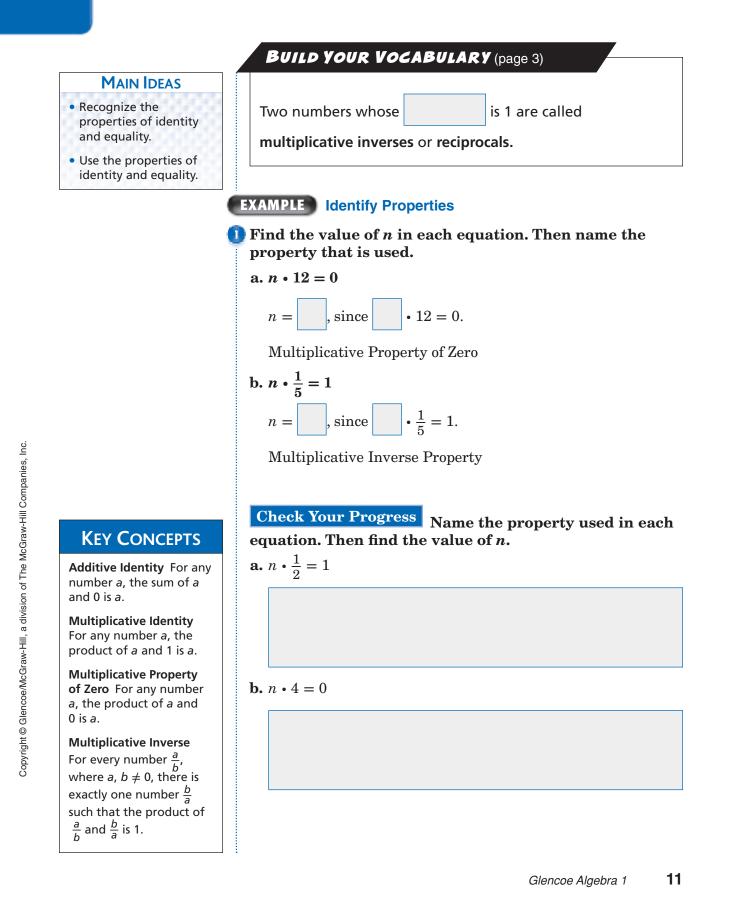
REVIEW IT Write in words how each of the following symbols is read: >, <, ≥, ≤.

### Homework Assignment

Page(s): Exercises:



## **Identity and Equality Properties**





### **KEY CONCEPTS**

**Reflexive** Any quantity is equal to itself.

**Symmetric** If one quantity equals a second quantity, then the second quantity equals the first.

**Transitive** If one quantity equals a second quantity and the second quantity equals a third quantity, then the first quantity equals the third quantity.

**Substitution** A quantity may be substituted for its equal in any expression.

**FOLDABLES** List the Identity and Equality Properties under the tab for Lesson 1–4. Include an example of each property.

HOMEWORK Assignment

Page(s): Exercises:



### **EXAMPLE** Evaluate Using Properties

2 Evaluate  $\frac{1}{4}(12 - 8) + 3(15 \div 5 - 2)$ . Name the property used in each step.

$$\frac{1}{4}(12 - 8) + 3(15 \div 5 - 2)$$

$$= \frac{1}{4}(4) + 3(15 \div 5 - 2)$$

$$; 12 - 8 = 4$$

$$= \frac{1}{4}(4) + 3(3 - 2)$$

$$; 15 \div 5 = 3$$

$$= \frac{1}{4}(4) + 3(1)$$

$$; 3 - 2 = 1$$

$$= 1 + 3(1)$$

$$; \frac{1}{4} \cdot 4 = 1$$

$$= 1 + 3$$

$$; 3 \cdot 1 = 3$$

$$= 4$$

$$; 1 + 3 = 4$$

**Check Your Progress** Evaluate  $\frac{1}{3}(10-7) + 4(18 \div 9 - 1)$ .

Name the property used in each step.

$$\frac{1}{3}(10 - 7) + 4(18 \div 9 - 1)$$

$$= \frac{1}{3}(3) + 4(18 \div 9 - 1)$$

$$= \frac{1}{3}(3) + 4(2 - 1)$$

$$= \frac{1}{3}(3) + 4(1)$$

$$= 1 + 4(1)$$

$$= 1 + 4$$

$$= 5$$

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### **The Distributive Property** 1-5

### **MAIN IDEAS**

- Use the Distributive Property to evaluate expressions.
- Use the Distributive Property to simplify expressions.

KEY CONCEPT

**Distributive Property** 

For any numbers a, b,

a(b + c) = ab + ac and (b + c)a = ba + ca and

a(b - c) = ab - ac and (b - c)a = ba - ca

FOLDABLES Under the tab

for Lesson 1–5, write the

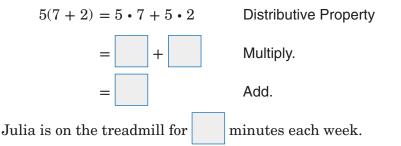
**Distributive Property.** Write a numeric and algebraic example of the

property.

and c,

**EXAMPLE** Distribute Over Addition or Subtraction

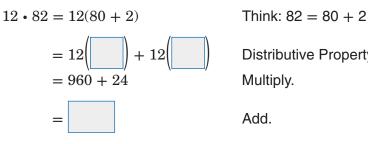
🚺 EXERCISE Julia walks 5 days a week. She walks at a fast rate for 7 minutes and then cools down for 2 minutes. Rewrite 5(7 + 2) using the Distributive Property. Evaluate to find the total number of minutes Julia walks.



**Check Your Progress** WALKING Susanne walks to school and home from school 5 days each week. She walks to school in 15 minutes and then walks home in 10 minutes. Rewrite 5(15 + 10) using the Distributive Property. Then evaluate to find the total number of minutes Susanne spends walking to and home from school.

### **EXAMPLE** The Distributive Property and Mental Math

**1** Use the Distributive Property to rewrite 12 • 82. Then evaluate.



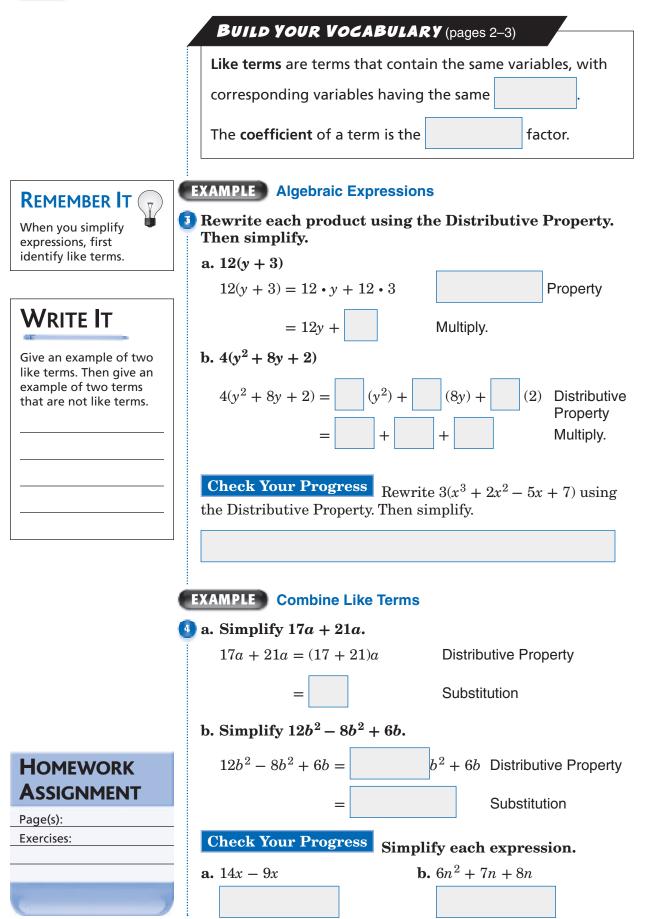
**Distributive Property** 

Multiply.

Add.

**Check Your Progress** Use the Distributive Property to find 6 • 54.

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## **Commutative and Associative Properties**

**EXAMPLE** Use Addition Properties

### **1** TRANSPORTATION Refer to Example 1 on p. 34 of MAIN IDEAS vour book. Find the distance between Lakewood/ Recognize the Ft. McPherson and Five Points. Explain how the Commutative and **Commutative Property makes calculating the answer** Associative Properties. unnecessary. • Use the Commutative and Associative Calculating the answer is actually unnecessary because the Properties to simplify route is the opposite of the one in Example 1 of the textbook. expressions. The Property states that the in which numbers are added does not matter. The distance is miles. EXAMPLE Use Multiplication Properties 🕗 Evaluate 2 • 8 • 5 • 7 using properties of numbers. Name the property used in each step. You can rearrange and group the factors to make mental calculations easier. $2 \cdot 8 \cdot 5 \cdot 7 = 2 \cdot 5 \cdot 8 \cdot 7$ Property (x) • (8 • 7) Property (x) Multiply. = Multiply. = **KEY CONCEPTS**

### **Check Your Progress**

**a.** The distance from Five Points to Garnett is 0.4 mile. From Garnett, West End is 1.5 miles. From West End, Oakland City is 1.5 miles. Write an expression to find the distance from Five Points to Oakland City. Then write an expression to find the distance from Oakland City to Five Points.

**b.** Evaluate 3 • 5 • 3 • 4.

**Commutative Property** 

The order in which you add or multiply numbers

does not change their

Associative Property The

way you group three or

more numbers when adding or multiplying does not change their sum or product.

**FOLDABLES** List the properties on the tab for

Lesson 1-6.

sum or product.



### **EXAMPLE** Write and Simplify an Expression

- Use the expression three times the sum of 3x and 2y added to five times the sum of x and 4y.
  - a. Write an algebraic expression for the verbal expression.

Words	Three times the sum of $3x$ and $2y$ added to five times the sum of $x$ and $4y$
Variables	Let <i>x</i> and <i>y</i> represent the numbers.
Expression	

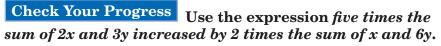
b. Simplify the expression and indicate the properties used.

$$3(3x + 2y) + 5(x + 4y)$$

$$= 3(3x) + 3(2y) + 5(x) + 5(4y)$$
Distributive Proper  

$$= 9x + 6y + 5x + 20y$$
Multiply.
$$= 9x + 5x + 6y + 20y$$
Commutative (+)
$$= (9x + 5x) + (6y + 20y)$$
Associative (+)
$$= (9 + 5)x + (6 + 20)y$$
Distributive Proper  

$$=$$
Substitution



**a.** Write an algebraic expression for the verbal expression.

Property

Property

**b.** Simplify the expression and indicate the properties used.

### HOMEWORK **ASSIGNMENT**

Page(s): Exercises:



# **Logical Reasoning and Counterexamples**

	Build Your Vocabulary (pages 2–3)	
MAIN IDEAS	<b>Conditional statements</b> can be written in the form	
• Identify the hypothesis and conclusion in a conditional statement.	A B.	
<ul> <li>Use a counterexample to show that an assertion is false.</li> </ul>	The part of the statement immediately after is called the <b>hypothesis</b> . The part of the statement immediately after is	
	called the <b>conclusion</b> .	
	EXAMPLE Identify Hyphothesis and Conclusion	
	Identify the hypothesis and conclusion of each statement.	
a. If it is raining, then Jon and Chloe will not play softball.		
	The hypothesis follows the word and the conclusion	
	follows the word	
	Hypothesis:	
	Conclusion:	
	b. If $7y + 5 \le 26$ , then $y \le 3$ .	
Foldables	Hypothesis:	
ORGANIZE IT On the tab for Lesson 1–7, write a conditional	Conclusion:	
sentence and label the hypothesis and	<b>Check Your Progress</b> Identify the hypothesis and conclusion of each statement.	
conclusion.	<b>a.</b> If it is above 75°, then you can go swimming.	
1-1     Variables and Equations       1-2     Crider of Operations       1-3     Open Sentences       1-4     Learning and writer Medicines       1-5     Learning and writer Medicines       0-6     Distributive Property		
1-6 Communities & Associations Property 1-8 Logic 0 Number Systems 1-9 Functions & Graphs	<b>b.</b> If $2x + 3 = 5$ , then $x = 1$ .	



### EXAMPLE Write a Conditional in If-Then Form

Identify the hypothesis and conclusion of the statement. Then write the statement in if-then form.
a. I eat light meals.
Hypothesis: I eat a meal
Conclusion: it is light
<b>b.</b> For a number <i>a</i> such that $8 + 5a = 43$ , $a = 7$ . Hypothesis: $8 + 5a = 43$
Conclusion:
<b>Check Your Progress</b> Identify the hypothesis and conclusion of the statement. Then write the statement in if-then form. For a number $x$ such that $11 + 5x < 21, x \le 2$ .
EXAMPLE
Determine a valid conclusion that follows from the statement, "If one number is odd and another number is even, then their sum is odd" for the given conditions. If a valid conclusion does not follow, write no valid conclusion and explain why.
The two numbers are 5 and 12
5 is odd and 12 is even, so the hypothesis is true.
<b>Check Your Progress</b> Determine a valid conclusion

that follows from the statement "*If the last digit in a number is 0, then the number is divisible by 10*" for the given conditions. If a valid conclusion does not follow, write *no valid conclusion*.

The number is 4005.

Homework Assignment

Page(s): Exercises:



# **Square Roots and Real Numbers**

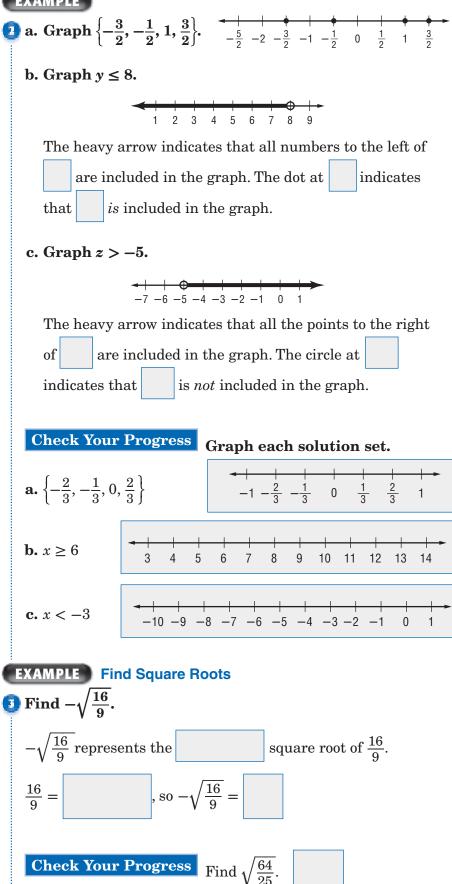
	BUILD YOUR VOCABULARY (page 31)			
MAIN IDEAS				
• Find square roots.	A square root is one of two square of a number.			
<ul> <li>Classify and order real numbers.</li> </ul>	A number whose square root is a number is			
	called a <b>perfect square.</b>			
	A radical sign is used to indicate the or			
	principal square root of the expression under the radical sign.			
	<b>EXAMPLE</b> Classify Real Numbers Name the set or sets of numbers to which each number			
	belongs.			
	<b>a.</b> $\sqrt{17}$			
	Because $\sqrt{17} =$ , which is neither a repeating			
	nor terminating decimal, this number is			
	<b>b.</b> $\frac{1}{6}$ Because 1 and 6 are integers and $1 \div 6 = 0.1666$ is a			
	repeating decimal, this number is a number. <b>c.</b> $\sqrt{169}$			
	Because $\sqrt{169} =$ , this number is a			
	number, a number, an and a			
WRITE IT	number.			
Are the square roots for $\sqrt{-81}$ and $\sqrt{81}$ the same? Explain.	<b>Check Your Progress</b> Name the set or sets of numbers to which each real number belongs.			
	<b>a.</b> $\frac{7}{9}$ <b>b.</b> $\sqrt{36}$			
	<b>c.</b> $\sqrt{45}$ <b>d.</b> $-\frac{56}{7}$			



### EXAMPLE

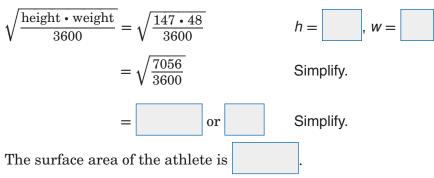


Real Numbers The set of real numbers consists of the set of rational numbers and the set of irrational numbers.



### EXAMPLE

SPORTS SCIENCE Refer to the application on p. 45 of your textbook. Find the surface area of an athlete whose height is 147 centimeters and whose weight is 48 kilograms.



**Check Your Progress SPORTS SCIENCE** Find the surface area of an athlete whose height is 152 centimeters and whose weight is 50 kilograms.

### EXAMPLE Order Real Numbers

**5** Write  $\frac{12}{5}$ ,  $\sqrt{6}$ , 2.4, and  $\frac{61}{25}$  in order from least to greatest. Write each number as a decimal.

$$\frac{12}{5} =$$

 $\sqrt{6} = 2.4494897...$  or about 2.4495.

 $2.\overline{4} = 2.444444...$  or about 2.4444.

 $\frac{61}{25} =$ 

Since 2.4 < 2.44 < 2.4444 < 2.4495, the numbers arranged in

order from least to greatest are

**Check Your Progress** Write  $\frac{5}{2}$ ,  $\sqrt{5}$ , 2. $\overline{2}$ , and  $\frac{51}{20}$  in order from least to greatest.

Homework Assignment

Page(s):

Exercises:

# **1-9** Functions and Graphs

MAIN IDEAS

Interpret graphs of functions.
Draw graphs of functions.

### BUILD YOUR VOCABULARY (page 2)

A function is a relationship between input and output, in		
which the depends on the .		
A <b>coordinate system</b> is used to graph		
n a function, the value of one quantity on		
he of the other. This is called		
he <b>dependent variable</b> . The other quantity is called		
the independent variable. The set of values for the		
variable is called the <b>domain</b> .		
The set of values for the variable is called variable.		

### EXAMPLE Identify Coordinates

**MEDICINE** Refer to the graph on p. 53 of your book. Name the ordered pair at point *E* and explain what it represents.

Point *E* is at 6 along the *x*-axis and about 100 along the *y*-axis.

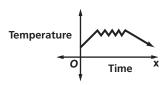
So, its ordered pair is

. This represents about

normal blood flow 6 days after the injury.

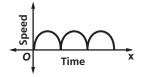
### EXAMPLE Analyze Graphs

The graph represents the temperature in Ms. Ling's classroom on a winter school day. Describe what is happening in the graph.





**Check Your Progress** The graph represents Macy's speed as she swims laps in a pool. Describe what is happening in the graph.



### **EXAMPLE** Draw Graphs

There are three lunch periods at a school cafeteria. During the first period, 352 students eat lunch. During the second period, 304 students eat lunch. During the third period, 391 students eat lunch.

WRITE IT

List three ways data can be represented.

**REMEMBER** IT

The *x*-axis is the horizontal axis and the *v*-axis is the vertical axis. The independent variable is graphed on the x-axis and the dependent variable is graphed on the *y*-axis.

a. Make a table showing the number of students for each of the three lunch periods.

Period	1	2	3
Number of Students			

### b. Write the data as a set of ordered pairs. Then graph the data.

The period is the variable and the number of students is the variable. The ordered pairs are When Students Eat Lunch Number of Students 375 350 325 300 0 2 and 3 0 2 3 1 Period

### **Check Your Progress**

At a car dealership, a salesman worked for three days. On the first day, he sold 5 cars. On the second day, he sold 3 cars. On the third day he sold 8 cars.

**a.** Make a table showing the number of cars sold for each day.

Day		
Number of Cars Sold		

- **b.** Write the data as a set of ordered pairs.
- **c.** Draw a graph that shows the relationship between the day and the number of cars sold.

### **EXAMPLE** Domain and Range

互 Mr. Ohms tutors students. He works at most 120 hours for \$4 per hour.

### a. Identify a domain and range for this situation.

The domain contains the number of hours he works. 

The domain is	to		hours. The range	contair	ıs
the amount he	makes fro	m \$0. T	hus, the range is		to

# $\times$ \$4 or

### b. Draw a graph that shows the relationship between the number of hours worked and the money Mr. Ohms makes.

500 Graph the ordered pairs **9** 400 200 Earned 200 Since any number and of hours up to 120 can be worked,

connect the two points with a line to include those points.



#### **Check Your Progress** Prom tickets cost \$25 per person. The prom is limited to 250 people.

**a.** Identitfy a domain and range for the situation.

**b.** Draw a graph that shows the relationship between the number of persons attending the prom and total admission price.

HOMEWORK ASSIGNMENT

Page(s): Exercises:



## **BRINGING IT ALL TOGETHER**

### STUDY GUIDE

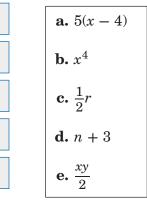
<b>FOLDABLES</b>	Vocabulary Puzzlemaker	Build your Vocabulary
Use your <b>Chapter 1 Foldable</b> to help you study for your chapter test.	To make a crossword puzzle, word search, or jumble puzzle of the vocabulary words in Chapter 1, go to: glencoe.com	You can use your completed <b>Vocabulary Builder</b> ( <i>pages 2–3</i> ) to help you solve the puzzle.

1-1

Variables and Expressions

# Write the letter of the algebraic expression that best matches each phrase.

three more than a number n
 five times the difference of x and 4
 one half the number r
 one half the number r
 the product of x and y divided by 2
 x to the fourth power



### Order of Operations

1-2

For each of the following expressions, write *addition*, *subtraction*, *multiplication*, *division*, or *evaluate powers* to tell what operation to use first when evaluating the expression.

6. 400 - 5[12 + 9]7. 26 - 8 + 148.  $17 + 3 \cdot 6$ 9.  $69 + 57 \div 3 + 16 \cdot 4$ 10.  $\frac{51 \div 729}{9^2}$ 

### Chapter **1** BRINGING IT ALL TOGETHER



1-4

11. How would you read each inequality symbol in words?

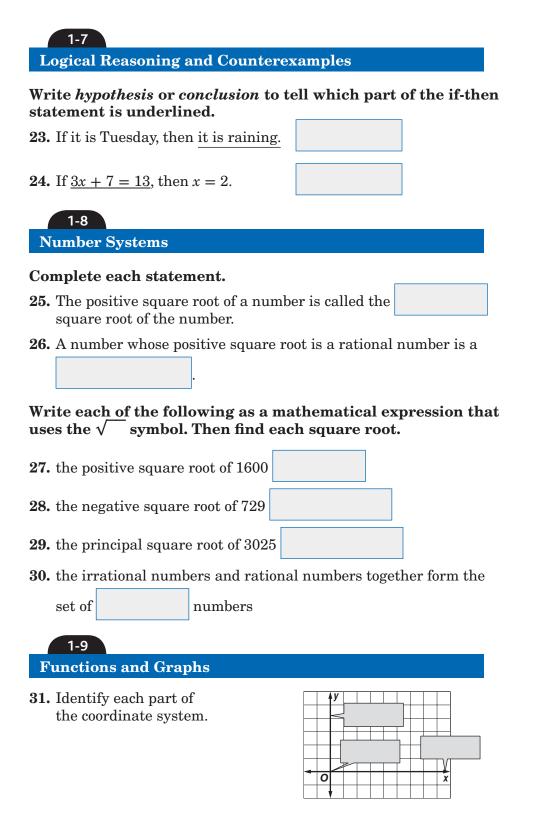
Symbol	Words	Symbol	Words
<		≤	
>		≥	

### **Identity and Equality Properties**

Name the property used in each statement.

12.  $\frac{5}{7} \cdot \frac{7}{5} = 1$ **13.**  $3 \cdot 1 = 3$ 14. 6 + 0 = 6**15.** If 2 + 4 = 5 + 1 and 5 + 1 = 6, then 2 + 4 = 6. **16.** If n = 2, then  $5n = 5 \cdot 2$ . 1-5 **The Distributive Property Rewrite using the distributive property.** 17. 5(6-4)**18.** 12*m* + 8*m* 1-6 **Commutative and Associative Properties** Write the letter of the term that best matches each equation. a. Associative Property of Addition **19**. 3 + 6 = 6 + 3**b.** Associative Property of Multiplication **20.** 2 + (3 + 4) = (2 + 3) + 4c. Commutative Property of Addition **21.**  $2 \cdot (3 \cdot 4) = (2 \cdot 3) \cdot 4$ d. Commutative Property of Multiplication **22.**  $2 \cdot (3 \cdot 4) = 2 \cdot (4 \cdot 3)$ 









Visit glencoe.com to access your textbook, more examples, self-check quizzes, and practice tests to help you study the concepts in Chapter 1.

## ARE YOU READY FOR THE CHAPTER TEST?

Check the one that applies. Suggestions to help you study are given with each item.

I completed the review of all or most lessons without using my notes or asking for help. • You are probably ready for the Chapter Test. • You may want to take the Chapter 1 Practice Test on page 65 of your textbook as a final check. I used my Foldable or Study Notebook to complete the review of all or most lessons. • You should complete the Chapter 1 Study Guide and Review on pages 60–64 of your textbook. If you are unsure of any concepts or skills, refer back to the specific lesson(s). • You may also want to take the Chapter 1 Practice Test on page 65. I asked for help from someone else to complete the review of all or most lessons. • You should review the examples and concepts in your Study Notebook and Chapter 1 Foldable. • Then complete the Chapter 1 Study Guide and Review on pages 60–64 of your textbook. • If you are unsure of any concepts or skills, refer back to the specific lesson(s). • You may also want to take the Chapter 1 Practice Test on page 65. Student Signature Parent/Guardian Signature

**Teacher Signature** 

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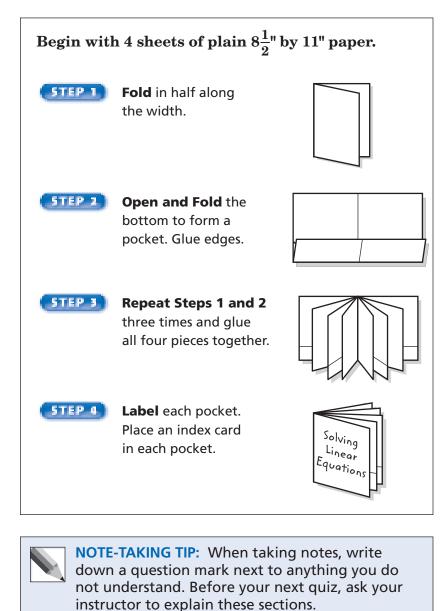


# **Solving Linear Equations**



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Use the instructions below to make a Foldable to help you organize your notes as you study the chapter. You will see Foldable reminders in the margin of this Interactive Study Notebook to help you in taking notes.





## BUILD YOUR VOCABULARY

This is an alphabetical list of new vocabulary terms you will learn in Chapter 2. As you complete the study notes for the chapter, you will see Build Your Vocabulary reminders to complete each term's definition or description on these pages. Remember to add the textbook page number in the second column for reference when you study.

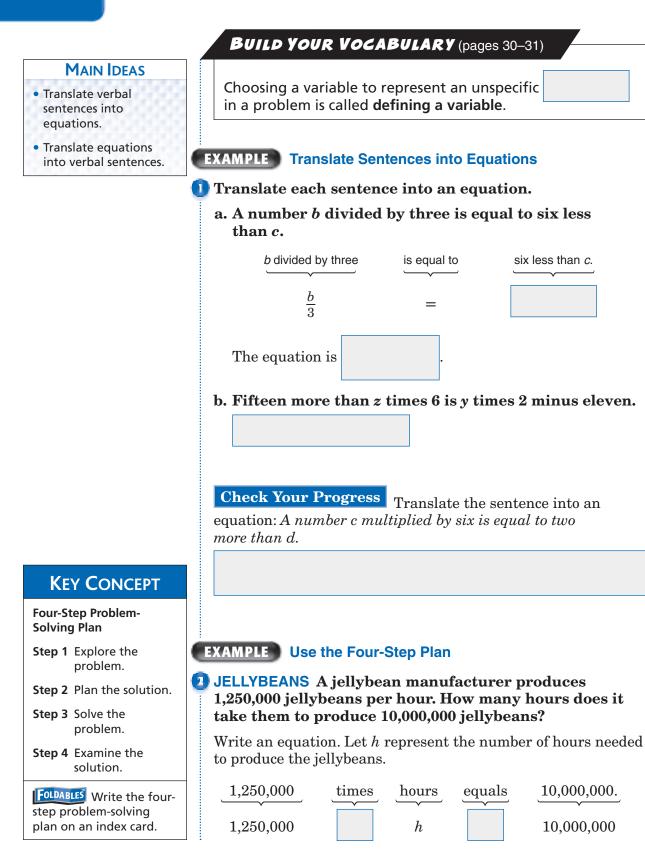
Vocabulary Term	Found on Page	Definition	Description or Example
consecutive integers			
[kuhn·SEH·kyuh·tihv]			
defining a variable			
dimensional analysis			
[duh·MEHNCH·nuhl]			
equivalent equations			
[ih·KWIHV·luhnt]			
extremes			
formula			
four-step problem-solving plan			
identity			
means			
mixture problem			
multi-step equations			

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Vocabulary Term	Found on Page	Definition	Description or Example
number theory			
percent of change			
percent of decrease			
percent of increase			
proportion [pruh·POHR·shun]			
ratio			
rate			
scale			
solve an equation			
uniform motion problem			
weighted average			

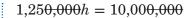


# 2–1 Writing Equations





for the



h =

Find *h* mentally by asking, "What number times 125 equals 1,000?"

It will take hours to produce 10,000,000 jellybeans.

**Check Your Progress** A person at the KeyTronic World Invitational Type-Off typed 148 words per minute. How many minutes would it take to type 3552 words?

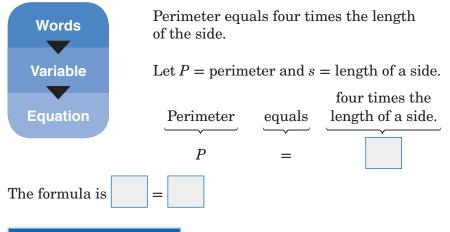
A formula is an that states a

**BUILD YOUR VOCABULARY** (pages 30-31)

relationship between certain quantities.

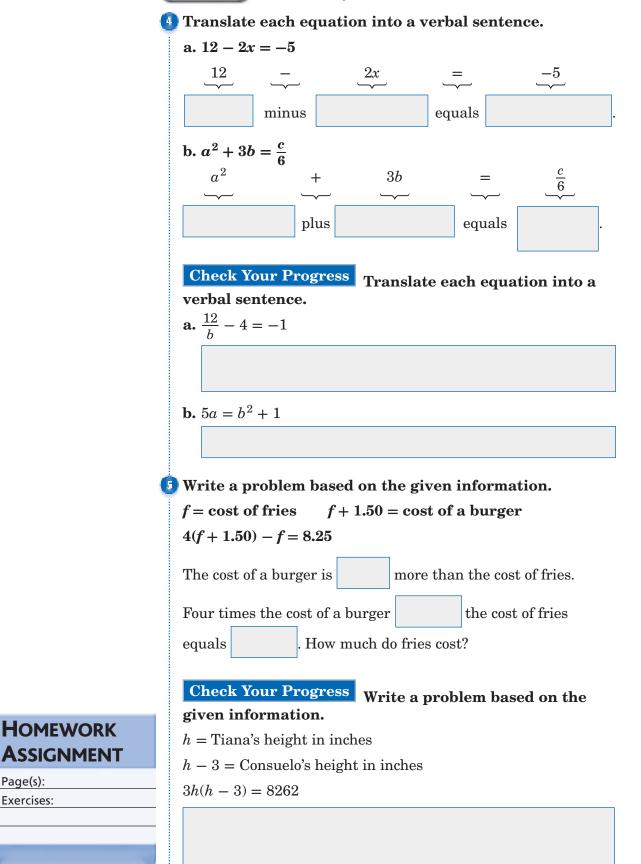
## EXAMPLE Write a Formula

Translate the sentence into a formula. The perimeter of a square equals four times the length of the side.



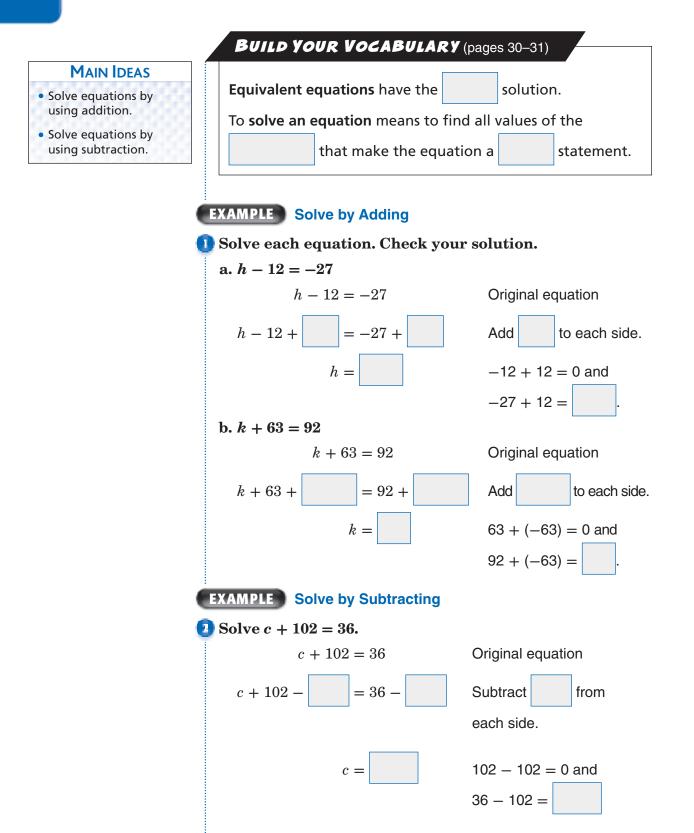
**Check Your Progress** Translate the sentence *The area of a circle equals the product of*  $\pi$  *and the square of the radius r* into a formula.

## **EXAMPLE** Translate Equations into Sentences





# **Solving Equations by Using Addition and Subtraction**

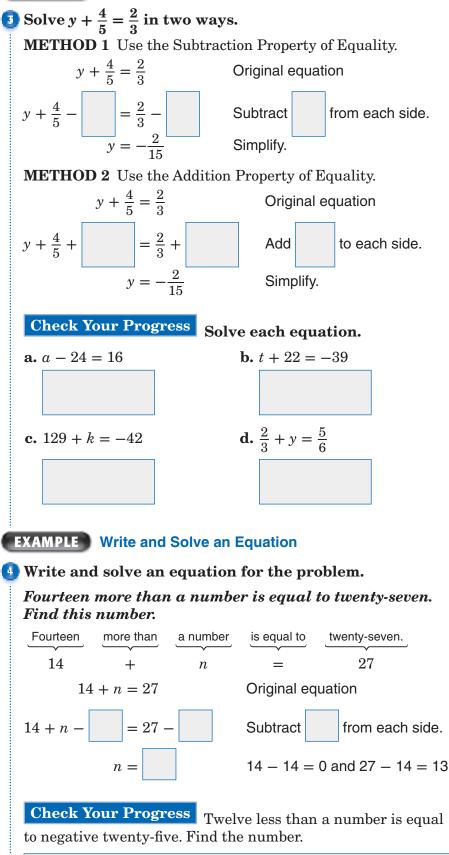




## **KEY CONCEPTS**

Addition Property of Equality If an equation is true and the same number is added to each side, the resulting equation is true.

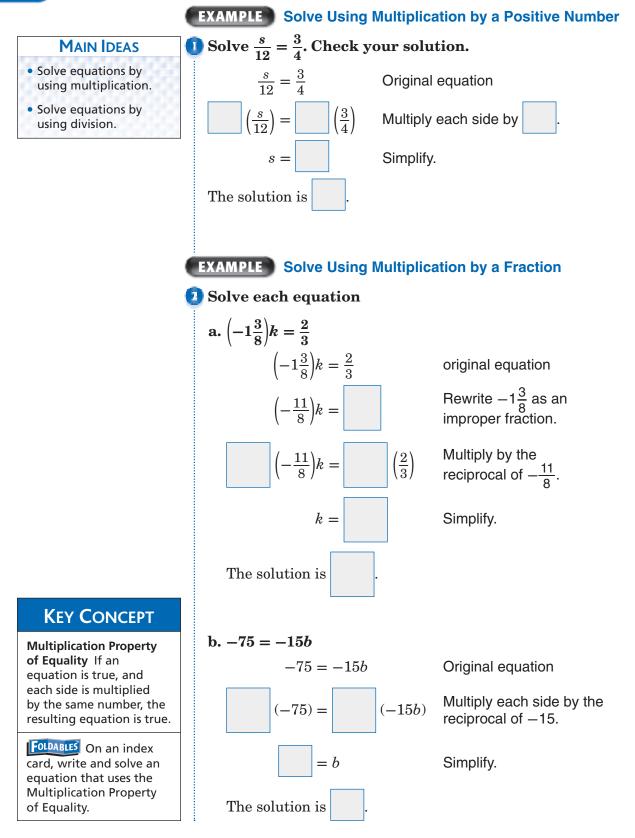
Subtraction Property of Equality If an equation is true and the same number is subtracted from each side, the resulting equation is true.



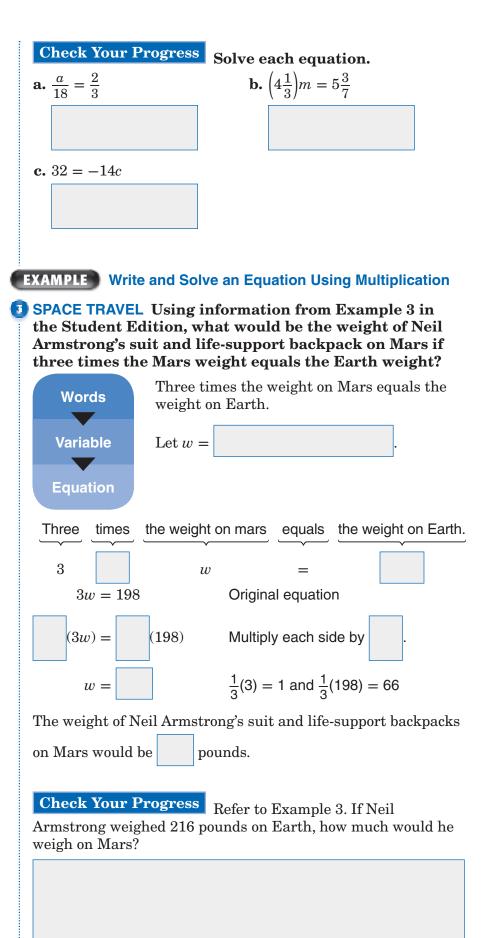
HOMEWORK ASSIGNMENT

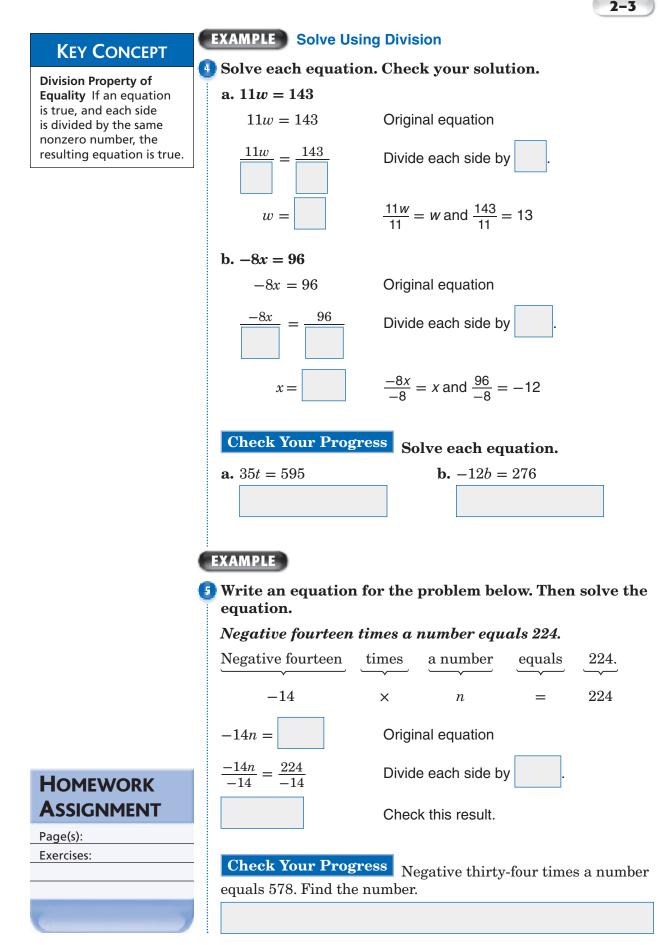
Page(s): Exercises:

# **Solving Equations by Using Multiplication and Division**



2-3







# **Solving Multi-Step Equations**

#### MAIN IDEAS

- Solve problems by working backward.
- Solve equations involving more than one operation.

BUILD YOUR VOCABULARY (pages 30-31)

**Work backward** is one of the many problem-solving strategies that you can use to solve multi-step equations.

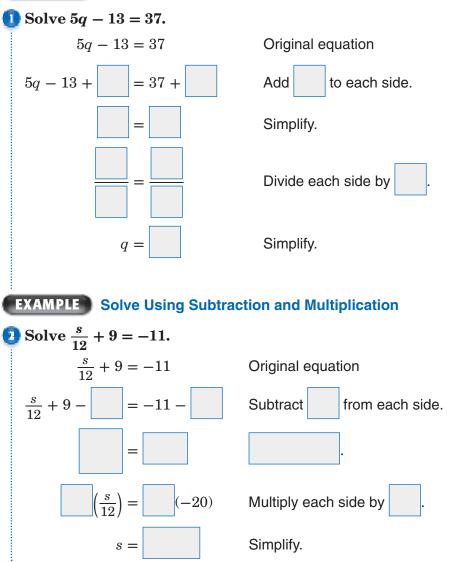
To solve equations with more than one operation, often

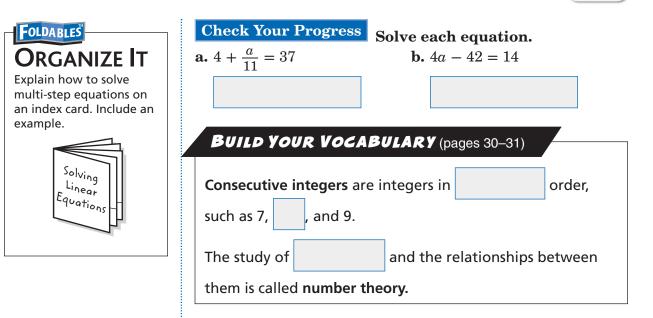
called multi-step equations,

operations by working

backward.

## EXAMPLE Solve Using Addition and Division

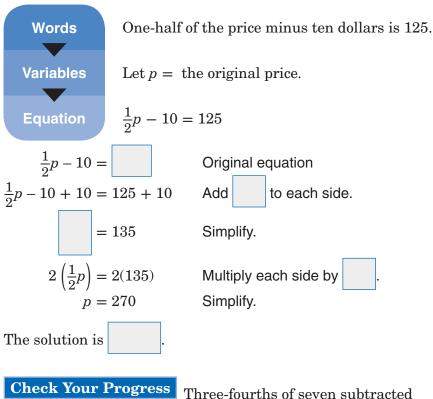




## EXAMPLE

 SHOPPING Susan had a \$10 coupon for the purchase of any item. She bought a coat that was <sup>1</sup>/<sub>2</sub> its original price.

After using the coupon, Susan paid \$125 for the coat before taxes. What was the original price of the coat? Write an equation for the problem. Then solve the equation.



from a number is negative fifteen. What is the number?

2 - 4



# WRITE IT

What is meant by undoing an equation?

-	-	

## EXAMPLE

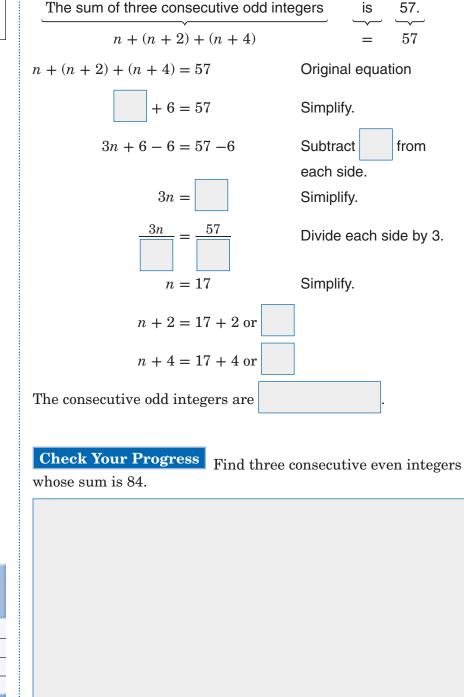
• NUMBER THEORY Write an equation for the problem below. Then solve the equation and answer the problem.

## Find three consecutive odd integers whose sum is 57.

Let n =the last odd integer.

Let n + 2 = the next greater odd integer.

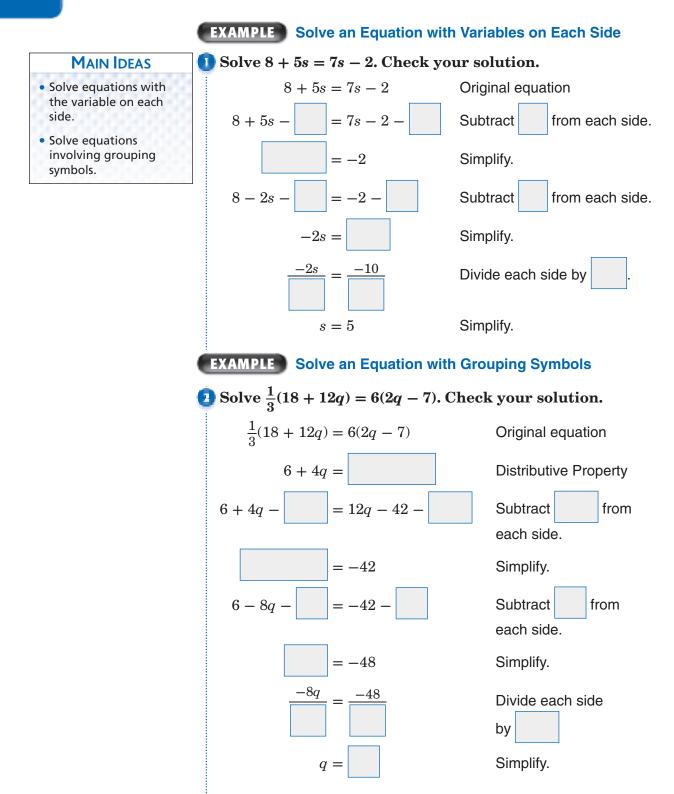
Let n + 4 = the greatest of the three odd integers.



Homework Assignment

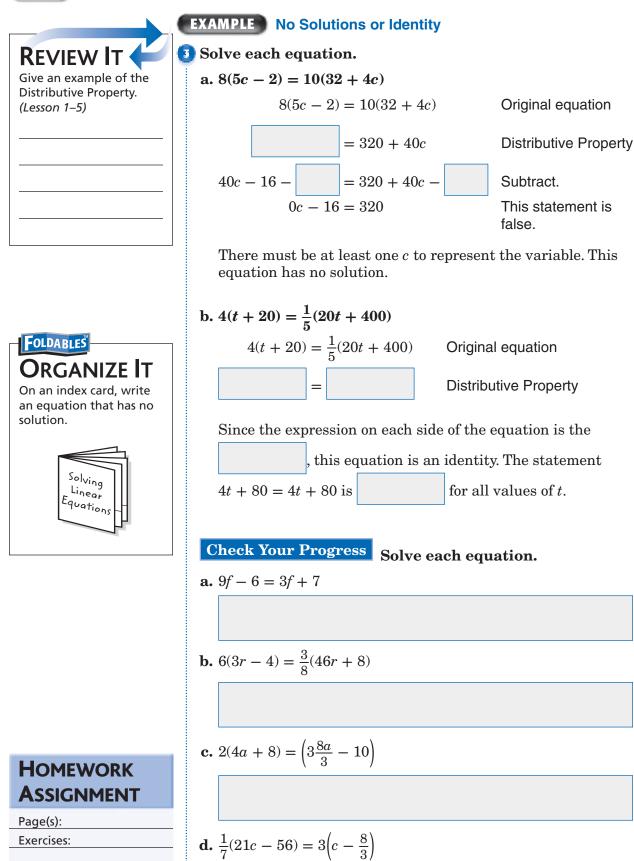
Page(s): Exercises:

# **Solving Equations with the Variable on Each Side**



2-5

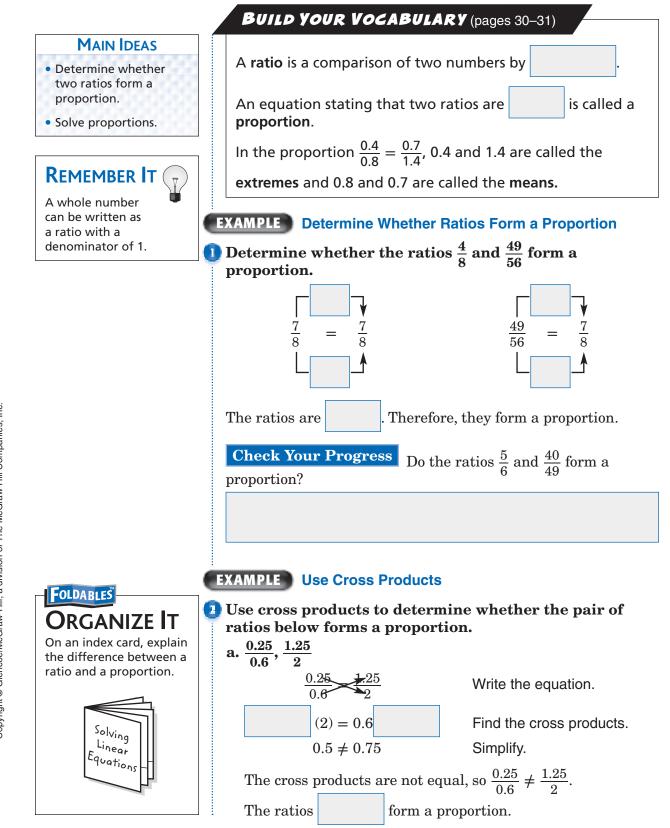


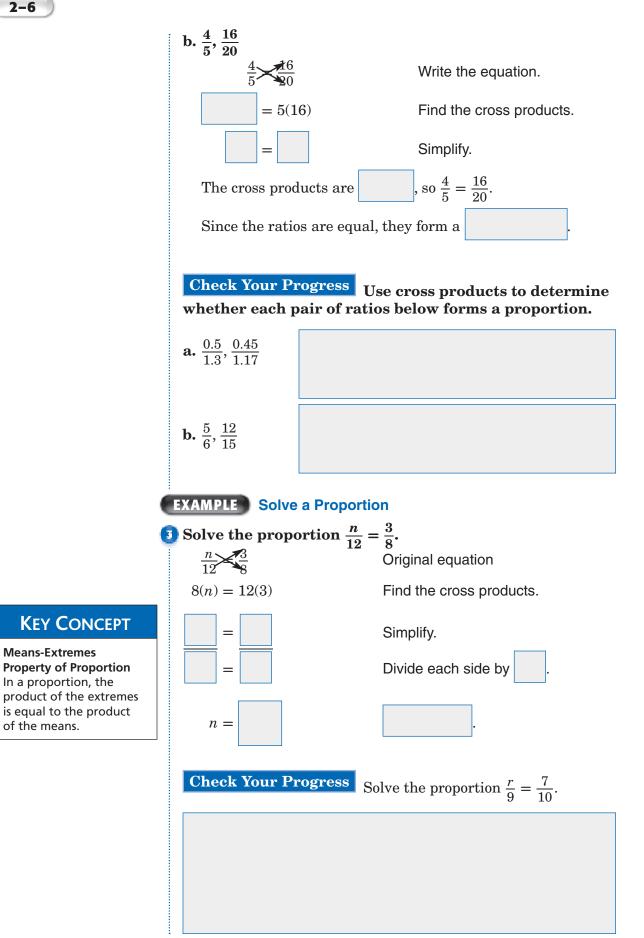


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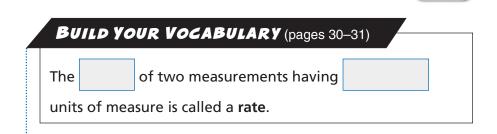
# **Ratios and Proportions**





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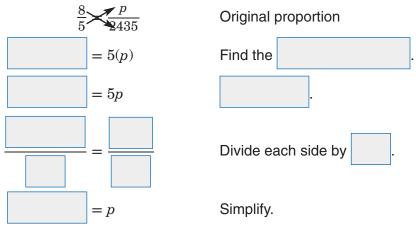
of the means.



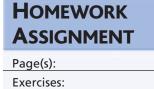
2 - 6

## EXAMPLE Use Rates

BICYCLING The gear on a bicycle is 8:5. This means that for every eight turns of the pedals, the wheel turns five times. Suppose the bicycle wheel turns about 2435 times during a trip. How many times would you have to turn the pedals during the trip?



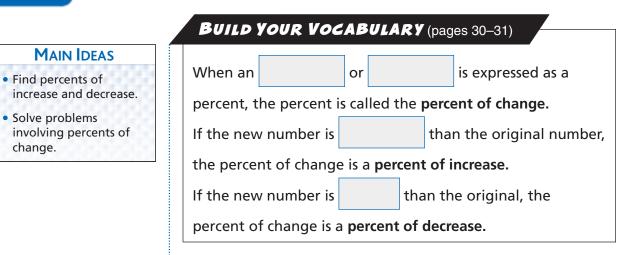
Your Turn Before 1980, Disney created animated movies using cels. These hand-drawn cels (pictures) of the characters and scenery represented the action taking place, one step at a time. For the movie *Snow White*, it took 24 cels per second to have the characters move smoothly. The movie is around 42 minutes long. About how many cels were drawn to produce *Snow White*?



# 2-7

change.

# **Percent of Change**

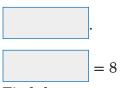


## EXAMPLE Find Percent of Change

#### State whether each percent of change is a percent of increase or a percent of decrease. Then find each percent of change.

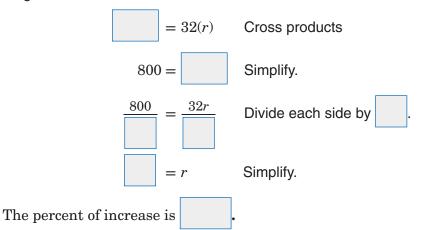
original: 32 **new: 40** 

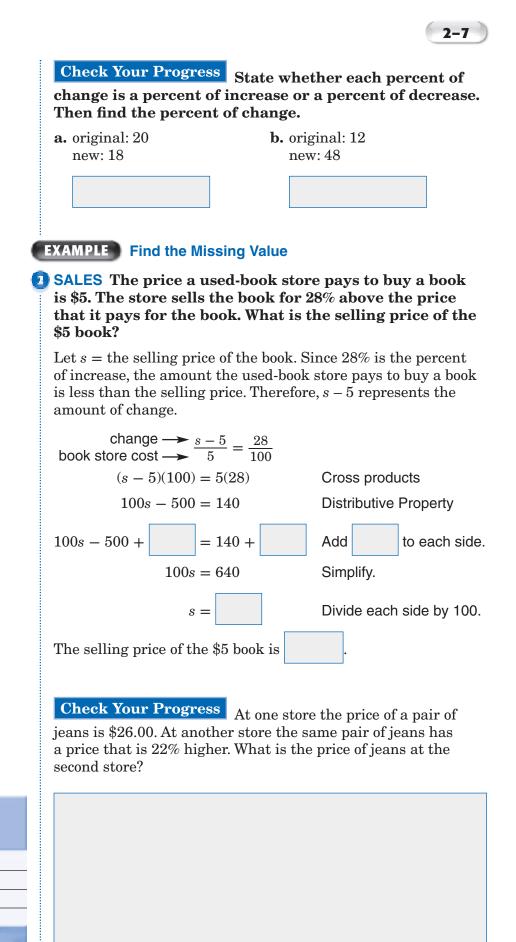
Find the *amount* of change. Since the new amount is greater than the original, the percent of change is a percent of



Find the percent using the original number, 32, as the base. change -> 8

= 100 original amount  $\rightarrow 32$ 





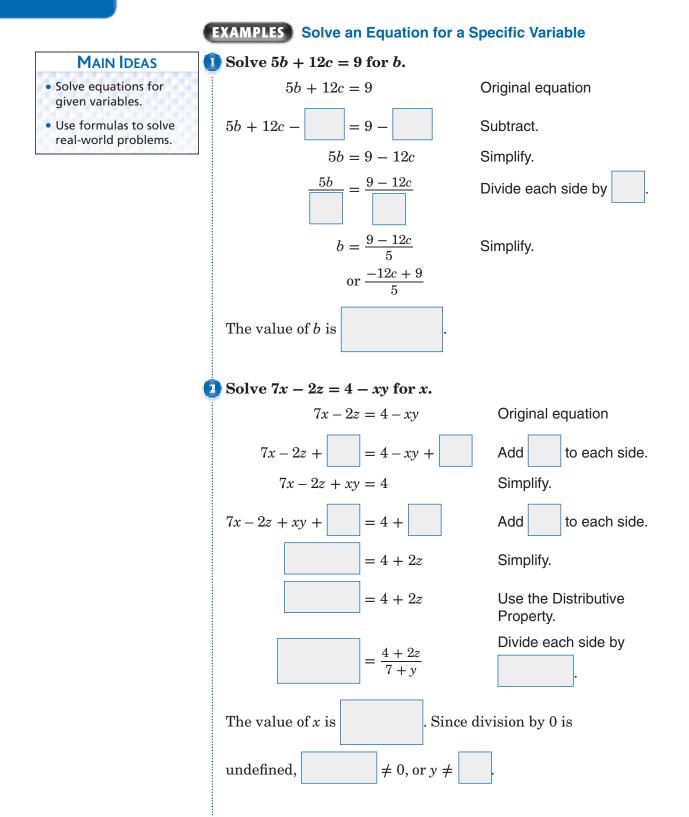
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HOMEWORK ASSIGNMENT

Page(s):

Exercises:

# **Solving Equations and Formulas**



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2-8



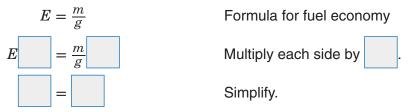
#### **Check Your Progress**

**a.** Solve 2x - 17y = 13 for *y*.

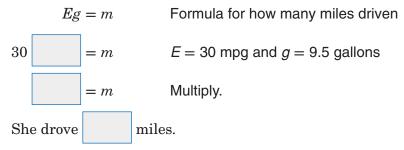
**b.** Solve 12a + 3c = 2ab + 6 for *a*.

#### **EXAMPLE** Use a Formula to Solve Problems

3 a. FUEL ECONOMY A car's fuel economy E (miles per gallon) is given by the formula  $E = \frac{m}{g}$ , where m is the number of miles driven and g is the number of gallons of fuel used. Solve the formula for m.

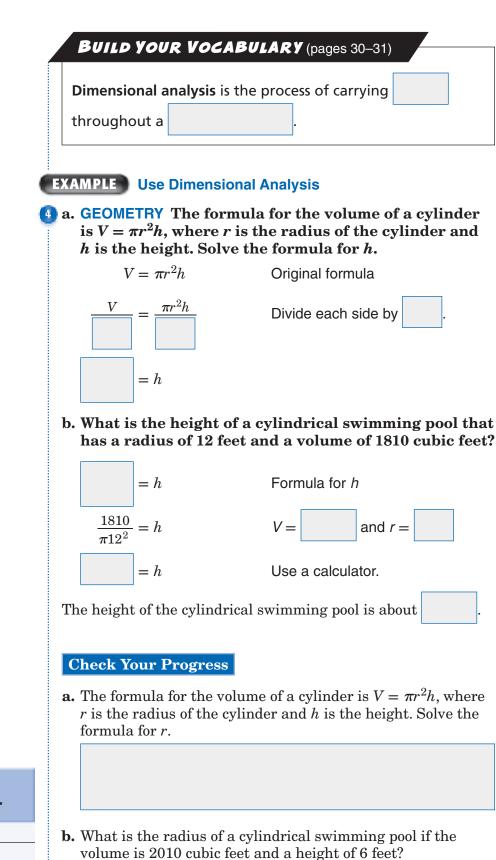


b. FUEL ECONOMY If Claudia's car has an average fuel consumption of 30 miles per gallon and she used 9.5 gallons, how far did she drive?



#### **Check Your Progress**

- a. Refer to Example 3. Solve the formula for g.
- **b.** If Claudia drove 1477 miles and her pickup has an average fuel consumption of 19 miles per gallon, how many gallons of fuel did she use?



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HOMEWORK Assignment

Page(s): Exercises:

2 - 8



# **Weighted Averages**

## MAIN IDEAS

- Solve mixture problems.
- Solve uniform motion problems.

## BUILD YOUR VOCABULARY (pages 30-31)

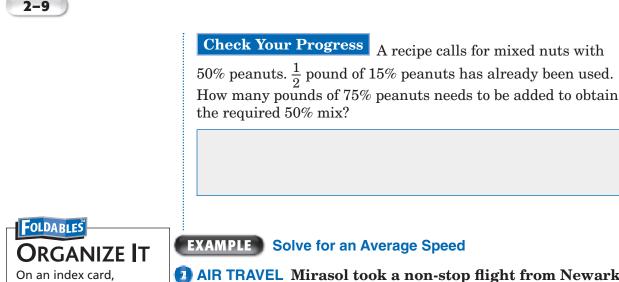
The **weighted average** *M* of a set of data is the sum of the product of the number of units and the value per unit divided by the sum of the number of units.

## EXAMPLE Solve a Mixture Problem with Prices

**PETS** Jeri feeds her cat gourmet cat food that costs \$1.75 per pound. However, food at that price is too expensive so she combines it with cheaper cat food that costs \$0.50 per pound. How many pounds of cheaper food should Jeri buy to go with 5 pounds of gourmet food, if she wants the price to be \$1.00 per pound?

Type of Cat Food	Units (lb)	Price per Unit	Price	
Gourmet cat food				
Cheaper cat food	w	\$0.50	0.5w	
Mixed cat food		\$1.00		
Price of gourmet	-	-	price of mixed cat food.	
8.75 +	0.5w		1.00(5+w)	
$8.75 + 0.5\iota$	v = 1.00(5 +	· w) O	riginal equation	
$8.75 + 0.5\iota$	v =		Distributive Property	
8.75 + 0.5w -	= 5.0 + 1u	v — S	ubtract.	
8.7	5 = 5.0 + 0.8	õw S	mplify.	
8.75 - 5.0	5w - 5.0 S	ubtract.		
3.7	Si	implify.		
7.	5 = w	D	ivide.	

Let w = the number of pounds of cheaper cat food.



2 AIR TRAVEL Mirasol took a non-stop flight from Newark to Austin to visit her grandmother. The 1500-mile trip took three hours and 45 minutes. Because of bad weather, the return trip took four hours and 45 minutes. What was her average speed for the round trip?

To find the average speed for each leg of the trip, rewrite

$$d = rt$$
 as  $r = \frac{d}{t}$ .

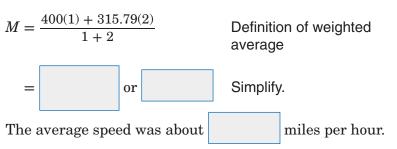
Going

 $r = \frac{d}{t} = \frac{1500 \text{ miles}}{\text{hours}}$  or miles per hour

Returning



Round trip





take notes on mixture

problems and uniform

Solving Linear Equations

motion problems.

Page(s): Exercises: **Check Your Progress** In the morning, when traffic is light, it takes 30 minutes to get to work. The trip is 15 miles through towns. In the afternoon when traffic is a little heavier, it takes 45 minutes. What is the average speed for the round trip?



# **BRINGING IT ALL TOGETHER**

## STUDY GUIDE

FOLDABLES	Vocabulary Puzzlemaker	Build your Vocabulary
Use your <b>Chapter 2 Foldable</b> to help you study for your chapter test.	To make a crossword puzzle, word search, or jumble puzzle of the vocabulary words in Chapter 2, go to: glencoe.com	You can use your completed <b>Vocabulary Builder</b> ( <i>pages 30–31</i> ) to help you solve the puzzle.

2-1 Writing Equations

#### Translate each sentence into an equation.

- **1.** Two times the sum of x and three minus four equals four times x
- **2.** The difference of k and 3 is two times k divided by five.
  - 2-2

## Solving Equations by Using Addition and Subtraction

#### **Complete each sentence.**

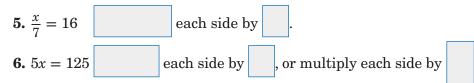
**3.** To solve y - 9 = -30 using the Addition Property of Equality, you

would add to each side.

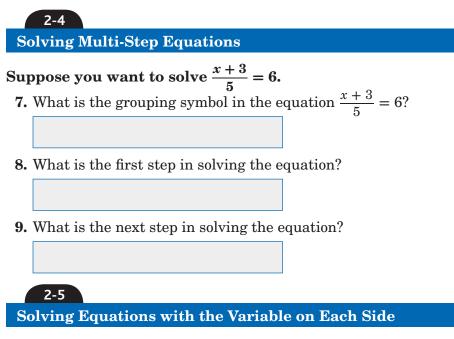
**4.** Write an equation that you could solve by subtracting 32 from each side.

2-3 Solving Equations by Using Multiplication or Division

# Complete the sentence after each equation to tell how you would solve the equation.



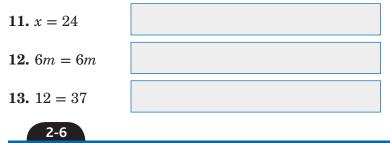
## Chapter 2 BRINGING IT ALL TOGETHER



**10.** When solving 2(3x - 4) = 3(x + 5), why is it helpful first to use the Distributive Property to remove the grouping symbols?

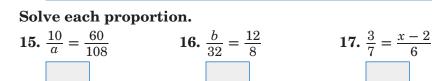


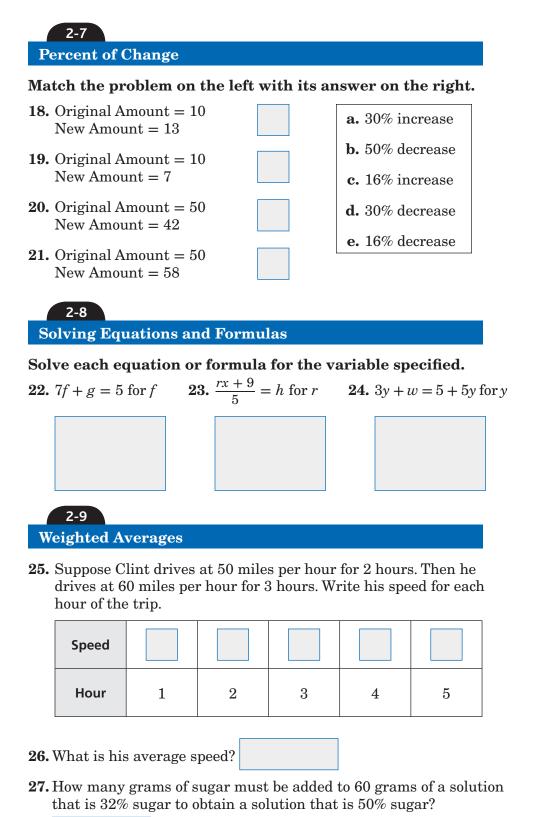
The solutions of three equations are shown in Exercises 11–13. Write a sentence to describe each solution.



## **Ratios and Proportions**

14. A jet flying at a steady speed traveled 825 miles in 2 hours. If you solved the proportion  $\frac{825}{2} = \frac{x}{1.5}$ , what would the answer tell you about the jet?



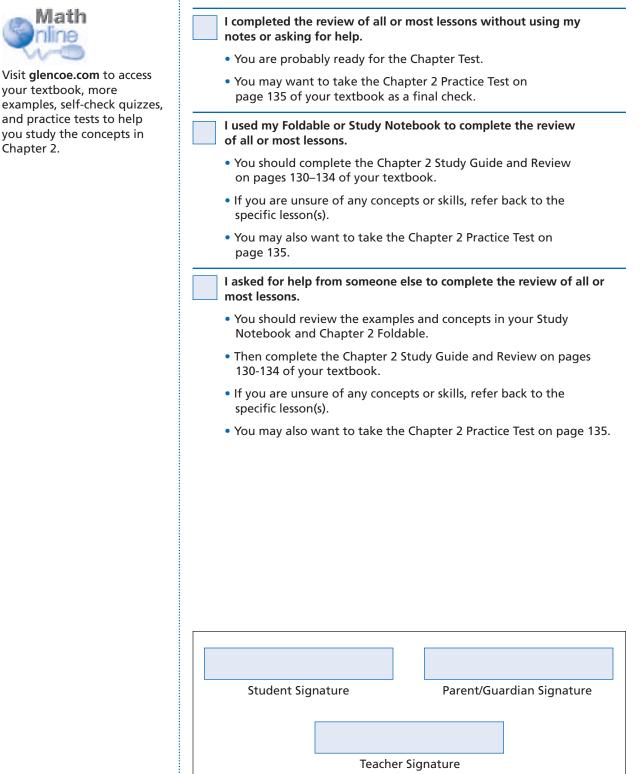




Chapter 2.

# ARE YOU READY FOR THE CHAPTER TEST?

Check the one that applies. Suggestions to help you study are given with each item.

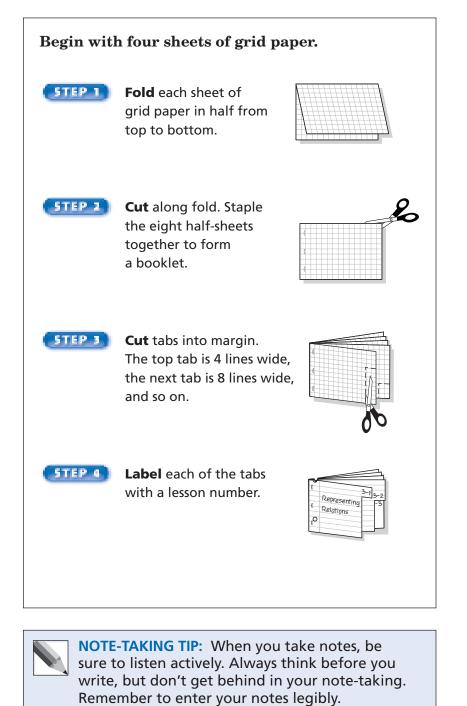




# **Functions and Patterns**

# FOLDABLES

Use the instructions below to make a Foldable to help you organize your notes as you study the chapter. You will see Foldable reminders in the margin of this Interactive Study Notebook to help you in taking notes.



Glencoe Algebra 1 59

Chapter 3



## BUILD YOUR VOCABULARY

This is an alphabetical list of new vocabulary terms you will learn in Chapter 3. As you complete the study notes for the chapter, you will see Build Your Vocabulary reminders to complete each term's definition or description on these pages. Remember to add the textbook page number in the second column for reference when you study.

Vocabulary Term	Found on Page	Definition	Description or Example
arithmetic sequence			
common difference			
function			
function notation			
function value			
inverse			
linear equation			
mapping			

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Vocabulary Term	Found on Page	Definition	Description or Example
sequence			
standard form			
terms			
vertical line test			
x-intercept			
y-intercept			
zero			

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# **Representing Relations**

## **MAIN IDEAS**

- Represent relations as sets of ordered pairs, tables, mappings, and graphs.
- Find the inverse of a relation.

## **BUILD YOUR VOCABULARY** (pages 60-61)

A mapping illustrates how each element of the

paired with an element in the

The inverse of any relation is obtained by switching the

in each

## **EXAMPLE** Represent a Relation

**1** Express the relation  $\{(4, 3), (-2, -1), (-3, 2), (2, -4), (-3, 2), (2, -4), (-3, 2), (-3, 2), (-3, 2), (-3, 2), (-3, 2), (-3, 2), (-3, 2), (-3, 2), (-3, 2), (-3, 2), (-3, 2), (-3, 2), (-3, 2), (-3, 2), (-3, 2), (-3, 2), (-3, 2), (-3, 2), (-3, 2), (-3, 2), (-3, 2), (-3, 2), (-3, 2), (-3, 2), (-3, 2), (-3, 2), (-3, 2), (-3, 2), (-3, 2), (-3, 2), (-3, 2), (-3, 2), (-3, 2), (-3, 2), (-3, 2), (-3, 2), (-3, 2), (-3, 2), (-3, 2), (-3, 2), (-3, 2), (-3, 2), (-3, 2), (-3, 2), (-3, 2), (-3, 2), (-3, 2), (-3, 2), (-3, 2), (-3, 2), (-3, 2), (-3, 2), (-3, 2), (-3, 2), (-3, 2), (-3, 2), (-3, 2), (-3, 2), (-3, 2), (-3, 2), (-3, 2), (-3, 2), (-3, 2), (-3, 2), (-3, 2), (-3, 2), (-3, 2), (-3, 2), (-3, 2), (-3, 2), (-3, 2), (-3, 2), (-3, 2), (-3, 2), (-3, 2), (-3, 2), (-3, 2), (-3, 2), (-3, 2), (-3, 2), (-3, 2), (-3, 2), (-3, 2), (-3, 2), (-3, 2), (-3, 2), (-3, 2), (-3, 2), (-3, 2), (-3, 2), (-3, 2), (-3, 2), (-3, 2), (-3, 2), (-3, 2), (-3, 2), (-3, 2), (-3, 2), (-3, 2), (-3, 2), (-3, 2), (-3, 2), (-3, 2), (-3, 2), (-3, 2), (-3, 2), (-3, 2), (-3, 2), (-3, 2), (-3, 2), (-3, 2), (-3, 2), (-3, 2), (-3, 2), (-3, 2), (-3, 2), (-3, 2), (-3, 2), (-3, 2), (-3, 2), (-3, 2), (-3, 2), (-3, 2), (-3, 2), (-3, 2), (-3, 2), (-3, 2), (-3, 2), (-3, 2), (-3, 2), (-3, 2), (-3, 2), (-3, 2), (-3, 2), (-3, 2), (-3, 2), (-3, 2), (-3, 2), (-3, 2), (-3, 2), (-3, 2), (-3, 2), (-3, 2), (-3, 2), (-3, 2), (-3, 2), (-3, 2), (-3, 2), (-3, 2), (-3, 2), (-3, 2), (-3, 2), (-3, 2), (-3, 2), (-3, 2), (-3, 2), (-3, 2), (-3, 2), (-3, 2), (-3, 2), (-3, 2), (-3, 2), (-3, 2), (-3, 2), (-3, 2), (-3, 2), (-3, 2), (-3, 2), (-3, 2), (-3, 2), (-3, 2), (-3, 2), (-3, 2), (-3, 2), (-3, 2), (-3, 2), (-3, 2), (-3, 2), (-3, 2), (-3, 2), (-3, 2), (-3, 2), (-3, 2), (-3, 2), (-3, 2), (-3, 2), (-3, 2), (-3, 2), (-3, 2), (-3, 2), (-3, 2), (-3, 2), (-3, 2), (-3, 2), (-3, 2), (-3, 2), (-3, 2), (-3, 2), (-3, 2), (-3, 2), (-3, 2), (-3, 2), (-3, 2), (-3, 2), (-3, 2), (-3, 2), (-3, 2), (-3, 2), (-3, 2), (-3, 2), (-3, 2), (-3, 2), (-3, 2), (-3, 2), (-3, 2), (-3, 2), (-3, 2), (-3, 2), (-$ (0, -4)} as a table, a graph, and a mapping.

## **Table**

List the set of *x*-coordinates in the first column and the corresponding y-coordinates in the second

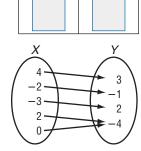
## Graph

Graph each ordered pair on a coordinate plane.

		-	y		
_	-				_
-		0			x
			-	-	

## Mapping

List the *x* values in set *X* and the *y* values in set Y. Draw an arrow from each x value in X to the corresponding *y* value in *Y*.

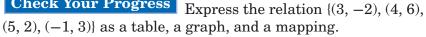


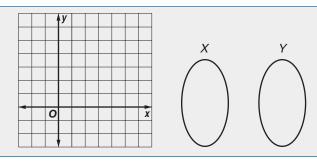
X

is

У

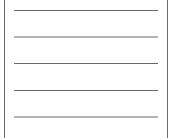
## Check Your Progress







number. (Prerequisite Skill)





## EXAMPLE Use a Relation

## **2** OPINION POLLS

The table shows the percent of people satisfied with the way things were going in the U.S. at the time of the survey.

ıe	Year	1992	1995	1998	2001
	Percent Satisfied	21	32	60	51

#### a. Determine the domain and range of the relation.

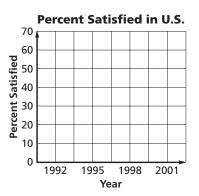


#### b. Graph the data.

from

The values of the *x*-axis need to go from 1992 to 2001. Begin at 1992 and extend to 2001 to include all of the data.

The values on the *y*-axis need to go from 21 to 60. Begin at 0 and extend to 70. You can use units of 10.



# c. What conclusions might you make from the graph of the data?

Americans became more satisfied with the country

, but the percentage dropped from

**Check Your Progress** The table shows the approximate world population of the Indian Rhinoceros from 1982 to 1998.

Indian Rhinoceros Population						
Year 1982 1986 1990 1994 1998						
Population	1000	1700	1700	1900	2100	

**a.** Determine the domain and range of the relation.

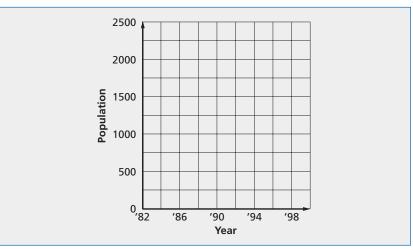


## KEY CONCEPT

Inverse of a Relation Relation Q is the inverse of relation *S* if and only if for every ordered pair (a, b) in S, there is an ordered pair (b, a) in Q.

FOLDABLES Under the tab for Lesson 3-1. Write a relation with four ordered pairs. Then find the inverse of the relation.

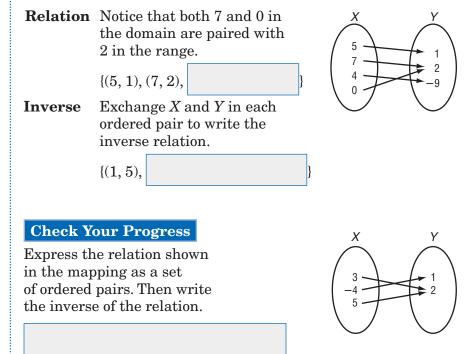
**b.** Graph the data.



c. What conclusions might you make from the graph of the data?

## **EXAMPLE** Inverse Relation

#### Express the relation shown in the mapping as a set of ordered pairs. Then write the inverse of the relation.



HOMEWORK ASSIGNMENT

Page(s): Exercises: **Representing Functions** 

#### MAIN IDEAS

3-2

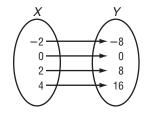
- Determine whether a relation is a function.
- Find function values.

#### **KEY CONCEPT**

A **function** is a relation in which each element of the domain is paired with exactly one element of the range.

**FOLDABLES** Use the tab for Lesson 3–2. Explain two ways to determine whether a relation is a function.

0	a. Determine	whether e	ach rela	tion is	a function	L.
	Explain.					



**EXAMPLE** Identify Functions

This is a function because the mapping shows each element of the

paired with exactly one

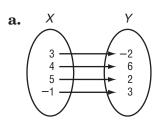
member of the

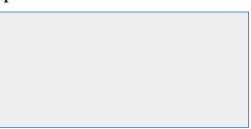
b.	x	У
	-7	-12
	-4	-9
	2	-3
	5	0

This table represents a function because the table shows each element of the domain paired with

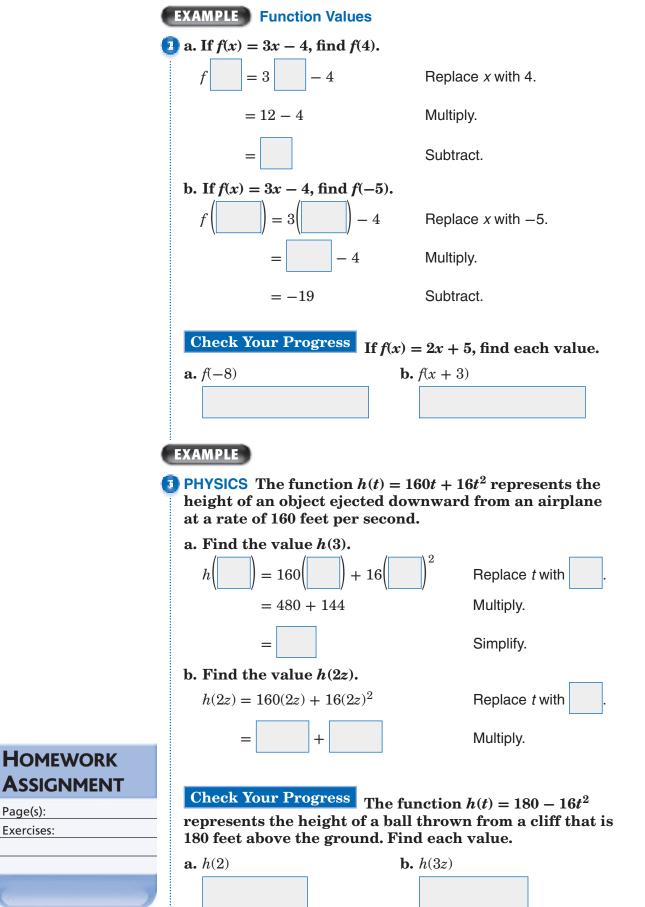
element of the range.

## **Check Your Progress** Determine whether each relation is a function. Explain.





b.	x	У
	3	2
	1	-2
	2	-4
	3	-1



Page(s):

Exercises:



### **Linear Functions**

#### **MAIN IDEAS**

- Determine whether an equation is linear.
- Graph linear equations.

#### **KEY CONCEPT**

Standard Form of a Linear Equation The standard form of a linear equation is  $Ax + By = C_{t}$ where  $A \ge 0$ , A and B are not both zero, and A, B, and C are integers whose greatest common factor is 1.

Lesson 3–3 tab, write an example of a linear equation and one that is not linear. Draw a graph of the linear equation.

FOLDABLES On the

**BUILD YOUR VOCABULARY** (pages 60-61)

A linear equation is the equation of a line. When an equation is written in the form Ax + By = C, it is said to be in standard form.

#### **EXAMPLE** Identifying Linear Equations

#### Determine whether each equation is a linear equation. If so, write the equation in standard form.

#### a. 5x + 3y = z + 2

Rewrite the equation with the variables on one side.

5x + 3y = z + 2	Original equation
5x + 3y - z = z + 2 - z	Subtract.
5x + 3y - z = 2	Simplify.

different variables on the left side Since there are

of the equation, it

be written in the form

Ax + By = C. This is not a

### b. $\frac{3}{4}x = y + 8$

Rewrite the equation with the variables on one side.

$\frac{3}{4}x = y + 8$	Original equation
$\frac{3}{4}x - y = y + 8 - y$	Subtract <i>y</i> from each side.
$\frac{3}{4}x - y = 8$	Simplify.

Write the equation with integer coefficients.

$$\frac{3}{4}x - y = 8$$

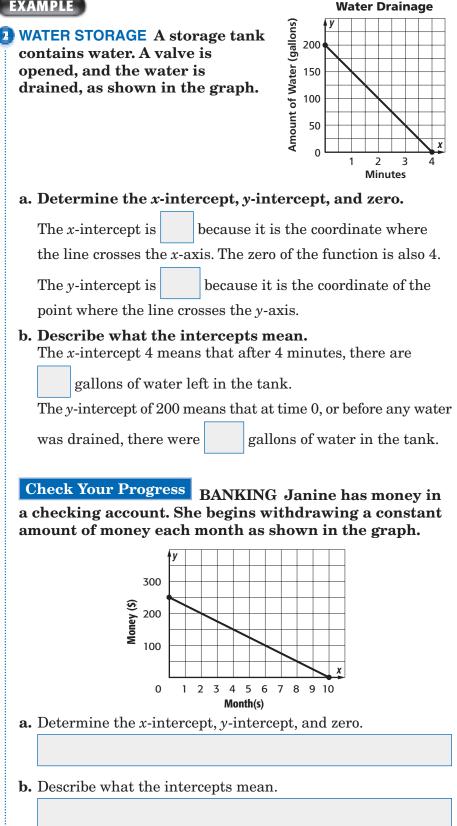
$$4\left(\frac{3}{4}x\right) - 4(y) = 8(4)$$
Multiply each side by 4.
$$3x - 4y = 32$$
Simplify.

plify.

The equation is now in standard form where A =

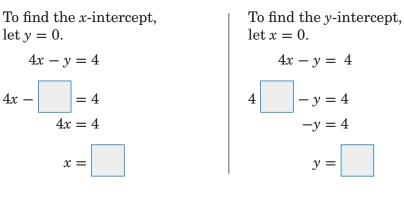
, and C =This is a B =equation.

#### EXAMPLE



#### EXAMPLE Graph Using Intercepts

#### **(1)** Graph 4x - y = 4 using the *x*-intercept and *y*-intercept.



The *x*-intercept is 1, so the graph

intersects the *x*-axis at

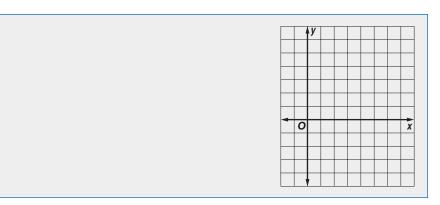
The *y*-intercept is -4, so the graph

intersects the *y*-axis at

Plot these points. Then draw a line that connects them.

		-	y		
					_
		0			X

**Check Your Progress** Graph 2x + 5y = 10 using the *x*-intercept and *y*-intercept.





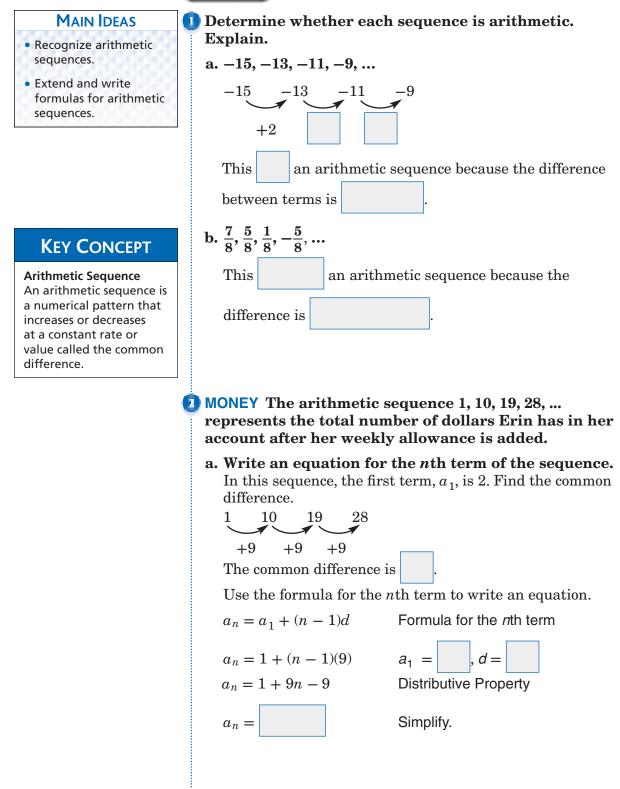
Homework Assignment

Page(s):

### **Arithmetic Sequences**

3-4

#### **EXAMPLES** Identify Arithmetic Sequences



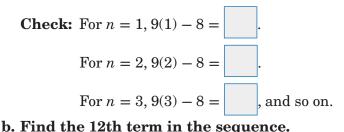
#### **KEY CONCEPT**

nth Term of an **Arithmetic Sequence** The *n*th term  $a_n$  of an arithmetic sequence with first term  $a_1$  and common difference *d* is given by  $a_n = a_1 + (n - 1)d$ , when n is a positive integer.

FOLDABLES Use the tab for Lesson 3-4. Write the general form for an arithmetic sequence. Explain what each of the variables means.

#### **KEY CONCEPT**

Writing Arithmetic Sequences Each term of an arithmetic sequence after the first term can be found by adding the common difference to the preceding term.



Replace *n* with 12 in the equation written in part **a**.

$$a_n = 9n - 8$$
Equation for the *n*th term $a_{25} = 9(12) - 8$ Replace *n* with

 $a_{25} =$ 

Replace *n* with

Simplify.

c. Graph the first five terms of the sequence.

n	9n — 8	a <sub>n</sub>	(n, a <sub>n</sub> )
1	9(1) - 8	1	(1, 1)
2	9(2) - 8	10	(2, 10)
3	9(3) - 8	19	(3, 19)
4	9(4) - 8	28	(4, 28)
5	9(5) - 8	37	(5, 37)

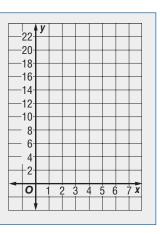
10	a <sub>n</sub>					
40						
35			-	-		
30						
40 35 30 25 20						
20						
			-	-		
15				-		
10						
5						
			_		<u> </u>	
0	1	Ż	3	4 !	56	5 <b>n</b>

The points fall on a line. The graph of an arithmetic

sequence is

**Check Your Progress MONEY** The arithmetic sequence 2, 7, 12, 17... represents the total number of pencils Claire has in her collection after she goes to her school store each week.

- **a.** Write an equation for the *n*th term of the sequence.
- **b.** Find the 12th term in the sequence
- **c.** Graph the first five terms of the sequence.



HOMEWORK ASSIGNMENT

Page(s):

Exercises:

## **Proportional and Nonproportional Relationships**

ENERGY The table shows the number of

hour of driving.

miles driven for each

#### **EXAMPLE** Proportional Relationships



Look for a pattern.

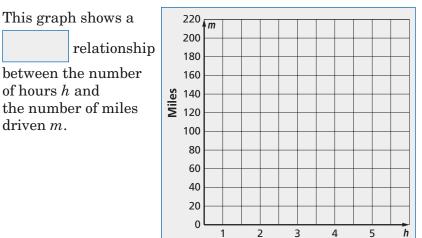
3-5

• Write an equation given some of the solutions.

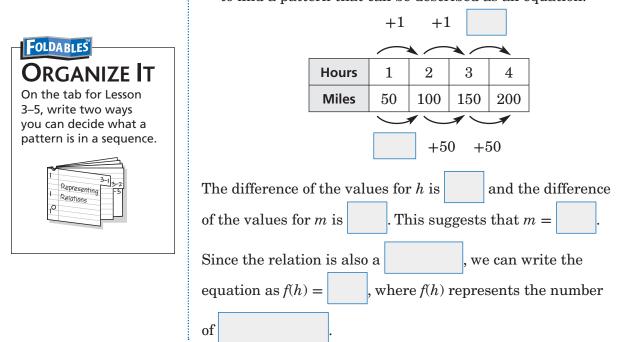
Hours	1	2	3	4
Miles	50	100	150	200

Hours

a. Graph the data. What conclusion can you make about the relationship between the number of hours driving and the number of miles driven?



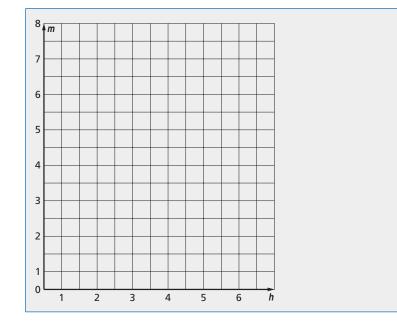
**b. Write an equation to describe this relationship.** Look at the relationship between the domain and the range to find a pattern that can be described as an equation.



# **Check Your Progress** The table below shows the number of miles walked for each hour of walking.

Hours	1	2	3	4	5
Miles	1.5	3	4.5	6	7.5

**a.** Graph the data. What conclusion can you make about the relationship between the number of miles and the time spent walking?



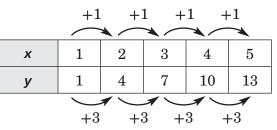
**b.** Write an equation to describe the relationship.

#### EXAMPLE

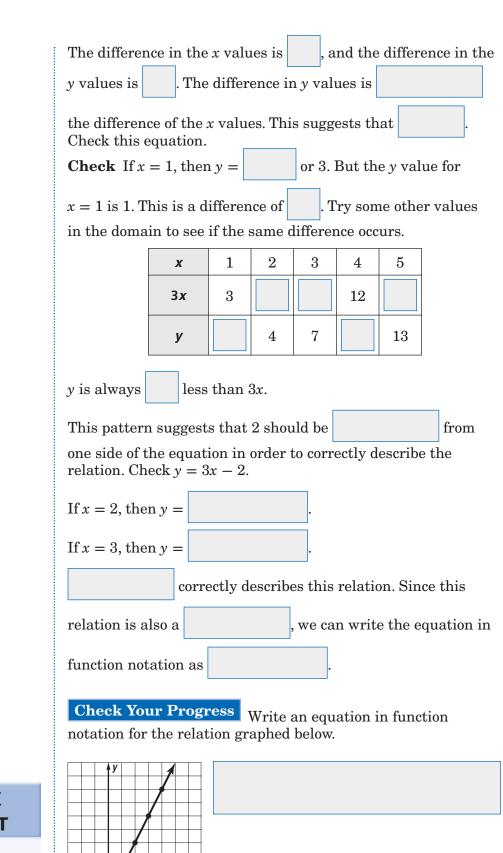
#### Write an equation in function notation for the relation graphed below.

	1 <sup>4</sup>					
12	<u> </u>					<u> </u>
40					L	
	개				-	
	3					
	1					
	й—					
	1 <u> </u>		-			
-2		]				
	4			-		
	<u> </u>					-
- C	) <sup>-</sup>	1 2	2 3	3 4	1 5	x
	ł					

Make a table of ordered pairs for several points of the graph.



(continued on the next page)



X

Ο

HOMEWORK Assignment

Page(s): Exercises:

3-5

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### **BRINGING IT ALL TOGETHER**

### STUDY GUIDE

	Vocabulary Puzzlemaker	Build your Vocabulary					
Use your <b>Chapter 3 Foldable</b> to help you study for your chapter test.	To make a crossword puzzle, word search, or jumble puzzle of the vocabulary words in Chapter 3, go to: glencoe.com	You can use your completed <b>Vocabulary Builder</b> ( <i>pages 60–61</i> ) to help you solve the puzzle.					

#### 3-1

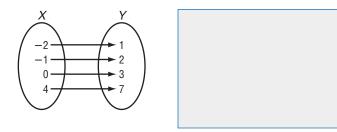
**Representing Relations** 

- xy0-214-35-20
- **2.** Write the inverse of the relation  $\{(1, 2), (2, 4), (3, 6), (4, 8)\}$ .

#### **Representing Functions**

3-2

**3.** Describe how the mapping shows that the relation represented is a function.





3-3 Linear Functions

Determine whether each equation is a linear equation. If so, write the equation in standard form.

	Equation	Linear or nonlinear?	Standard Form
4.	4xy + 2y = 7		
5.	$\frac{x}{5} - \frac{4y}{3} = 2$		

3-4 Arithmetic Sequences

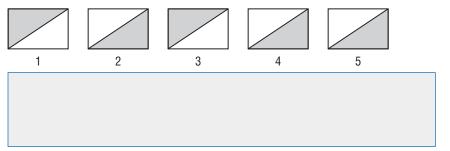
Complete the table.

3-5

	Pattern	Is the sequence increasing or decreasing?	Is there common difference? If so, what is it?
6.	55, 50, 45, 40,		
7.	1, 2, 4, 9, 16,		
8.	$\frac{1}{2}, 0, -\frac{1}{2}, -1, \dots$		

**Proportional and Nonproportional Relationships** 

9. Explain why Figure 5 does not follow the pattern below.



**10.** Write the next 3 terms of the sequence  $1, 5, 25, 125, \ldots$ .



### ARE YOU READY FOR THE CHAPTER TEST?



Visit glencoe.com to access your textbook, more examples, self-check quizzes, and practice tests to help you study the concepts in Chapter 3. Check the one that applies. Suggestions to help you study are given with each item.

I completed the review of all or most lessons without using my notes or asking for help.

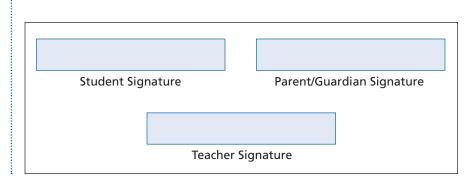
- You are probably ready for the Chapter Test.
- You may want to take the Chapter 3 Practice Test on page 181 of your textbook as a final check.

I used my Foldables or Study Notebook to complete the review of all or most lessons.

- You should complete the Chapter 3 Study Guide and Review on pages 177–180 of your textbook.
- If you are unsure of any concepts or skills, refer back to the specific lesson(s).
- You may also want to take the Chapter 3 Practice Test on page 181.

I asked for help from someone else to complete the review of all or most lessons.

- You should review the examples and concepts in your Study Notebook and Chapter 3 Foldable.
- Then complete the Chapter 3 Study Guide and Review on pages 177–180 of your textbook.
- If you are unsure of any concepts or skills, refer back to the specific lesson(s).
- You may also want to take the Chapter 3 Practice Test on page 181.

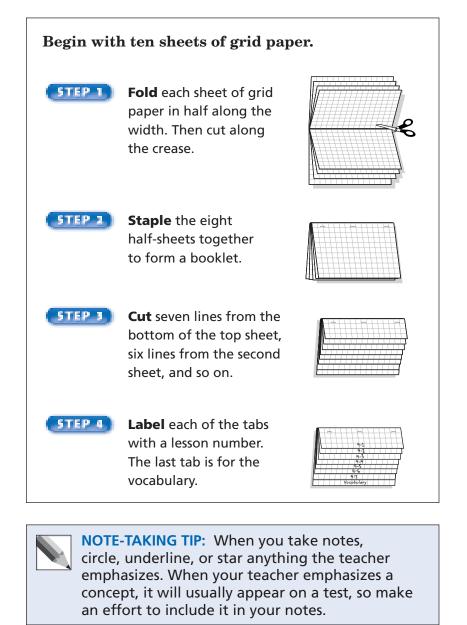




## **Analyzing Linear Equations**

### **FOLDABLES**

Use the instructions below to make a Foldable to help you organize your notes as you study the chapter. You will see Foldable reminders in the margin of this Interactive Study Notebook to help you in taking notes.





#### BUILD YOUR VOCABULARY

This is an alphabetical list of new vocabulary terms you will learn in Chapter 4. As you complete the study notes for the chapter, you will see Build Your Vocabulary reminders to complete each term's definition or description on these pages. Remember to add the textbook page number in the second column for reference when you study.

Vocabulary Term	Found on Page	Definition	Description or Example
best-fit line			
constant of variation			
direct variation			
family of graphs			
line of fit			
linear <u>extrapolation</u> [ihk·stra·puh·LAY·shun]			
linear <u>intrapolation</u> [ihn·tuhr·puh·LAY·shun]			
negative <u>correlation</u> [kawr·uh·LAY·shun]			
parallel lines			
parent graph			

Vocabulary Term	Found on Page	Definition	Description or Example
perpendicular lines			
[puhr·puhn·DIH·kyuh·luhr]			
point-slope form			
positive correlation			
rate of change			
scatter plot			
slope			
slope-intercept form			
[IHN·tuhr·sehpt]			



### **Rate of Change and Slope**

#### BUILD YOUR VOCABULARY (pages 80-81)

#### MAIN IDEAS

- Use rate of change to solve problems.
- Find the slope of a line.

The **rate of change** tells, on average, how a quantity is changing over time.

The **slope** of a line is a number determined by any two points on the line.

#### EXAMPLE

#### **KEY CONCEPT**

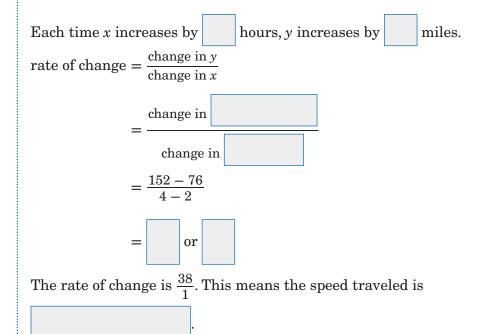
**Slope of a Line** The slope of a line is the ratio of the rise to the run.

#### FOLDABLES

Write the formula for finding the slope of a line under the tab for Lesson 4-1.

DRIVING TIME The table shows how the distance traveled changes with the number of hours driven. Use the table to find the rate of change. Explain the meaning if the rate of change.

Time Driving (h)	Distance Traveled (mi) <i>y</i>
2	76
4	152
6	228



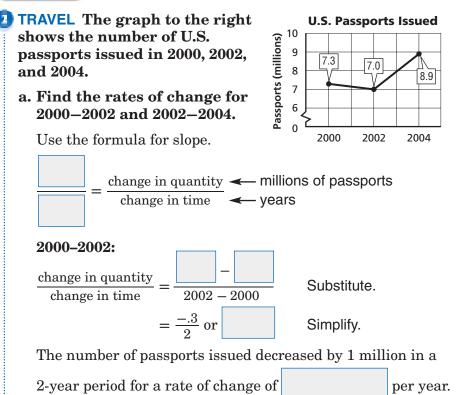
**Check Your Progress CELL PHONE** The table shows how the cost changes with the number of minutes used. Use the table to find the rate of change. Explain the meaning of the rate of change.

4 - 1

Minutes Used <i>x</i>	Cost (\$) <i>y</i>
20	1
40	2
60	3

- A rate of change is  $\frac{.05}{1}$ ; This means that it costs \$0.05 per minute to use the cell phone.
- **B** rate of change is  $\frac{5}{1}$ ; This means that it costs \$5 per minute to use the cell phone.
- C rate of change is  $\frac{.05}{1}$ ; This means that it costs \$0.50 per minute to use the cell phone.
- **D** rate of change is  $\frac{.20}{1}$ ; This means that it costs \$0.20 per minute to use the cell phone.

#### EXAMPLE



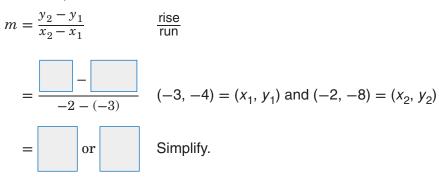
	$\frac{2002-2004:}{\text{change in quantity}}_{\text{change in time}} = \frac{2004-2002}{2004-2002}$ Substitute.
	$=\frac{1.8}{2}$ or Simplify.
	Over this 2-year period, the number of U.S. passports
	issued by 1.8 million for a rate of change
	of per year.
	b. Explain the meaning of the rate of change in each case.
	For 2000–2002, on average, fewer passports
	were issued each year than the last. For 2002–2004, on
	average, more passports were issued each year
	than the last.
	<ul> <li>c. How are the different rates of change shown on the graph?</li> <li>The first rate of change is, and the line goes on the graph; the second rate of change is, and the graph goes</li> </ul>
REVIEW IT Describe how you find cross products. (Lesson 2-6)	
	Check four Progress
	AIRLINES The graph shows the number of airplane
	departures in the United8.0States in recent years.7.5
	departures in the United States in recent years. a. Find the rates of change for 1990–1995 and 1995–2000.
]	<b>b.</b> Explain the meaning of the slope in each case.



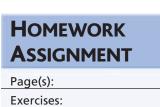
c. How are the different rates of changes shown on the graph?

#### EXAMPLE Finding Slope

**5** Find the slope of the line that passes through (-3, -4)and (-2, -8).

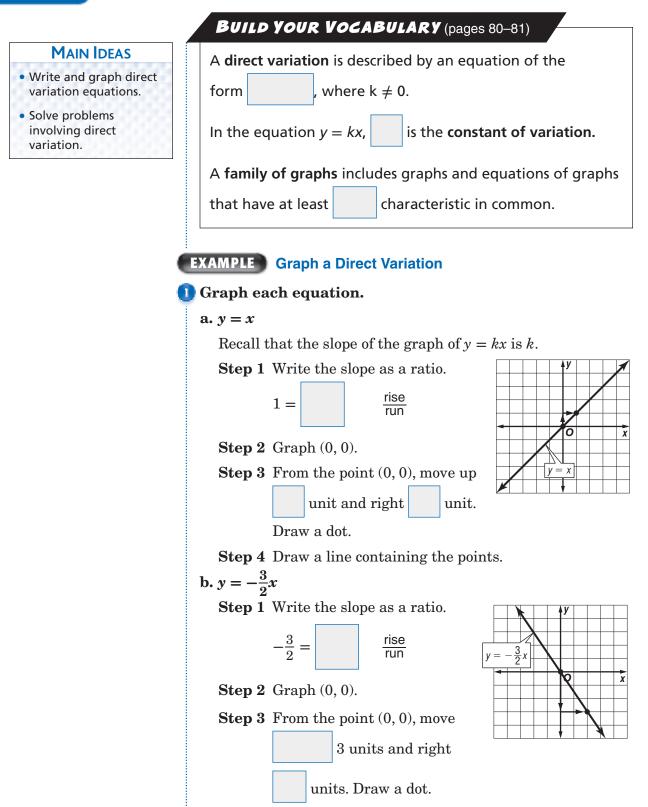


**Check Your Progress** Find the slope of the line that passes through (-3, 4) and (4, 4).

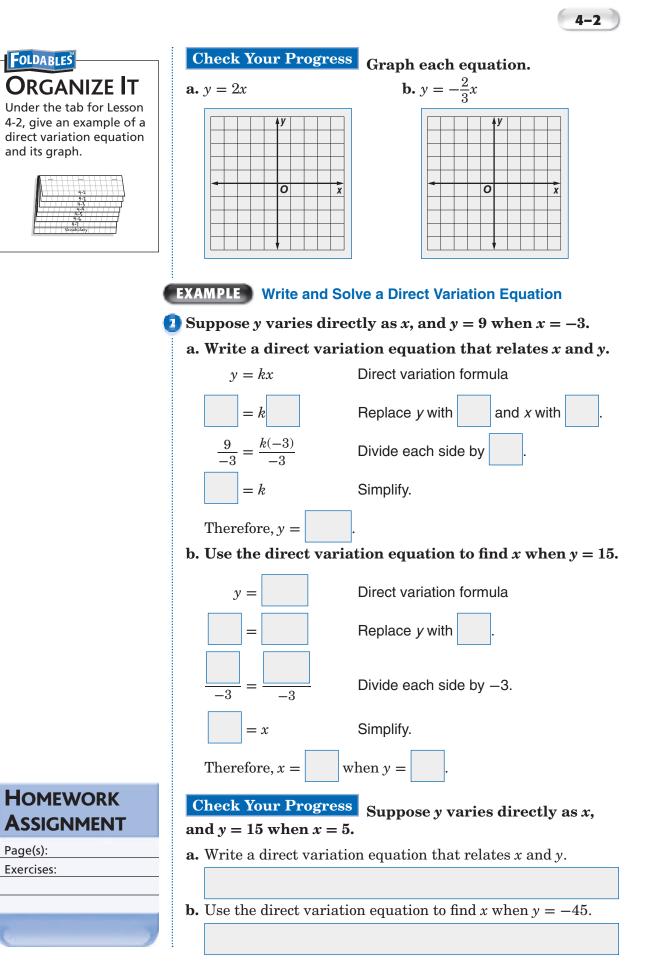




### **Slope and Direct Variation**

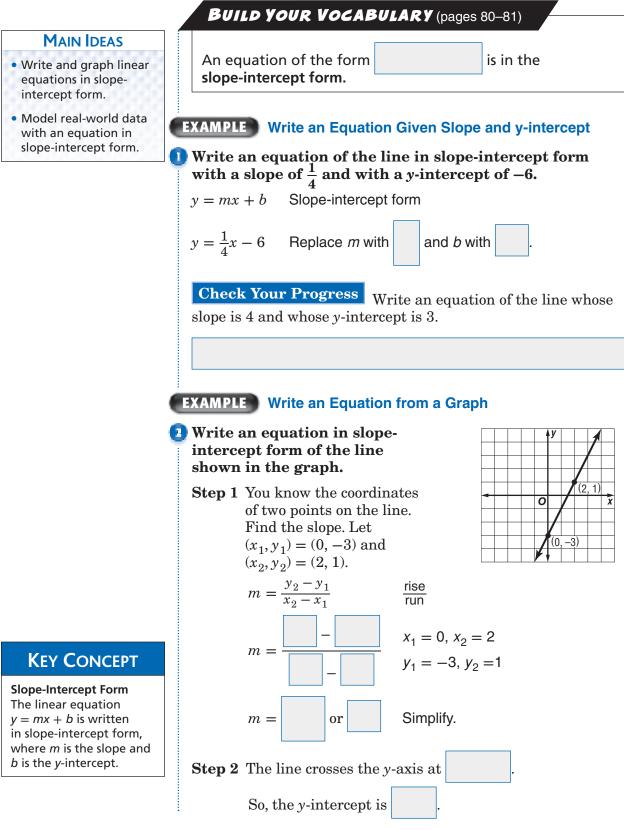


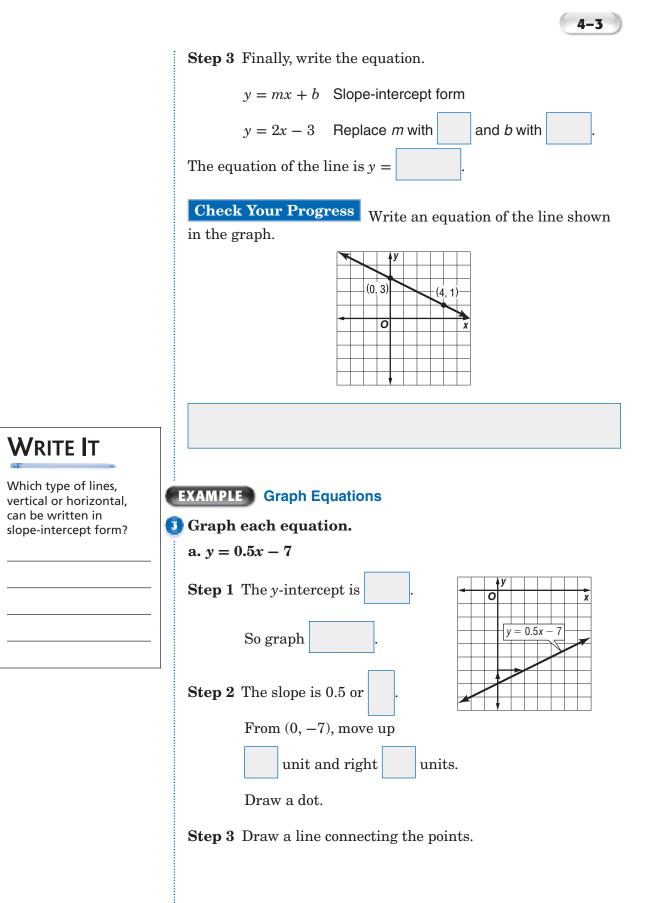
**Step 4** Draw a line containing the points.



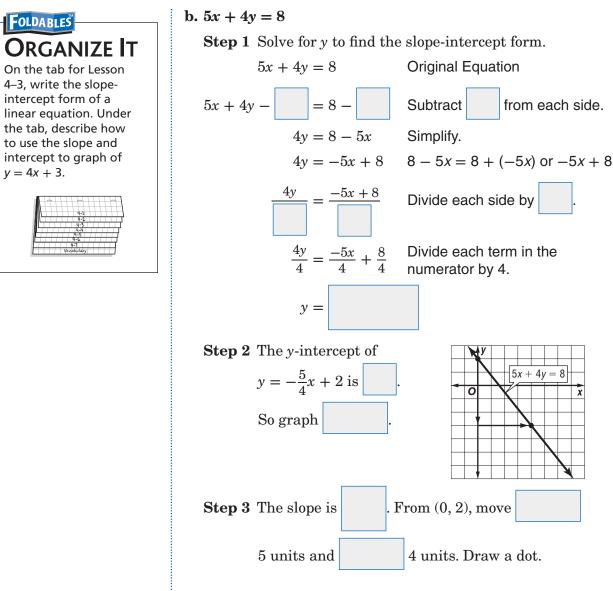


### **Graphing Equations in Slope-Intercept Form**









Step 4 Draw a line connecting the points.

C	hec	k Y	lou	ır I	Pro	)g	re	ss	G	ra	pł	ı e	a	ch	<b>e</b>	q	ua	ıti	01	n.	
<b>a.</b>	<i>y</i> =	2x	_ 4	1							b	. 3	x	+	2	y =	=	6			
				y															y		
														_							
			0					x						1				0			
			,															1	,		

### HOMEWORK Assignment

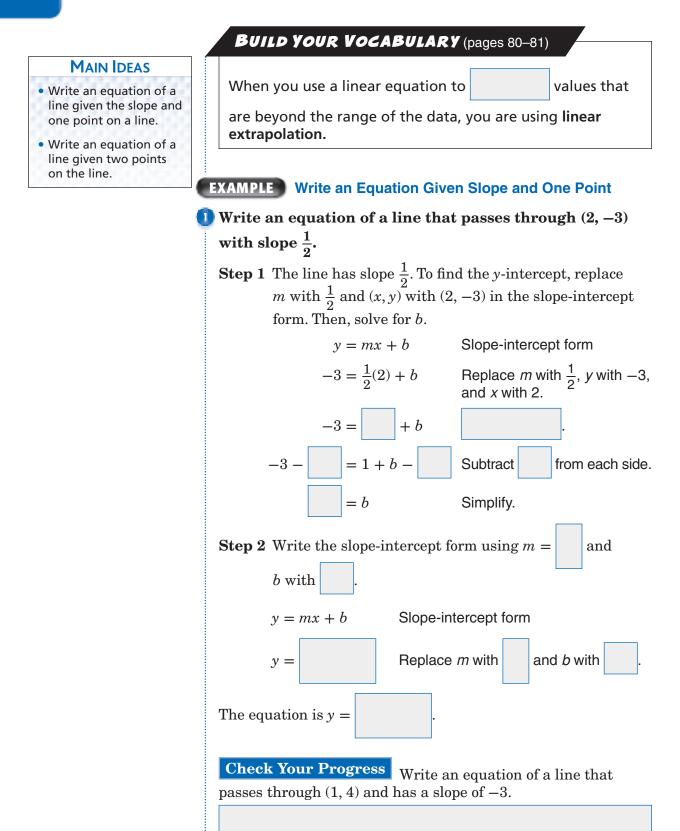
Page(s):

Exercises:

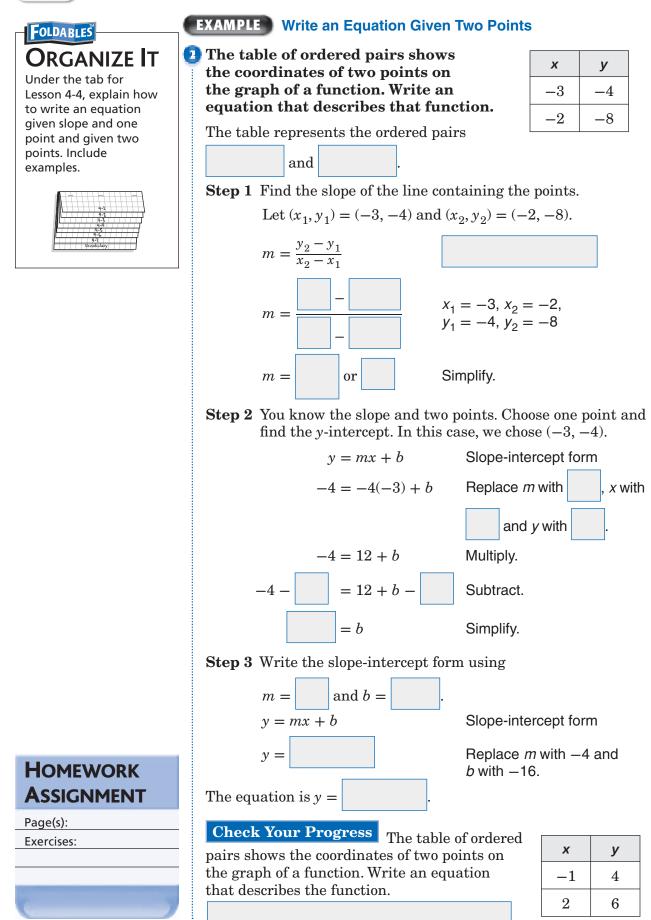
X



### Writing Equations in Slope-Intercept Form









### Writing Equations in Point-Slope Form

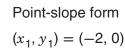
#### **MAIN IDEAS**

- Write the equation of a line in point-slope form.
- Write linear equations
- in different forms.

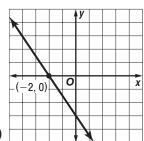
**EXAMPLE** Write an Equation Given Slope and a Point

Write the point-slope form of an equation for a line that passes through (-2, 0) with slope  $-\frac{3}{2}$ .

$$y - y_1 = m(x - x_1)$$
  
$$y - 0 = -\frac{3}{2}[x - (-2)]$$



Simplify.



The equation is y =

 $y - y_1 = m(x - x_1)$ 

=

= 0

The equation is

y =

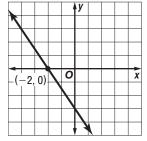


#### EXAMPLE Write an Equation Given Slope and a Point

2) Write the point-slope form of an equation for a horizontal line that passes through (0, 5).

```
Point-slope form
```

 $(x_1, y_1) = (0, 5)$ 



#### **Check Your Progress**

**a.** Write the point-slope form of an equation for a line that passes through (4, -3) with slope -2.

Simplify.

**b.** Write the point-slope form of an equation for a horizontal line that passes through (-3, -4).

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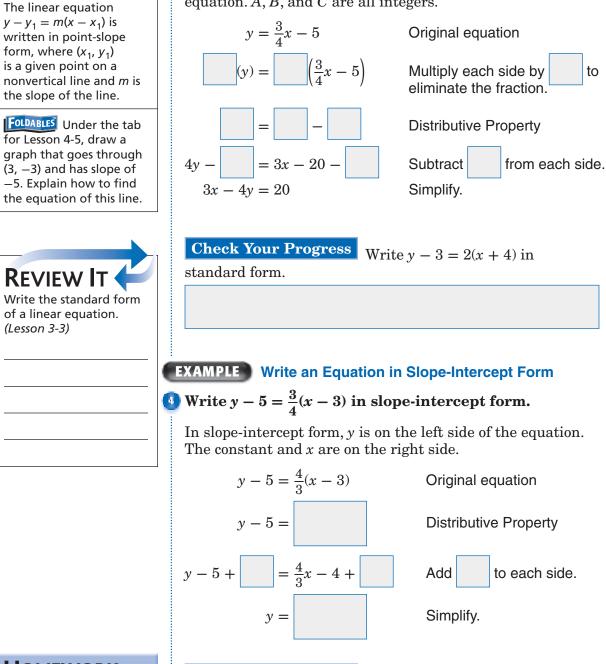
#### EXAMPLE Write an Equation in Standard Form

**1** Write  $y = \frac{3}{4}x - 5$  in standard form.

#### **KEY CONCEPT**

**Point-Slope Form** 

In standard form, the variables are on the left side of the equation. A, B, and C are all integers.



Homework Assignment

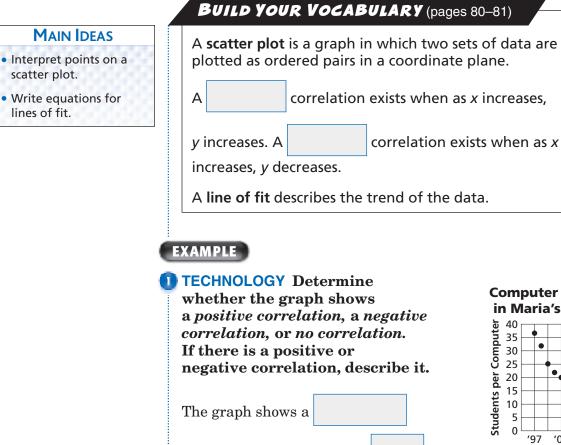
**Check Your Progress** Write 3x + 2y = 6 in slope-intercept form.

Page(s):

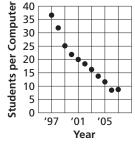
Exercises:



### Statistics: Scatter Plots and Lines of Fit







correlation. With each year,

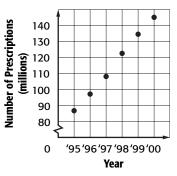
computers are in Maria's school,

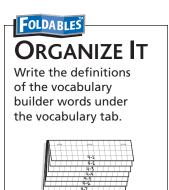
making the students per computer rate

#### **Check Your Progress**

**Determine whether the** graph shows a *positive* correlation, a negative correlation, or no correlation. If there is a positive or negative correlation, describe it.

#### **Mail-Order Prescriptions**







#### **EXAMPLE** Make and Evaluate Predictions



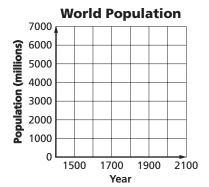
The table shows the world's population growing at a

rapid rate.

Year	Population (millions)
1650	500
1850	1000
1930	2000
1975	4000
1998	5900

a. Draw a scatter plot and determine what relationship exists, if any, in the data.

Let the independent variable x be the year and let the dependent variable y be the population (in millions).



The scatter plot seems to indicate that as the year



the population . There is a

correlation between the two variables.

#### b. Draw a line of fit for the scatter plot.

No one line will pass through all of the data points. Draw a

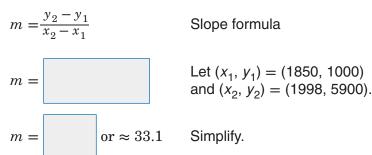
that passes to the points. A line is shown

in the scatter plot.

## c. Write the slope-intercept form of an equation for the equation for the line of fit.

The line of fit shown passes through the data points (1850, 1000) and (1998, 5900).

Step 1 Find the slope.



**Step 2** Use m = 33.1 and either the point-slope form or the slope-intercept form to write the equation. You can use either data point. We chose (1850, 1000).

4-6

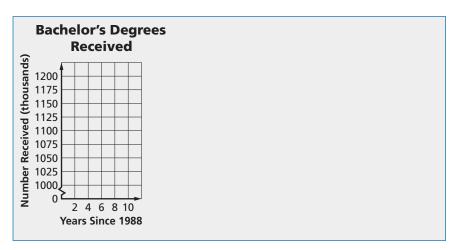
Point-slope form	Slope-intercept form				
$y - y_1 = m(x - x_1)$	y = mx + b				
$y - 1000 \approx 33.1(x - 1850)$	$1000 \approx 33.1(1850) + b$				
$y - 1000 \approx 33.1x - 61,235$	$1000\approx 61{,}235+b$				
$y \approx$	$-60,235 \approx b$				
	<i>y</i> ≈				
The equation of the line is $y \approx$					

**Check Your Progress** The table shows the number of bachelor's degrees received since 1988.

Years since 1998	2	4	6	8	10
Bachelor's Degrees Received (thousands)	1051	1136	1169	1165	1184

Source: National Center for Education Statistics

- **a.** Draw a scatter plot and determine what relationship exists, if any, in the data.
- **b.** Draw a line of best fit for the scatter plot.
- **c.** Write the slope-intercept form of an equation for the line of fit.





HOMEWORK

**ASSIGNMENT** 

Page(s): Exercises:



### **Geometry: Parallel and Perpendicular Lines**

#### MAIN IDEAS

- Write an equation of the line that passes through a given point, parallel to a given line.
- Write an equation of the line that passes through a given point, perpendicular to a given line.

#### KEY CONCEPT

Parallel Lines in a Coordinate Plane Two nonvertical lines are parallel if they have the same slope. All vertical lines are parallel.

#### BUILD YOUR VOCABULARY (pages 80-81)

Lines in the same plane that do not parallel lines.

Lines that intersect at

perpendicular lines.

#### EXAMPLE Parallel Line Through a Given Point

Write the slope-intercept form of an equation for the line that passes through (4, -2) and is parallel to the graph

of 
$$y = \frac{1}{2}x - 7$$
.

The line parallel to y = x - 7 has the same slope,  $\frac{1}{2}$ . Replace *m* with  $\frac{1}{2}$  and (x, y) with (4, -2) in the point-slope form.

$$y - y_1 = m(x - x_1)$$
Point-slope form $y - (-2) = \frac{1}{2}(x - 4)$ Replace  $m$  with  $\frac{1}{2}$ ,  $y$  with  $-2$ ,  
and  $x$  with 4. $y = \frac{1}{2}(x - 4)$ Simplify. $y + 2 =$ Distributive Property $y + 2 - 1 = \frac{1}{2}x - 2 - 1$ Subtract 1 from each side. $y =$ Write the equation in slope-intercept form.

**Check Your Progress** Write the slope-intercept form of an equation for the line that passes through (2, 3) and is parallel to the graph of  $y = \frac{1}{2}x - 1$ .

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are called

are called

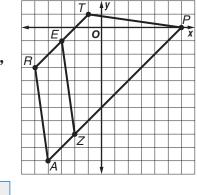


#### **KEY CONCEPT**

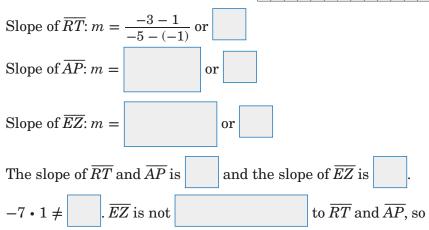
Perpendicular Lines in a Coordinate Plane Two nonvertical lines are perpendicular if the product of their slopes is -1. That is, the slopes are opposite reciprocals of each other. Vertical lines and horizontal lines are also perpendicular.

#### EXAMPLE Determine Whether Lines are Perpendicular

**GEOMETRY** The height of a trapezoid is measured on a segment that is perpendicular to a base. In a trapezoid *ARTP*, *RT* and *AP* are bases. Can *EZ* be used to measure the height of the trapezoid? Explain.

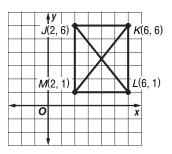


Find the slope of each segment.



it cannot be used to measure height.

**Check Your Progress** The graph shows the diagonals of a rectangle. Determine whether  $\overline{JL}$  is perpendicular to  $\overline{KM}$ .

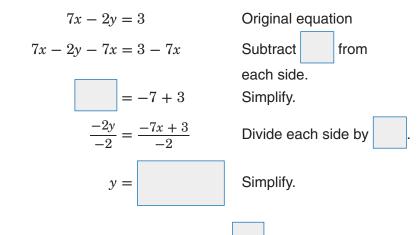


4-7

#### **EXAMPLE** Perpendicular Line Through a Given Point

Write the slope-intercept form for an equation of a line that passes through (4, -1) and is perpendicular to the graph of 7x - 2y = 3.

**Step 1** Find the slope of the given line.



**Step 2** The slope of the given line is So, the slope of the

> line perpendicular to this line is the opposite reciprocal of  $\frac{7}{2}$ , or  $-\frac{2}{7}$ .

**Step 3** Use the point-slope form to find the equation.

$$y - y_1 = m(x - x_1)$$

 $y - (-1) = -\frac{2}{7}(x - 4)$  (x<sub>1</sub>, y<sub>1</sub>) = (4, -1), m =

 $= -\frac{2}{7}(x - 4)$  Simplify.  $y + 1 = -\frac{2}{7}x + \frac{8}{7}$  Distribution **Distributive Property** y + 1 =  $-\frac{2}{7}x + \frac{8}{7}$ 

**Check Your Progress** Write the slope-intercept form

for an equation of a line that passes through (-3, 6) and is

y =

perpendicular to the graph of 3x + 2y = 6.

Subtract.

Point-slope form

Simplify.



Page(s):

Exercises:



# **BRINGING IT ALL TOGETHER**

### STUDY GUIDE

	Vocabulary Puzzlemaker	Build your Vocabulary		
Use your <b>Chapter 4 Foldable</b> to help you study for your chapter test.	To make a crossword puzzle, word search, or jumble puzzle of the vocabulary words in Chapter 4, go to: glencoe.com	You can use your completed <b>Vocabulary Builder</b> ( <i>pages 80–81</i> ) to help you solve the puzzle.		

### 4-1

**Rate of Change and Slope** 

#### Describe each type of slope.

	Type of Slope	Description of Graph
1.	positive	
2.	negative	
3.	zero	

#### **Slope and Direct Variation**

4-2

# For each situation, write an equation with the proper constant of variation.

**4.** The distance d varies directly as time t, and a cheetah can

travel 88 feet in 1 second.

**5.** The perimeter p of a pentagon with all sides of equal length varies directly as the length s of a side of the pentagon. A

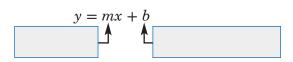
pentagon has 5 sides.

### Chapter 4 BRINGING IT ALL TOGETHER



**Graphing Equations in Slope-Intercept Form** 

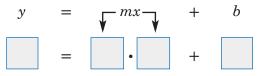
**6.** Fill in the boxes with the correct words to describe what *m* and *b* represent.



- 7. What are the slope and *y*-intercept of a vertical line?
- **8.** What are the slope and *y*-intercept of a horizontal line?

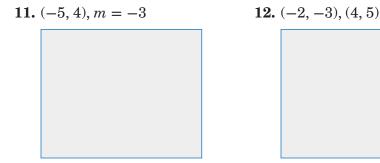
4-4 Writing Equations in Slope-Intercept Form

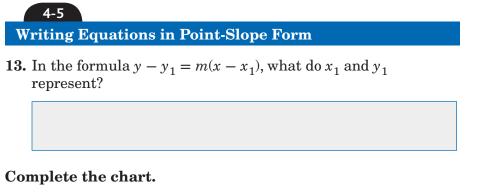
**9.** Suppose you are given that a line goes through (2, 5) and has a slope of -2. Use this information to complete the following equation.



**10.** What must you first do if you are not given the slope in the problem?

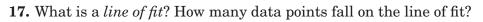
# Write an equation of the line that passes through each pair of points.





	Form of Equation	Formula	Example
14.	slope-intercept		y = 3x + 2
15.	point-slope		y - 2 = 4(x + 3)
16.	standard		3x - 5y = 15

#### 4-6 Statistics: Scatter Plots and Lines of Fit

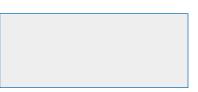


Geometry: Parallel and Perpendicular Lines

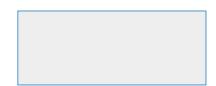
Write the slope-intercept form for an equation of the line that passes through the given point and is either parallel or perpendicular to the graph of the equation.

**18.** (-2, 2), y = 4x - 2 (parallel)

4-7



**19.** (4, 2),  $y = \frac{1}{2}x + 1$  (perpendicular)



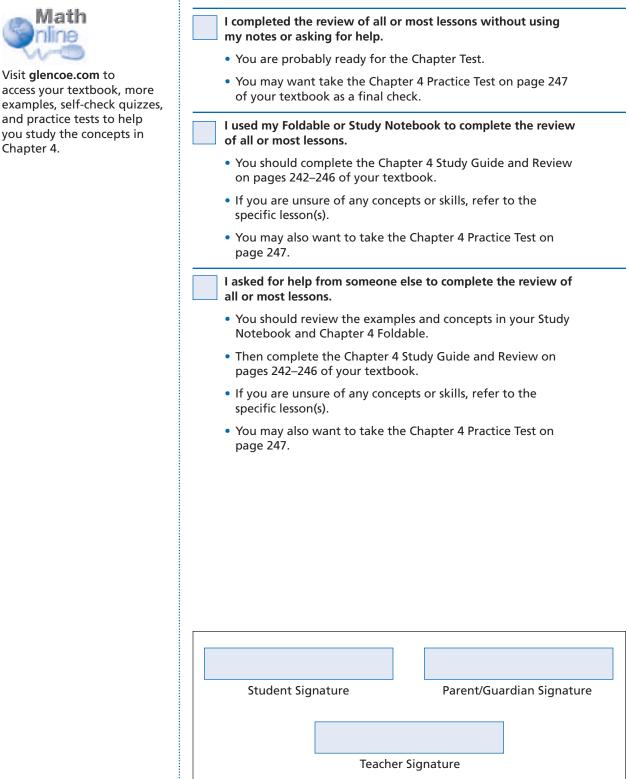


Math

Chapter 4.

### ARE YOU READY FOR THE CHAPTER TEST?

Check the one that applies. Suggestions to help you study are given with each item.





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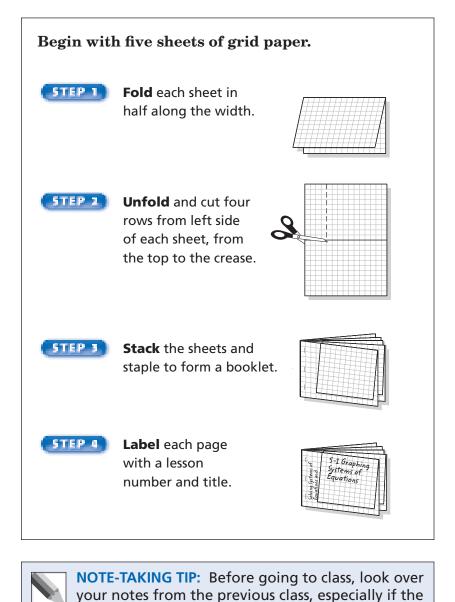
Chapter



# Solving Systems of Linear Equations and Inequalities



Use the instructions below to make a Foldable to help you organize your notes as you study the chapter. You will see Foldable reminders in the margin of this Interactive Study Notebook to help you in taking notes.



day's topic builds from the last one.



### BUILD YOUR VOCABULARY

This is an alphabetical list of new vocabulary terms you will learn in Chapter 5. As you complete the study notes for the chapter, you will see Build Your Vocabulary reminders to complete each term's definition or description on these pages. Remember to add the textbook page number in the second column for reference when you study.

Vocabulary Term	Found on Page	Definition	Description or Example
consistent			
[kuhn·SIHS·tuhnt]			
dependent			
elimination			
[ih·LIH·muh·NAY·shuhn]			

Vocabulary Term	Found on Page	Definition	Description or Example
independent			
inconsistent			
substitution [SUHB·stuh·TOO·shuhn]			
system of equations			



# **Graphing Systems of Equations**

#### **MAIN IDEAS**

- Determine whether a system of linear equations has 0, 1, or infinitely many solutions.
- Solve systems of equations by graphing.

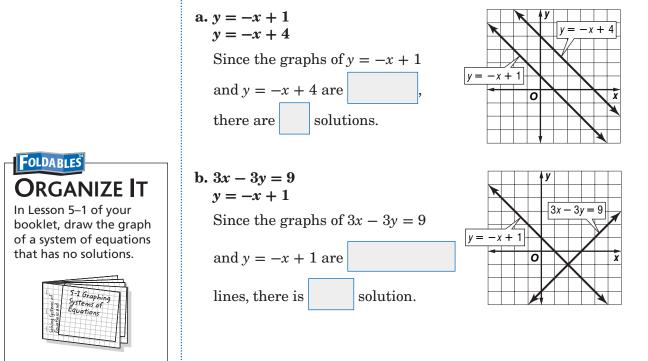
### BUILD YOUR VOCABULARY (pages 106-107)

Two equations together are called a system of equations. If the graphs intersect or coincide, the system of equations is said to be consistent. If the graphs are the system of equations is said to be inconsistent. If a system has exactly solution, it is independent. If the system has an number of solutions, it is

dependent.

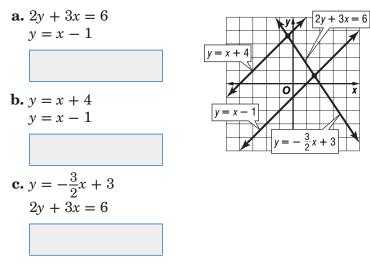
#### **EXAMPLE** Number of Solutions

Use each graph to determine whether the system has no solution, one solution, or infinitely many solutions.



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**Check Your Progress** Use the graph to determine whether each system has *no* solution, *one* solution, or *infinitely many* solutions.



### EXAMPLE Solve a System of Equations

Graph the system of equations. Then determine whether the system has *no* solution, *one* solution, or *infinitely many* solutions. If the system has one solution, name it.

$$2x - y = -3$$

$$8x - 4y = -12$$
The graphs of the equations
There are solutions of this system of equations.
$$0$$

$$8x - 4y = -12$$

**Check Your Progress** Graph the system of equations. Then determine whether the system has *no* solution, *one* solution, or *infinitely many* solutions. If the system has one solution, name it.

$$= 2x + 3$$
$$= \frac{1}{2}x + 3$$

у у

0 X

Describe the graph of a linear equation. (Lesson 3-3)

HOMEWORK ASSIGNMENT

Page(s):

Exercises:



### Substitution



- Solve systems of equations by using substitution.
- Solve real-world problems involving systems of equations.

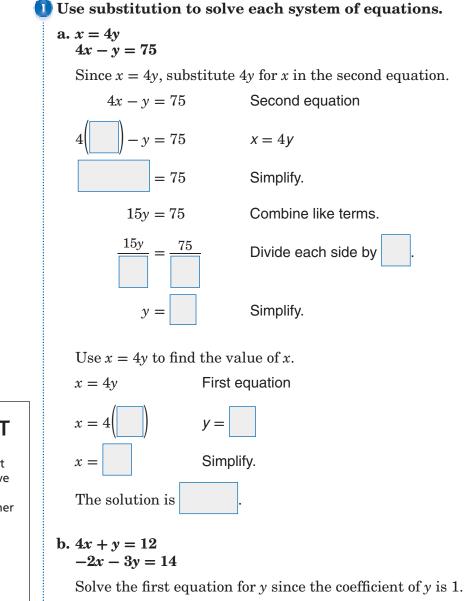
BUILD YOUR VOCABULARY (pages 106-107)

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The	

solution of a system of equations can be

found by using algebraic methods. One such method is called **substitution**.

### EXAMPLE Solve Using Substitution

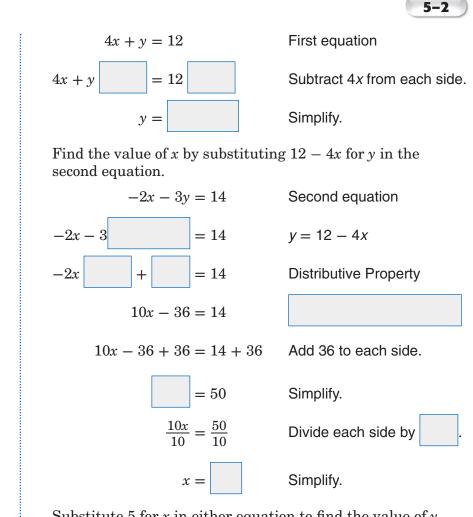


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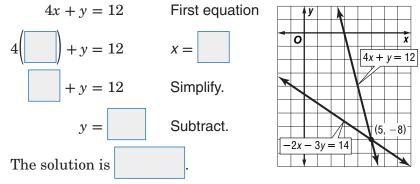


In Lesson 5-2 of your booklet, explain why it might be easier to solve a system of equations using substitution rather than graphing.





Substitute 5 for *x* in either equation to find the value of *y*.

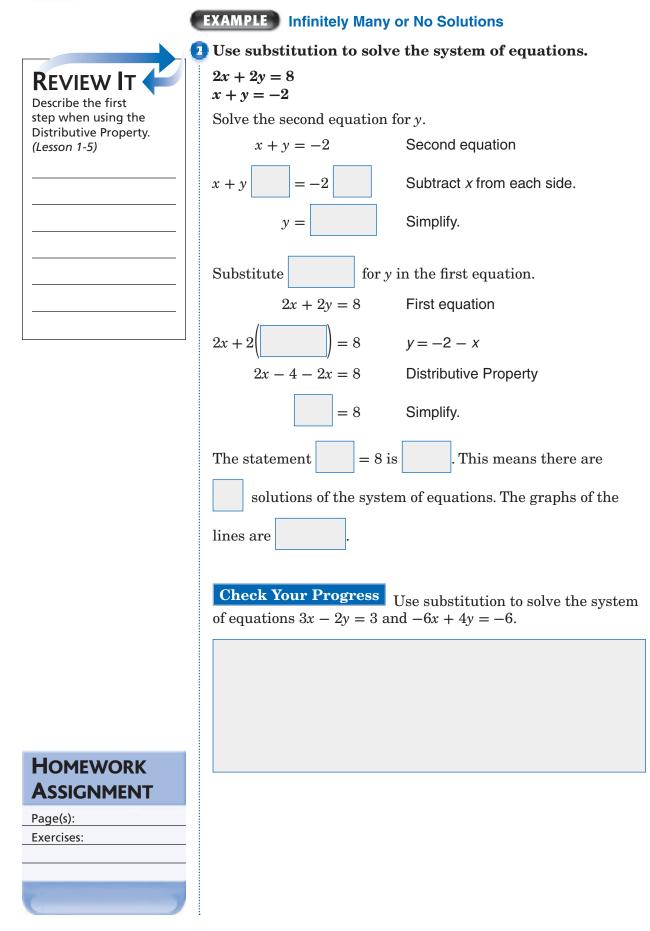


The graph verifies the solution.

Check Your Progress Use substitution to solve each system of equations.

**a.** y = 2x and 3x + 4y = 11

**b.** x + 2y = 1 and 5x - 4y = -23





# **Elimination Using Addition and Subtraction**

#### MAIN IDEAS

- Solve systems of equations by using elimination with addition.
- Solve systems of equations by using elimination with subtraction.

### BUILD YOUR VOCABULARY (pages 106-107)

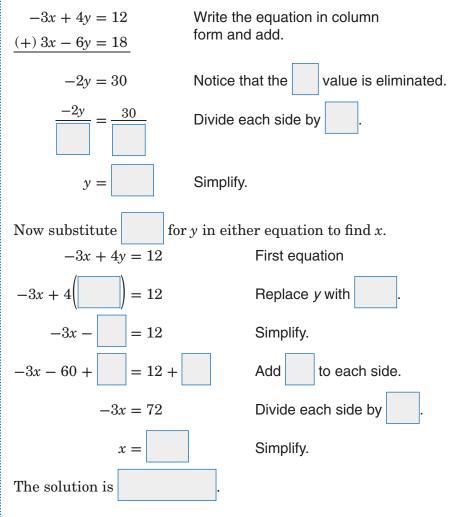
Sometimes adding two equations together will eliminate one variable. Using this step to solve a system of equations is called **elimination**.

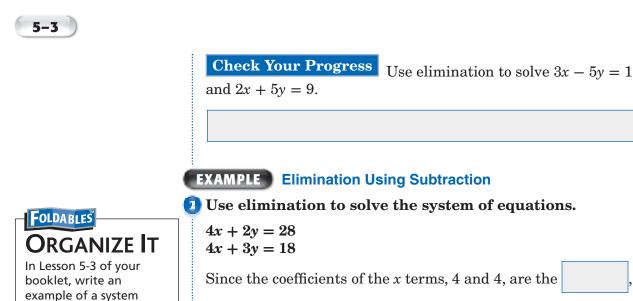
#### EXAMPLE Elimination Using Addition

#### Use elimination to solve the system of equations.

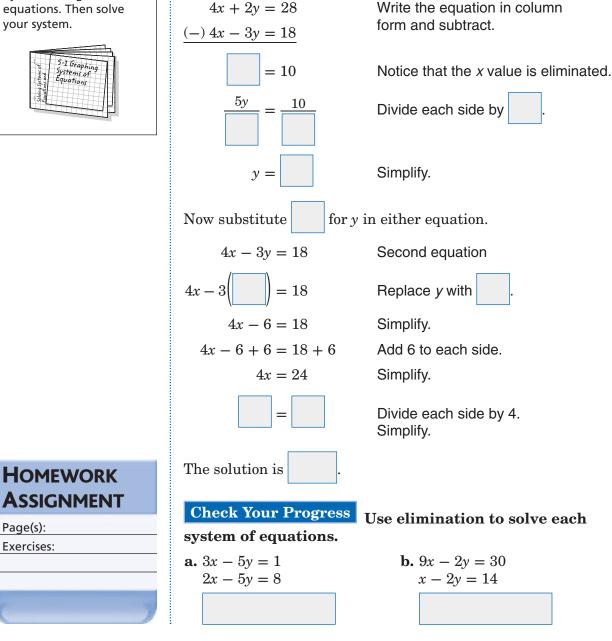
-3x + 4y = 123x - 6y = 18

Since the coefficients of the *x* terms, -3 and 3, are additive inverses, you can eliminate the *x* terms by adding the equations.





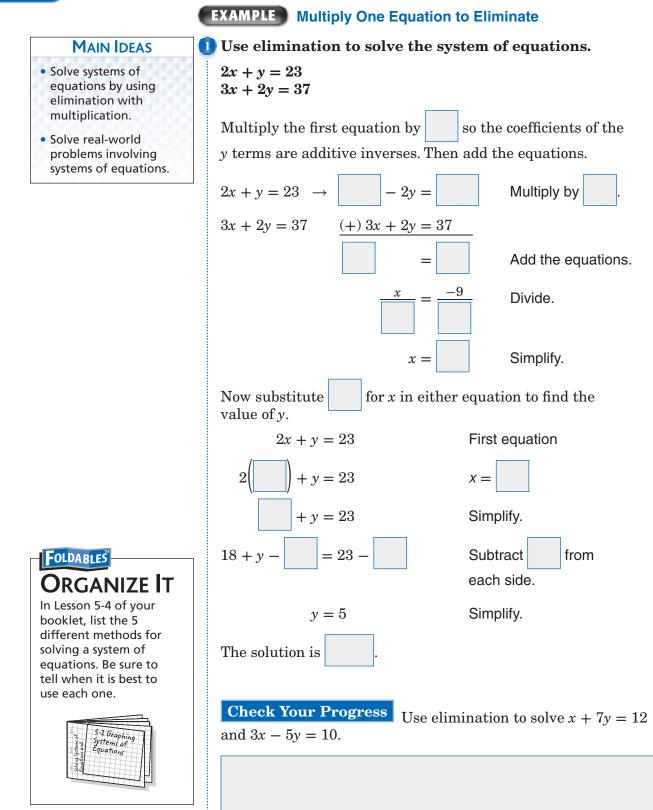
you can eliminate the *x* terms by subtracting the equations.



that can be solved

by subtracting the

## **Elimination Using Multiplication**



5-4



REMEMBER IT When solving a system of equations by elimination, you can choose to eliminate either variable. See Example 2 on page 271 of your textbook.

#### **EXAMPLE** Multiply Both Equations to Eliminate

1 Use elimination to solve the system of equations.

$$4x + 3y = 8$$
$$3x - 5y = -23$$

Choose either variable to eliminate. Let's eliminate *x*.

4x + 3y = $8 \rightarrow$  $9\gamma$ = 24Multiply by +  $3x - 5y = -23 \rightarrow (+) - 12x +$ = 92Multiply by Add the = equations.  $\frac{29y}{29} = \frac{166}{29}$ Divide each side by Simplify. y =Now substitute for *y* in either equation to find *x*. 4x + 3y = 8First equation = 84x + 3y =Simplify. = 8+4x + 12 from each side. = 8 -Subtract 4x =Simplify.  $\frac{4x}{4} = \frac{-4}{4}$ Divide each side by 4. x =Simplify. The solution is **Check Your Progress** Use elimination to solve 3x + 2y = 10and 2x + 5y = 3.

ASSIGNMENT Page(s):

HOMEWORK

Exercises:



## **Applying Systems of Linear Equations**

#### **MAIN IDEAS**

- Determine the best method for solving systems of equations.
- Apply systems of linear equations.

#### EXAMPLE Determine the Best Method

FUND-RAISING At a Boy Scout fund-raising dinner, Mr. Jones bought 2 adult meals and 3 child meals for \$23. Mrs. Gomez bought 4 adult meals and 2 child meals for \$34. All adult meals are the same price and all child meals are the same price. The following system can be used to represent this situation. Determine the best method to solve the system of equations. Then solve the system.

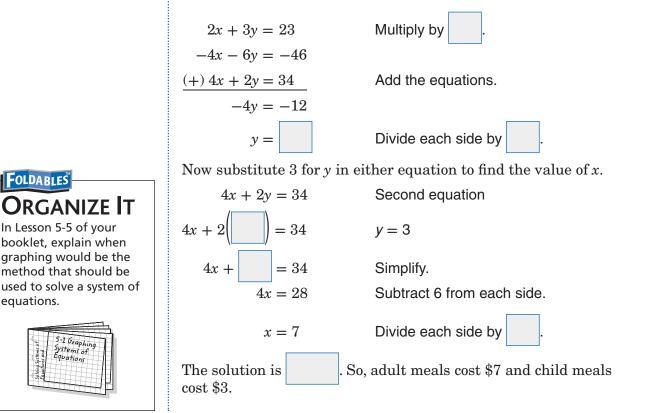
2x + 3y = 234x + 2y = 34

- For an exact solution, an algebraic method is best.
- Since neither the coefficients of nor the coefficients of
  - are 1 or -1, you cannot use the substitution method.
- Since the coefficients are not the same for either *x* or *y*, you

will need to use

with multiplication.

Multiply the first equation by -2 so the coefficients of the *x*-terms are additive inverses. Then add the equations.



FOLDABLES

equations.

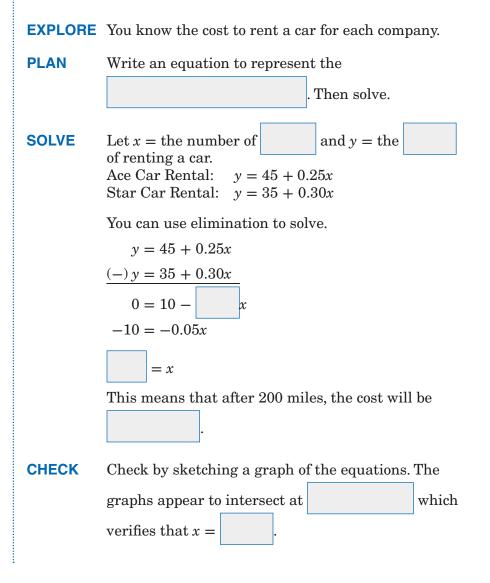
5-1 Graph

**Check Your Progress POOL PARTY** At the school pool party, Mr. Lewis bought 1 adult ticket and 2 child tickets for \$10. Mrs. Vroom bought 2 adult tickets and 3 child tickets for \$17. All adult tickets are the same price and all child tickets are the same price. The following system can be used to represent this situation. Determine the best method to solve the system of equations. Then solve the system.

$$x + 2y = 10$$
$$2x + 3y = 17$$

#### EXAMPLE Solve Systems of Equations to Solve Problems

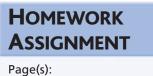
2 CAR RENTAL Ace Car Rental rents a car for \$45 a day and \$0.25 per mile. Star Car Rental rents a car for \$35 per day and \$0.30 per mile. After how many miles will the cost of renting a car at Ace Car Rental be the same as the cost of renting a car at Start Car Rental?



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**Check Your Progress VIDEO GAMES** The cost to rent a video game from Action Video is \$2 plus \$0.50 per day. The cost to rent a video game at TeeVee Rentals is \$1 plus \$0.75 per day. After how many days will the cost of renting a video game at Action Video be the same as the cost of renting a video game at TeeVee Rentals?

5-5



Exercises:



# **BRINGING IT ALL TOGETHER**

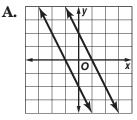
### STUDY GUIDE

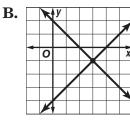
FOLDABLES	Vocabulary Puzzlemaker	Build your Vocabulary		
Use your <b>Chapter 5 Foldable</b> to help you study for your chapter test.	To make a crossword puzzle, word search, or jumble puzzle of the vocabulary words in Chapter 5, go to: glencoe.com	You can use your completed <b>Vocabulary Builder</b> ( <i>pages 106–107</i> ) to help you solve the puzzle.		

C.



Each figure shows the graph of a system of two equations. Write the letter(s) of the figures that illustrate each statement





-	y			D.			4	y		7
$\geq$	$\triangleleft$	€						/	_	
0		_	X		-		0		-	X
1							1			

1. A system of two linear equations can have an infinite number

of solutions.

2. If two graphs are parallel, there are no ordered pairs that satisfy

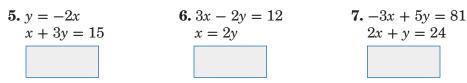
both equations.

- **3.** If a system of equations has exactly one solution, it is independent.
- 4. If a system of equations has an infinite number of solutions, it is



Substitution

#### Solve each system using substitution.



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Write *addition* or *subtraction* to tell which operation it would be easiest to use to eliminate a variable of the system. Explain your choice.

	System of Equations	Operation	Explanation
8.	3x + 5y = 12 $-3x + 2y = 6$		
9.	3x + 5y = 7 $3x - 2y = 8$		

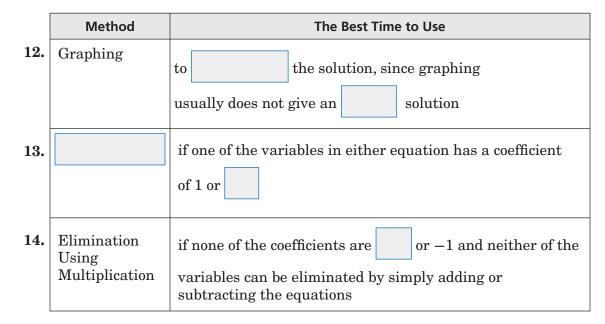
Use elimination to solve each system of equations.

**10.** 7x + 2y = 10 **11.** 2x + 5y = -22 

 -7x + y = -16 10x + 3y = 22 

5-4 Elimination Using Multiplication

Three methods for solving systems of linear equations are summarized below. Complete the table.





**Applying Systems of Linear Equations** 

Determine the best method to solve each system of equations. Then solve the system.

- 1. -2x + 3y = 0-1x + 5y = 7
- **2.** -3x 4y = -653x + 2y = 43

**3.** 6x - 2y = 224x + 1y = 24



## ARE YOU READY FOR THE CHAPTER TEST?

-



Visit glencoe.com to access your textbook, more examples, self-check quizzes, and practice tests to help you study the concepts in Chapter 5.

Check the one that applies. Suggestions to help you study are	
given with each item.	

I completed the review of all or most lessons without using my notes or asking for help.

- You are probably ready for the Chapter Test.
- You may want to take the Chapter 5 Practice Test on page 289 of your textbook as a final check.

I used my Foldable or Study Notebook to complete the review of all or most lessons.

- You should complete the Chapter 5 Study Guide and Review on pages 285–288 of your textbook.
- If you are unsure of any concepts or skills, refer back to the specific lesson(s).
- You may also want to take the Chapter 5 Practice Test on page 289.

I asked for help from someone else to complete the review of all or most lessons.

- You should review the examples and concepts in your Study Notebook and Chapter 5 Foldable.
- Then complete the Chapter 5 Study Guide and Review on pages 285–288 of your textbook.
- If you are unsure of any concepts or skills, refer back to the specific lesson(s).
- You may also want to take the Chapter 5 Practice Test on page 289.

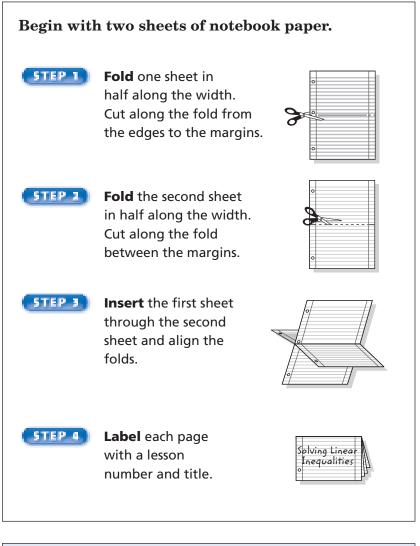
Student Signature	Parent/Guardian Signature
Teacher	Signature



# **Solving Linear Inequalities**

### **FOLDABLES**

Use the instructions below to make a Foldable to help you organize your notes as you study the chapter. You will see Foldable reminders in the margin of this Interactive Study Notebook to help you in taking notes.



**NOTE-TAKING TIP:** When you take notes, write down the math problem and each step in the solution using math symbols. Next to each step, write down, in your own words, exactly what you are doing.



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### BUILD YOUR VOCABULARY

This is an alphabetical list of new vocabulary terms you will learn in Chapter 6. As you complete the study notes for the chapter, you will see Build Your Vocabulary reminders to complete each term's definition or description on these pages. Remember to add the textbook page number in the second column for reference when you study.

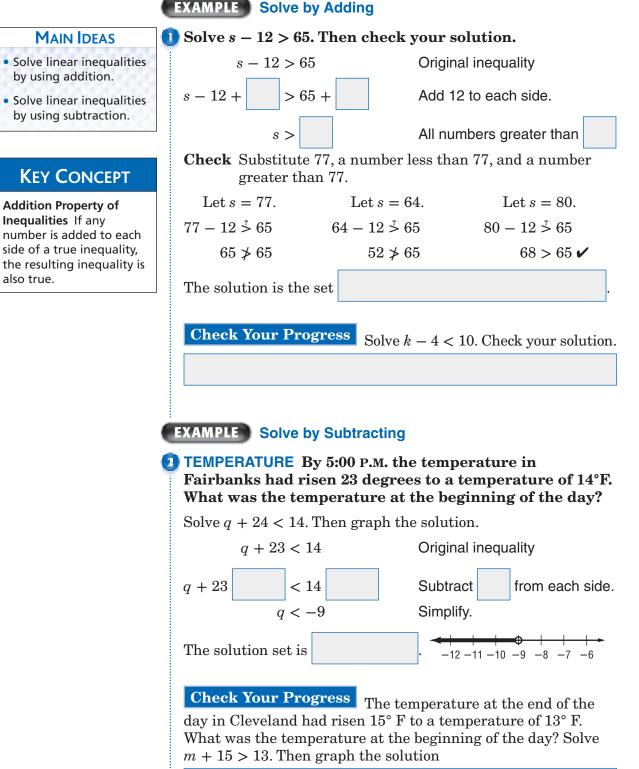
Vocabulary Term	Found on Page	Definition	Description or Example
absolute value			
boundary			
compound inequality			
half-plane			

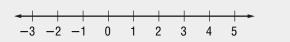
(continued on the next page)

Vocabulary Term	Found on Page	Definition	Description or Example
intersection			
set-builder notation			
system of inequalities			
union			

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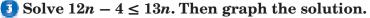
# Solving Inequalities by Addition and Subtraction





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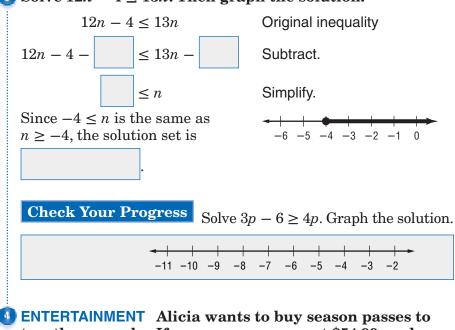
#### **EXAMPLE** Variables on Each Side



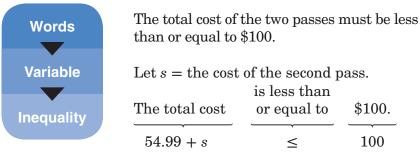
#### **KEY CONCEPT**

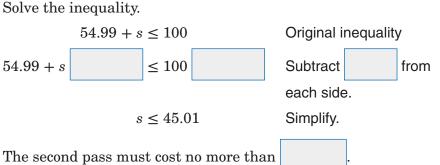
**Subtraction Property** of Inequalities If any number is subtracted from each side of a true inequality, the resulting inequality is also true.

FOLDABLES Include the Addition and Subtraction **Properties of Inequalities** in your Foldable. Be sure to show examples.



two theme parks. If one season pass cost \$54.99, and Alicia has \$100 to spend on passes, the second season pass must cost no more than what amount?





The second pass must cost no more than

**Check Your Progress** Michael scored 30 points in the four rounds of the free throw contest. Randy scored 11 points in the first round, 6 points in the second round, and 8 in the third round. How many points must he score in the final round to surpass Michael's score?

### HOMEWORK ASSIGNMENT

#### Page(s):

Exercises:

\$100.

100

 $\leq$ 



### **Solving Inequalities by Multiplication and Division**

#### MAIN IDEAS

- Solve linear inequalities by using multiplication.
- Solve linear inequalities by using division.

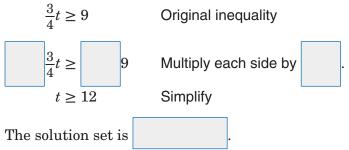
#### **KEY CONCEPTS**

Multiplying by a Positive Number If each side of a true inequality is multiplied by the same positive number, the resulting inequality is also true.

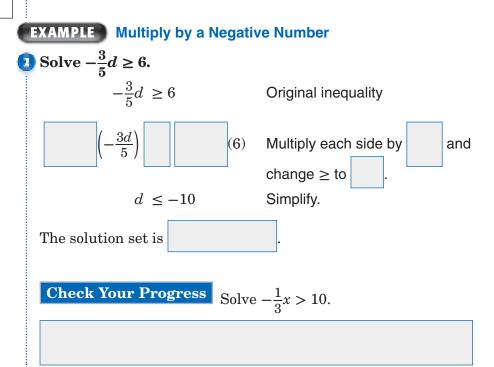
Multiplying by a Negative Number If each side of a true inequality is multiplied by the same negative number, the direction of the inequality symbol must be reversed so that the resulting inequality is also true.

#### **EXAMPLE** Write and Solve an Inequality

HIKING Bob is walking at a rate of <sup>3</sup>/<sub>4</sub> mile per hour. He knows that it is at least 9 miles to Onyx Lake. How long will it take Bob to get there? Write and solve an inequality to find the length of time.

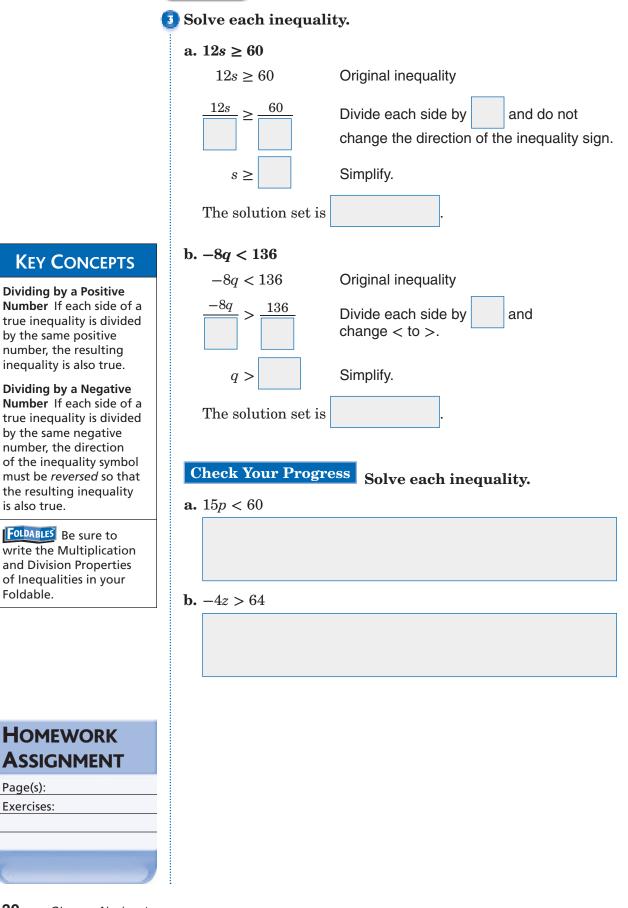


**Check Your Progress SCHOOL** At Midpark High School,  $\frac{2}{3}$  of the junior class attended the dance. There were at least 200 juniors at the dance. How many students are in the junior class?



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#### **EXAMPLE** Divide to Solve an Inequality



Page(s):



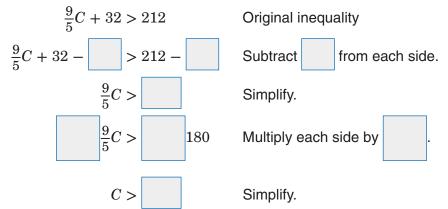
### **Solving Multi-Step Inequalities**

#### **MAIN IDEAS**

- Solve linear inequalities involving more than one operation.
- Solve linear inequalities involving the Distributive Property.

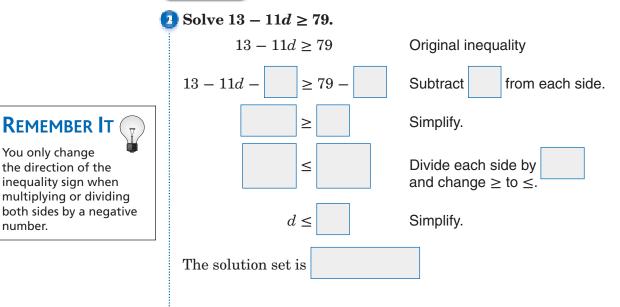
**EXAMPLE** Multi-Step Inequality

- **D** SCIENCE The inequality F > 212 represents the temperature in degrees Fahrenheit for which water is
  - a gas (steam). Similarly, the inequality  $\frac{9}{5}C + 32 > 212$
  - represents the temperature in degrees Celsius for which water is a gas. Find the temperature in degrees Celsius for which water is a gas.



Water will be a gas for all temperatures greater than 100°C.

### EXAMPLE Inequality Involving a Negative Coefficient



number.



In Lesson 6-3 of your Foldable, explain how solving an inequality is different from solving an equation.



**REMEMBER IT** (

inequality results in a statement that is

real numbers.

• false, the solution is the empty set, Ø.

HOMEWORK ASSIGNMENT

Page(s): Exercises:

If solving an

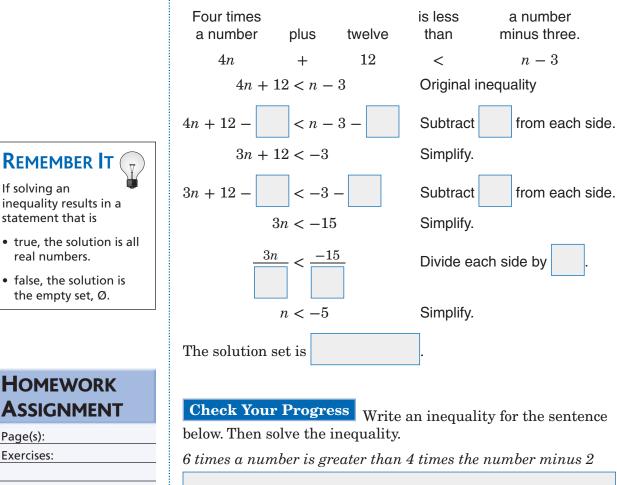
#### **Check Your Progress**

- **a.** The boiling point of helium is -452°F. Solve
  - $\frac{9}{5}C + 32 > -452$  to find the temperatures in degrees
  - Celsius for which helium is a gas.

**b.** Solve -8y + 3 > -5

Define a variable, write an inequality, and solve the problem below. Check your solution.

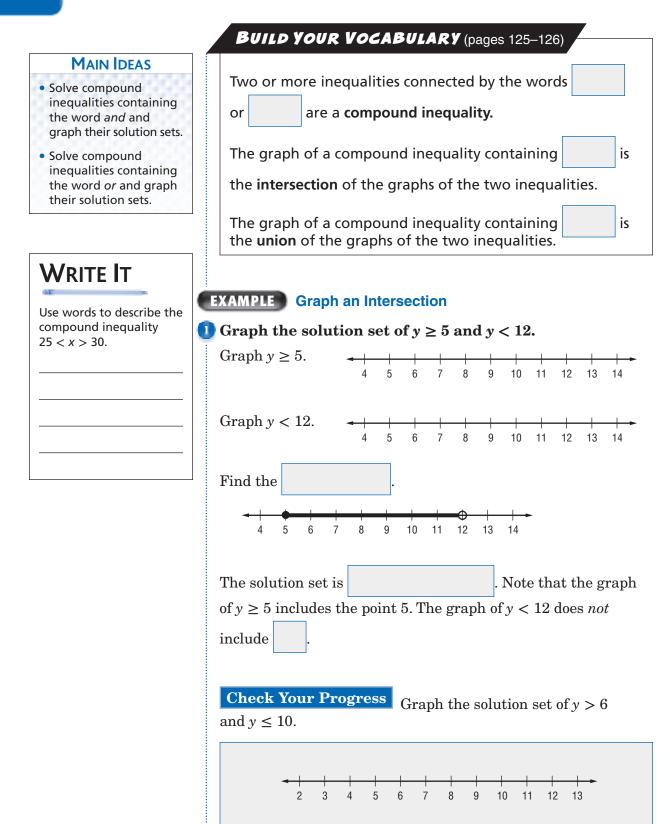
#### Four times a number plus twelve is less than a number minus three.



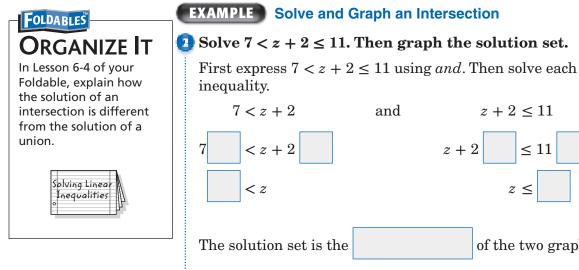


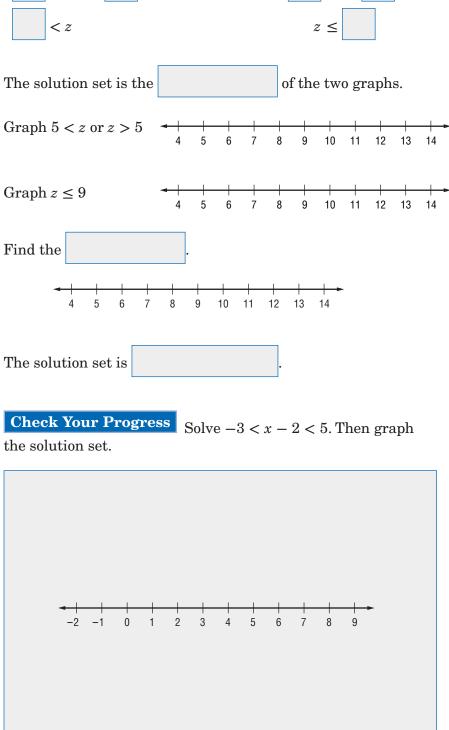


# **Solving Compound Inequalities**







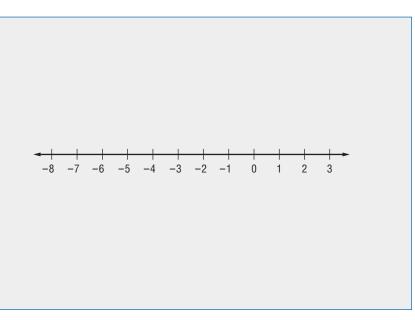


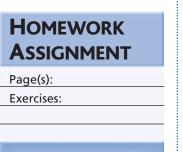
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#### **EXAMPLE** Solve and Graph a Union

3 Solve  $4k - 7 \le 25$  or  $12 - 9k \ge 30$ . Then graph the solution set.  $4k - 7 \le 25$  $12 - 9k \ge 30$ or 4k - 7 $\leq 25$ 12 - 9k $\geq 30$  $-9k \ge 18$  $4k \leq 32$  $\frac{4k}{4} \leq \frac{32}{4}$  $\frac{-9k}{-9} \leq \frac{18}{-9}$  $k \leq$  $k \leq$ Graph  $k \leq 8$ . -3-2-1 0 1 2 3 4 5 6 7 8 9 10 Graph  $k \ge -2$ . -4 -3 -2 -1 0 1 2 3 4 5 6 7 8 9 10 -4-3-2-1 0 1 2 3 4 5 6 7 8 9 10 Notice that the graph of  $k \leq 8$  contains point in the graph of  $k \leq -2$ . So, the is the graph of  $k \leq 8$ . The solution set is

**Check Your Progress** Solve -2x + 5 < 15 or 5x + 15 > 20. Then graph the solution set.





6 - 4

## Solving Open Sentences Involving Absolute Value



- Solve absolute value equations.
- Solve absolute value inequalities.

REVIEW IT Why is the absolute value of a number always greater than or equal to zero? (Lesson 2-1).

#### EXAMPLE Solve an Absolute Value Equation

**1** a. WEATHER The average January temperature in a northern Canadian city is 1 degree Fahrenheit. The actual January temperature for that city may be about 5 degrees Fahrenheit warmer or colder. Solve |t-1| = 5 to find the range of temperatures.

#### METHOD 1 Graphing

|t - 1| = 5 means that the distance between t and 1 is 5 units. To find t on the number line, start at 1 and move 5 units in either direction.

5 Units

-3 -2 -1 0 1 2

5 Units

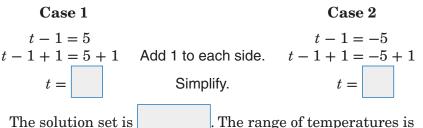
3 4

5

The distance from 1 to 6 is 5 units. The distance from 1 to -4 is 5 units. The solution set is  $\{-4, 6\}$ .

METHOD 2 Compound Sentence

Write |t - 1| = 5 as t - 1 = 5 or t - 1 = -5.



The solution set is  $-4^{\circ}$ F to 6°F.

#### b. Solve |x + 2| = -1.

is

|x + 2| = -1 means that the distance between x and -2

. Since distance cannot be negative, the solution is

#### **Check Your Progress**

**a. WEATHER** The average temperature for Columbus on Tuesday was 45°F. The actual temperature for anytime during the day may have actually varied from the average temperature by 15°F. Solve |t - 45| = 15 to find the range of temperatures.

**b.** Solve |x - 3| = -5.

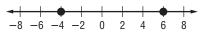


# WRITE IT

Will the solution to |x + 7| < 11 require finding the intersection or union of the two cases? Explain.

### EXAMPLE Write an Absolute Value Equation

Write an open sentence involving absolute value for the graph.



Find the midpoint between -4 and 6, which is 1. So the equation is |y - 1| = 5.

**Check Your Progress** Write an open sentence involving absolute value for the graph.

### EXAMPLE Graphing Absolute Value Functions

### **3** a. Graph f(x) = |x + 3|.

-3 = x

First, find the minimum point of the graph, this is f(x) = 0.

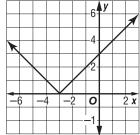
f(x) = |x + 3| Original function

$$0 = x + 3$$
  $f(x) = 0$ 

Subtract 3 from each side.

Next, complete a table of values to graph the function.

х	-6	-4	-3	-2	0
f(x)	3	1	0		



### b. Graph f(x) = |x - 5|.

Find the minimum point of the graph.

f(x) = |x - 5| Original function

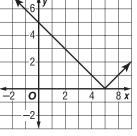
 $0 = x - 5 \qquad f(x) = 0$ 

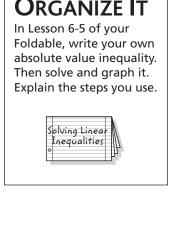
5 = x Add 5 to each side.

Next, complete a table of values to graph the function.

x	3	4	5	6	7
f(x)	2		0		







HOMEWORK Assignment

Page(s):

Exercises:





# **Solving Inequalities Involving Absolute Value**

EXAMPLE Solve an Absolute Value Inequality (<)

#### MAIN IDEAS

• Solve absolute value inequalities.

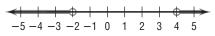
6-6

 Apply absolute value inequalities in realworld problems. Solve each open sentence. Then graph the solution set. a.  $|s - 3| \le 12$ Write  $|s - 3| \le 12$  as  $s - 3 \le 12$  and  $s - 3 \ge -12$ . **Case 1** s - 3 is positive. **Case 2** s - 3 is negative. -(s-3) < 12 $s - 3 \le 12$  $s-3 \ge -12$  $s - 3 + 3 \le 12 + 3$  $s - 3 + 3 \ge -12 + 3$  $s \leq 15$ s > -9The solution set is  $\{s \mid -9 \le s \le 15\}$ . + + + + + + + + -9-6-3 0 3 6 9 12 15 18 21 24 b. |x+6| < 8Write |x + 6| < 8 as x + 6 < 8 and x + 6 > -8. **Case 1** x + 6 is positive. **Case 2** x + 6 is negative. x + 6 < 8-(x+6) < 8x + 6 - 6 < 8 - 6x + 6 > -8x + 6 - 6 > -8 - 6x < 2x > -14The solution set is  $\{x \mid -14 < x < 2\}$ . -16-14-12-10-8-6-4-2024 **Check Your Progress** Solve each open sentence. Then graph the solution set. a. |y + 4| < 5-9 -8 -7 -6 -5 -4 -3 -2 -1 0 1 b.  $|z - 3| \le -2$ 

### EXAMPLE Solve an Absolute Value Inequality (>)

2 Solve each open sentence. Then graph the solution set.

a. |3y - 3| > 9**Case 1** 3y - 3 is positive. 3v - 3 > 9 3v - 3 is positive. 3y - 3 + 3 > 9 + 3 Add 3 to each side. 3y > 12Simplify. y > 4Divide each side by 3. **Case 2** 3y - 3 is negative. -(3y - 3) > 9 3y - 3 is negative. 3y - 3 < -9 Simplify. 3y - 3 + 3 < -9 + 3 Add 3 to each side. 3y < -6Simplify. y < -2 Divide each side by 3. The solution set is  $\{y \mid y < -2 \text{ or } y > 4\}$ .



### b. $|2x + 7| \ge -11$

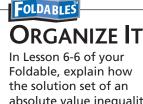
Since |2x + 7| is always greater than zero, the solution set is  $\{x \mid x \text{ is a real number}\}$ .

-5-4-3-2-1 0 1 2 3 4 5

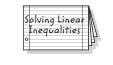
**Check Your Progress** Solve each open sentence. Then graph the solution set.

a. |2m - 3| > 7

b.  $|3x + 4| \ge 2$ 



the solution set of an absolute value inequality differs when the absolute value is greater than or less than the number.



HOMEWORK ASSIGNMENT

Page(s):

Exercises:

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# **Graphing Inequalities in Two Variables**

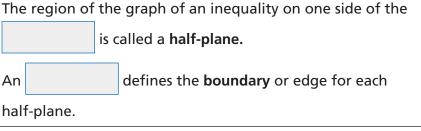
#### MAIN IDEAS

- Graph inequalities on the coordinate plane.
- Solve real-world problems involving linear inequalities.

### **KEY CONCEPT**

Half-Planes and Boundaries Any line in the plane divides the plane into two regions called half-planes. The line is called the boundary of each of the two half-planes.

# BUILD YOUR VOCABULARY (pages 125–126)



### EXAMPLE Graph an Inequality

#### (1) Graph 2y - 4x > 6. **Step 1** Solve for *y* in terms of *x*. 2y - 4x > 6**Original Inequality** 2y - 4x + >+6Add to each side. 2y > 4x + 6Simplify. $\frac{2y}{2} > \frac{4x+6}{2}$ Divide each side by 2. *y* > Simplify. **Step 2** Graph y = 2x + 3. Since y > 2x + 3 does not include values when y = 2x + 3, the boundary is in the solution set. The boundary should be drawn as a **Step 3** Select a point in one of the half-planes and test it. Let's use (0, 0). v = 2x + 3y > 2x + 3Original inequality 0 > 2(0) + 3 x = 0, y = 00 0 > 3False Since the statement is false, the containing the origin is part of the solution. Shade the other half-plane.



**Check** Test a point in the other half-plane, for example, (-3, 1).

y > 2x + 3 Original inequality 1 > 2(-3) + 3 x = -3, y = 11 > -3 ✓

Since the statement is true, the half-plane containing (-3, 1)

should be

**Check Your Progress** 

### REMEMBER IT

A dashed line indicates that the boundary is *not* part of the solution set. A solid line indicates that the boundary line *is* part of the solution set.

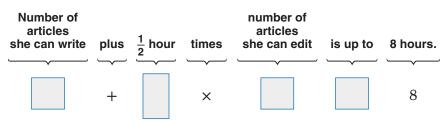
	<b>A Y</b>			
•	0		x	
		-	_	

Graph v = 3r < 2

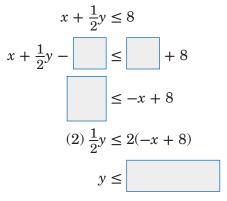
### EXAMPLE Write and Solve an Inequality

**3** JOURNALISM Lee Cooper writes and edits short articles for a local newspaper. It generally takes her an hour to write an article and about a half-hour to edit an article. If Lee works up to 8 hours a day, how many articles can she write and edit in one day?

**Step 1** Let *x* equal the number of articles Lee can write. Let *y* equal the number of articles that Lee can edit. Write an open sentence representing the situation.



#### **Step 2** Solve for y in terms of x.



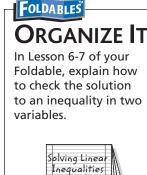
Original inequality

Subtract from each side.

Simplify.

Multiply each side by 2.

Simplify.



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Step 3 Since the open sentence includes the equation, graph

y = -2x + 16 as a line. Test a in

in one

of the half-planes, for example, (0, 0). Shade the halfplane containing (0, 0) since  $0 \le -2(0) + 16$  is true.

	y									
-18-	-							_		
-16-										
-14-										
1 · · ·										
-12-										
-10-										
6										
-4-										
										-
<sup>-</sup> 0	2	2 4	16	5 8	3 1	01	21	41	61	8 <b>x</b>
						_				

Step 4 Examine the situation

• Lee cannot work a negative number of hours. Therefore, the

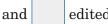
domain and range contain only

numbers.

• Lee only wants to count articles that are completely written or completely edited. Thus, only points in the half-plane

whose *x*- and *y*-coordinates are numbers are possible solutions.

• One solution is (2, 3). This represents written articles



edited articles.

**Check Your Progress** You offer to go to the local deli and pick up sandwiches for lunch. You have \$30 to spend. Chicken sandwiches cost \$3.00 and tuna sandwiches are \$1.50 each. How many sandwiches can you purchase for \$30?

### HOMEWORK Assignment

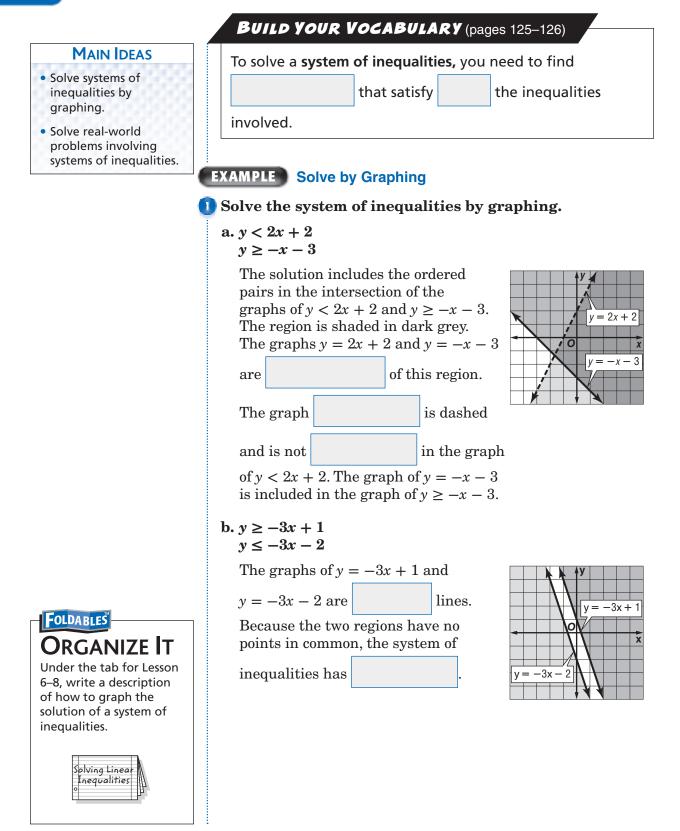
Page(s):

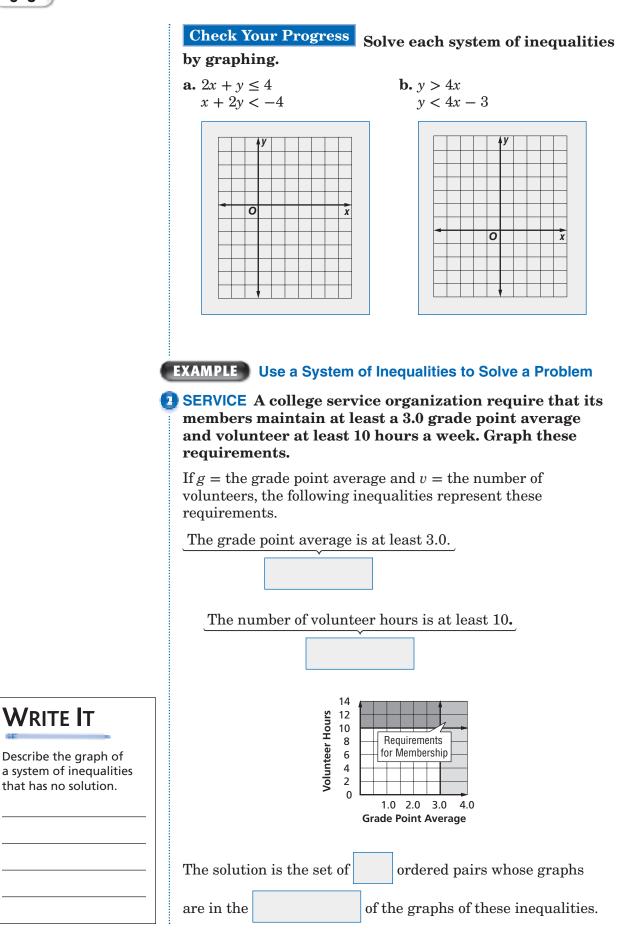
6-7

Exercises:

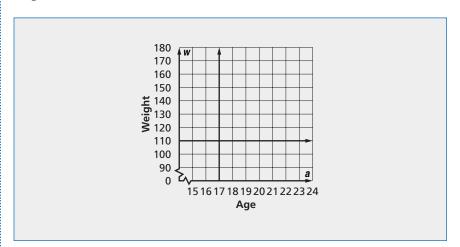


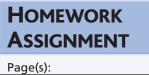
# **Graphing Systems of Inequalities**





**Check Your Progress** The senior class is sponsoring a blood drive. Anyone who wishes to give blood must be at least 17 years old and weigh at least 110 pounds. Graph these requirements.





Exercises:

6-8



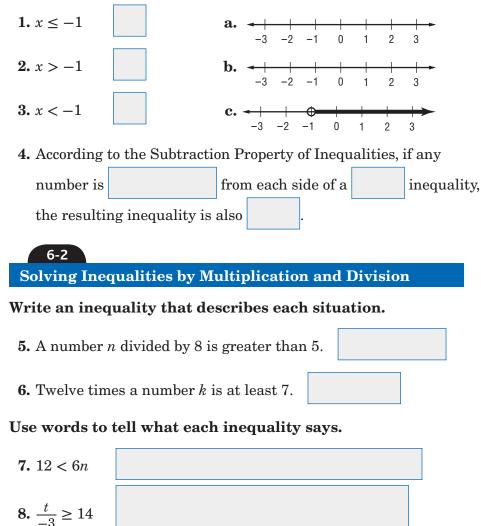
# **BRINGING IT ALL TOGETHER**

# STUDY GUIDE

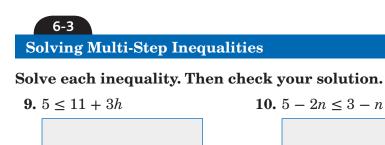
FOLDABLES	Vocabulary Puzzlemaker	Build your Vocabulary	
Use your <b>Chapter 6 Foldable</b> to help you study for your chapter test.	To make a crossword puzzle, word search, or jumble puzzle of the vocabulary words in Chapter 6, go to: glencoe.com	You can use your completed <b>Vocabulary Builder</b> ( <i>pages 125–126</i> ) to help you solve the puzzle.	

#### 6-1 Solving Inequalities by Addition and Subtraction

Write the letter of the graph that matches each inequality.







#### Define a variable, write an inequality, and solve each problem. Then check your solution.

- 11. Six plus four times a number is no more than the number.
- **12.** Three times a number plus eight is at least ten less than four times the number.
- **13.** Six times a number is greater than twelve less than 8 times the number.

**14.** When is a compound inequality containing *and* true?

**Solving Compound Inequalities** 

6-4

15. The graph of a compound inequality containing and is the

of the graphs of the two inequalities.

- **16.** When is a compound inequality containing *or* true?
- **17.** The graph of a compound inequality containing *or* is the

of the graphs of the two inequalities.

### Chapter 6 BRINGING IT ALL TOGETHER

### 6-5

### Solving Open Sentence Involving Absolute Value

#### Solve each open sentence. Then graph the solution set.

	Open Sentence	Solution Set	Graph
18.	m + 4  = 6		<mark>&lt;                                      </mark>
19.	2p-3  = 9		<mark>→                                      </mark>
20.	3n + 4  = -6		<mark>→                         →</mark> -5 -4 -3 -2 -1 0 1 2 3 4 5
21.	2r+4  = 6		-6 -5 -4 -3 -2 -1 0 1 2 3 4

**22.** The temperature of an oven is accurate to within 1.5% of the temperature marked on the dial. If the dial is set to 375°, what is the maximum and minimum that the temperature of the oven could actually be? Round to the nearest tenth.

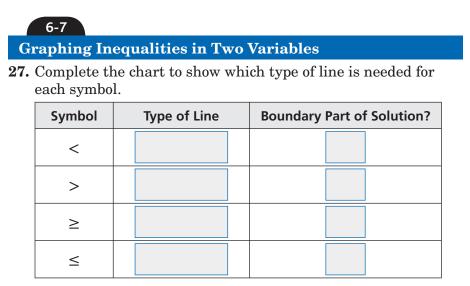
### 6-6

#### Solving Inequalities Involving Absolute Value

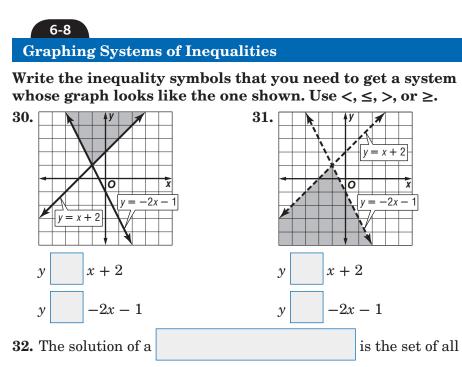
Complete each compound sentence by writing *and* or *or* in the blank. Use the result to help you graph the absolute value sentence.

	Absolute Value Sentence	Compound Sentence	Graph
23.	$ 2x+2  \ge 8$	$2x + 2 \ge 8 \qquad \qquad 2x + 2 \le -8$	
24.	$ x-5  \le 4$	$x - 5 \le 4 \qquad x - 5 \ge -4$	
25.	2x-3  > 5	$2x - 3 > 5 \qquad \qquad 2x - 3 < -5$	-3 -2 -1 0 1 2 3 4 5 6 7

**26.** A thermometer is guaranteed to give a temperature no more than 2.1°F from the actual temperature. If the thermometer reads 58°F, what is the range for the actual temperature?



- **28.** If a test point results in a false statement, what do you know about the graph?
- **29.** If a test point results in a true statement, what do you know about the graph?

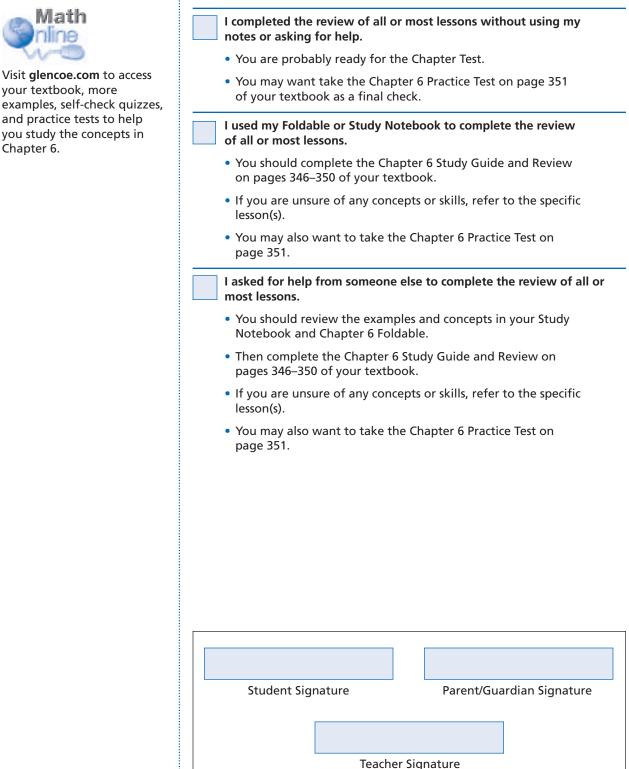


ordered pairs that satisfy both inequalities.



# ARE YOU READY FOR THE CHAPTER TEST?

Check the one that applies. Suggestions to help you study are given with each item.

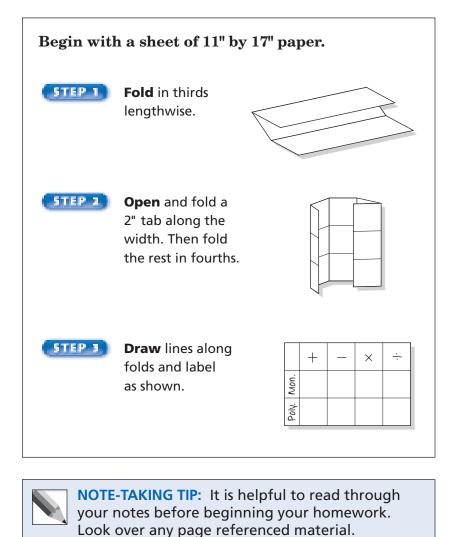




# **Polynomials**

# **FOLDABLES**

Use the instructions below to make a Foldable to help you organize your notes as you study the chapter. You will see Foldable reminders in the margin this Interactive Study Notebook to help you in taking notes.



Chapter 7



### BUILD YOUR VOCABULARY

This is an alphabetical list of new vocabulary terms you will learn in Chapter 7. As you complete the study notes for the chapter, you will see Build Your Vocabulary reminders to complete each term's definition or description on these pages. Remember to add the textbook page number in the second column for reference when you study.

Vocabulary Term	Found on Page	Definition	Description or Example
binomial [by·NOH·mee·uhl]			
constant			
degree of monomial			
degree of polynomial			
difference of squares			

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Vocabulary Term	Found on Page	Definition	Description or Example
FOIL method			
monomial [mah·NOH·mee·uhl]			
nogativo ovnonont			
negative exponent			
polynomial			
[PAH·luh·NOH-mee·uhl]			
trinomial			
[try·NOH·mee-uhl]			
zero exponent			



# **Multiply Monomials**

### MAIN IDEAS

- Multiply monomials.
- Simplify expressions involving powers of monomials.

### BUILD YOUR VOCABULARY (pages 150-151)

A **monomial** is a number, a

or a product of a

number and one or more variables.

Monomials that are

### numbers are called **constants**.

### **EXAMPLES** Identify Monomials

# Determine whether each expression is a monomial. Explain your reasoning.

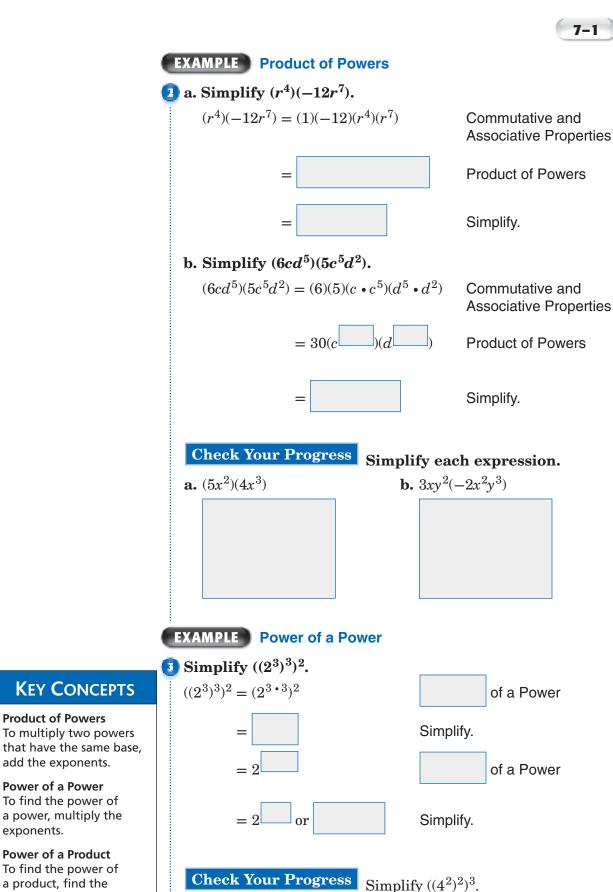
	Expression	Monomial?	Reason
a.	17 - s	no	The expression involves subtraction, not the product, of two variables.
b.	$8f^2g$		The expression is the product of a number and two variables.
c.	$\frac{3}{4}$	yes	$\frac{3}{4}$ is a real number and an example of a constant.

**Check Your Progress** Determine whether each expression is a monomial. Explain your reasoning.

	Expression	Monomial?	Reason
a.	$x^5$		
b.	3p - 1		
c.	$\frac{9x}{y}$		
d.	$\frac{cd}{8}$		

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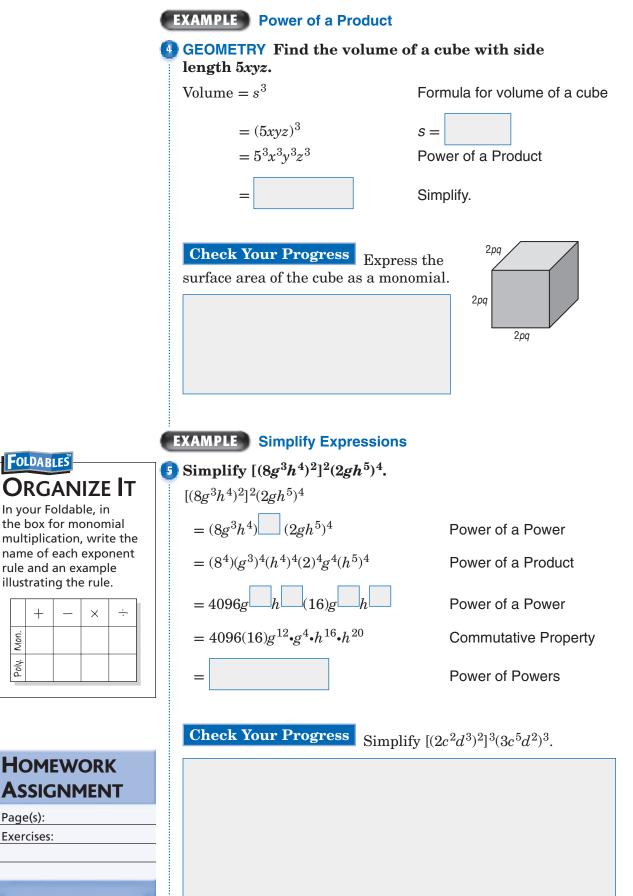


Power of a Power

power of each factor and multiply.

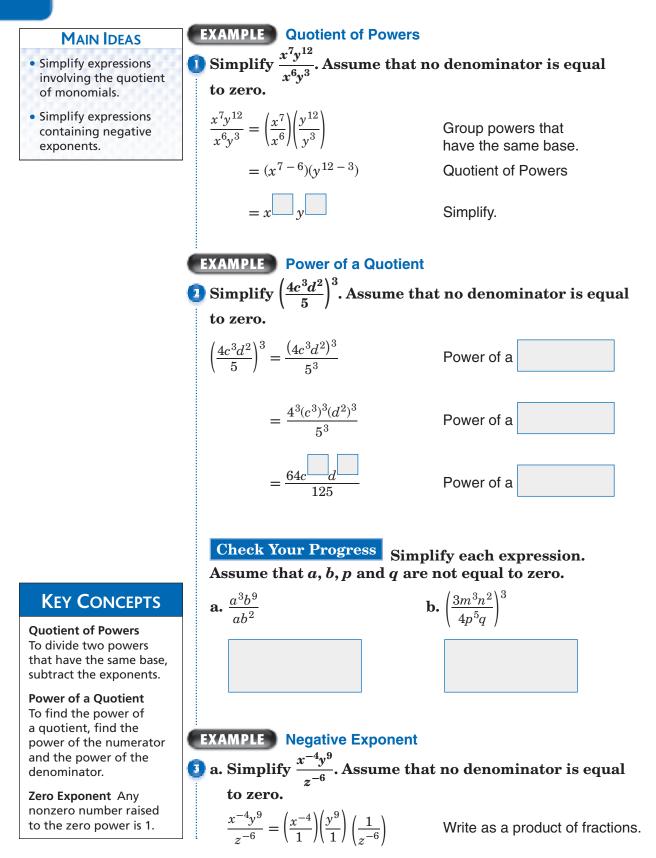
exponents.





# **Dividing Monomials**

7-2



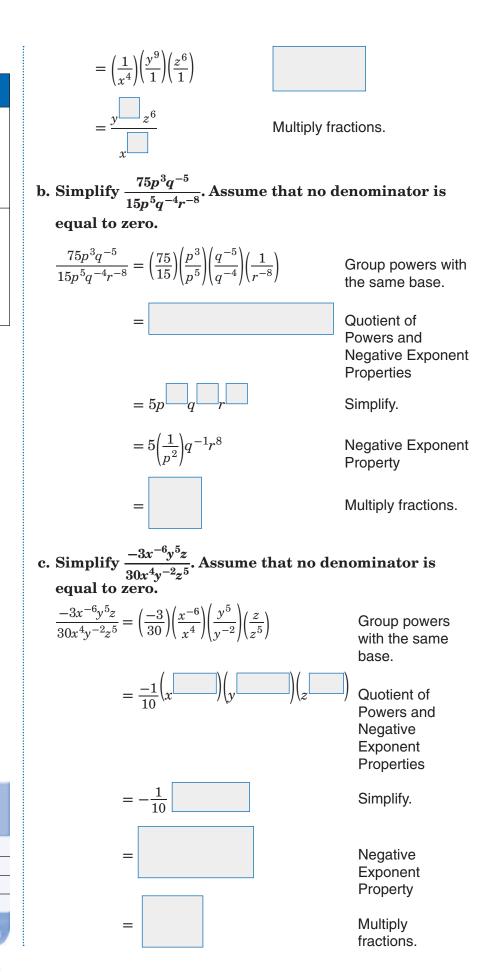
Glencoe Algebra 1 157



### KEY CONCEPT

Negative Exponent For any nonzero number aand any integer n,  $a^{-n}$ is the reciprocal of  $a^n$ . In addition, the reciprocal of  $a^{-n}$  is  $a^n$ .

FOLDABLES In your Foldable, in the monomial division box, write the name of each exponent rule in the lesson and an example illustrating the rule.



HOMEWORK

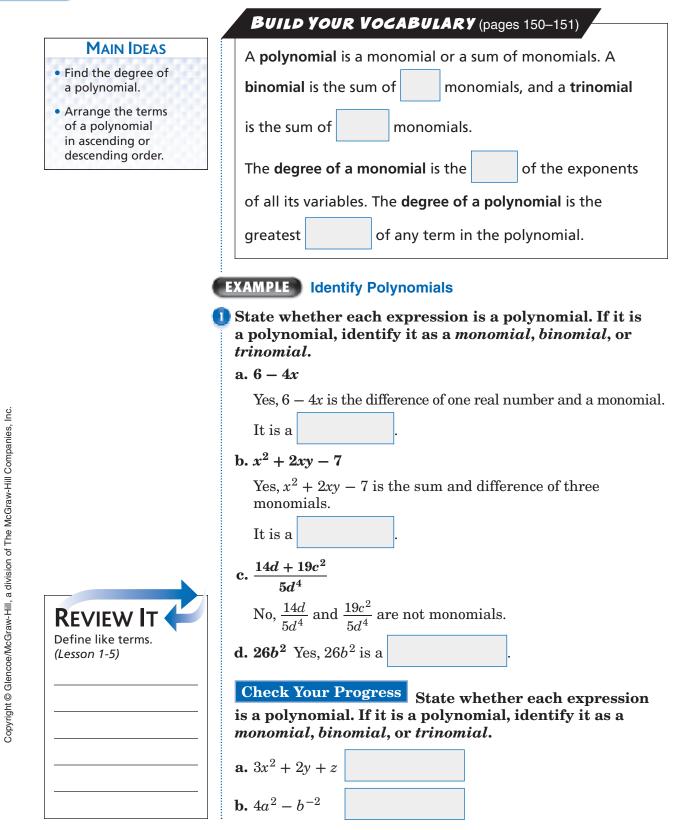
**ASSIGNMENT** 

Page(s):

Exercises:



# **Polynomials**





### EXAMPLE Degree of a Polynomial

	Polynomial	Terms	Degree of Each Term	Degree of Polynomial
a.	$12 + 5b + 6bc + 8bc^2$	$12, 5b, 6bc, 8bc^2$	0, 1, 2, 3	
b.	$9x^2 - 2x - 4$	$9x^2, -2x, \\ -4$		
c.	$14g^2h^5i$			

#### 1 Find the degree of each polynomial.

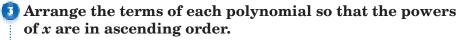
### **Check Your Progress**

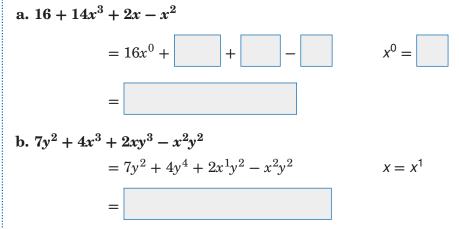
### Find the degree of each

polynomial.

	Polynomial	Terms	Degree of Each Term	Degree of Polynomial
a.	$11ab + 6b + 2ac^2 - 7$			
b.	$3r^3 + 5r^2s^2 - s^3$			
с.	$2x^5yz - x^2yz^2$			

#### **EXAMPLE** Arrange Polynomials in Ascending Order





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#### EXAMPLE Arrange Polynomials in Descending Order

Arrange the terms of each polynomial so that the powers
 i of x are in descending order.

a. 
$$8 + 7x^2 - 12xy^3 - 4x^3y$$
  
 $= 8x^0 + 7x^2 - 12x^1y^3 - 4x^3y$   
 $x^0 = 1 \text{ and } x = x^1$   
 $=$   
b.  $a^4 + ax^2 - 2a^3xy^3 - 9x^4y$   
 $= a^4x^0 + a^1x^2 - 2a^3x^1y^3 - 9x^4y^1$   
 $x^0 = 1 \text{ and } x = x^1$   
 $=$ 

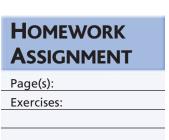
**Check Your Progress** Arrange the terms of each polynomial so that the powers of *x* are in descending order.

**a.**  $6x^2 - 3x^4 - 2x + 1$ 

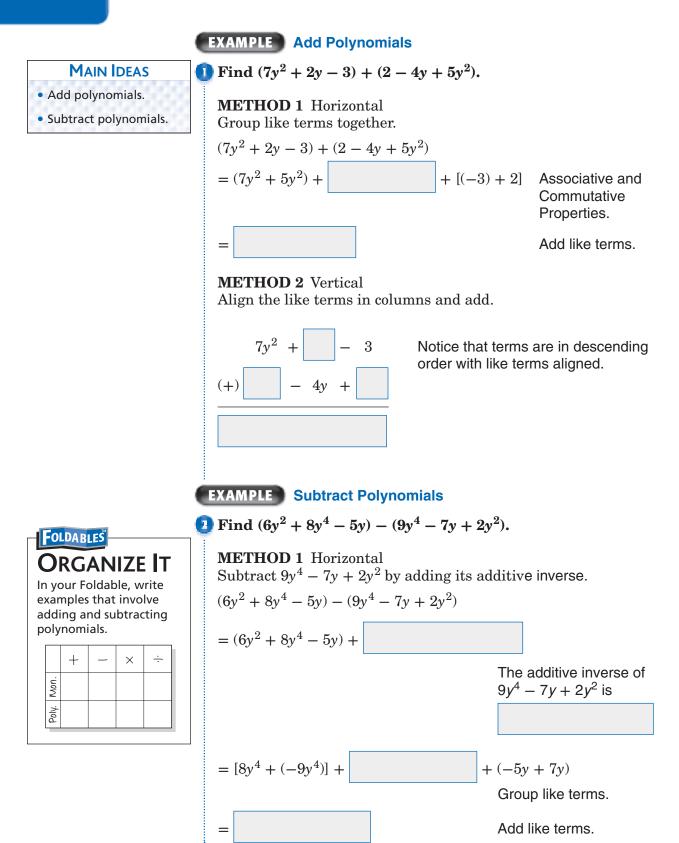
**b.**  $3 - 2xy^4 + 4x^3yz - x^2$ 

**c.**  $3x^3 + 4x^4 - x^2 + 2$ 

**d.**  $2y^5 - 7y^3x^2 - 8x^3y^2 - 3x^5$ 



# **Adding and Subtracting Polynomials**

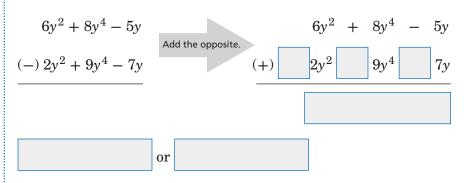


7-4



#### METHOD 2 Vertical

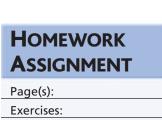
Align like terms in columns and subtract by adding the additive inverse.



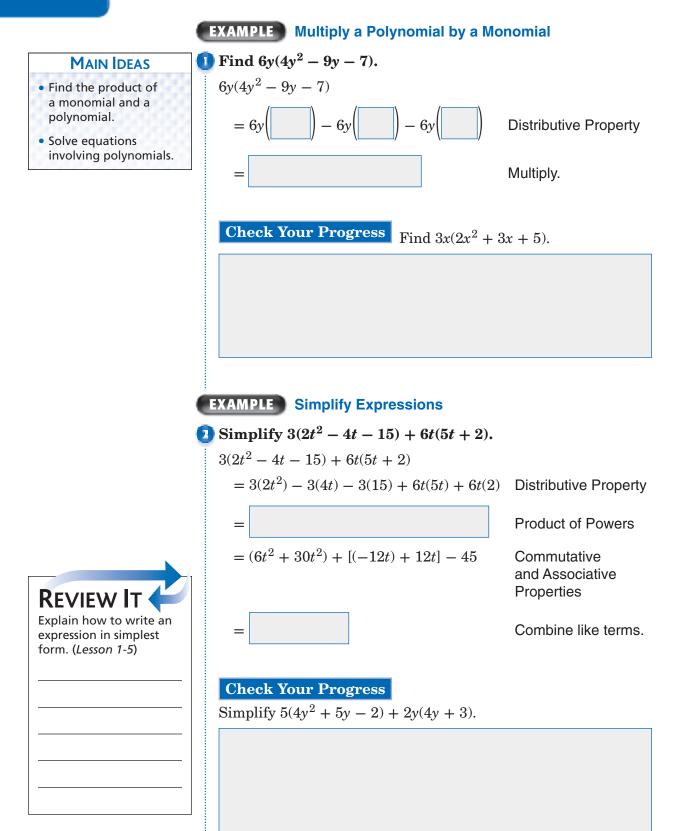
### **Check Your Progress**

**a.** Find  $(3x^2 + 2x - 1) + (-5x^2 + 3x + 4)$ .

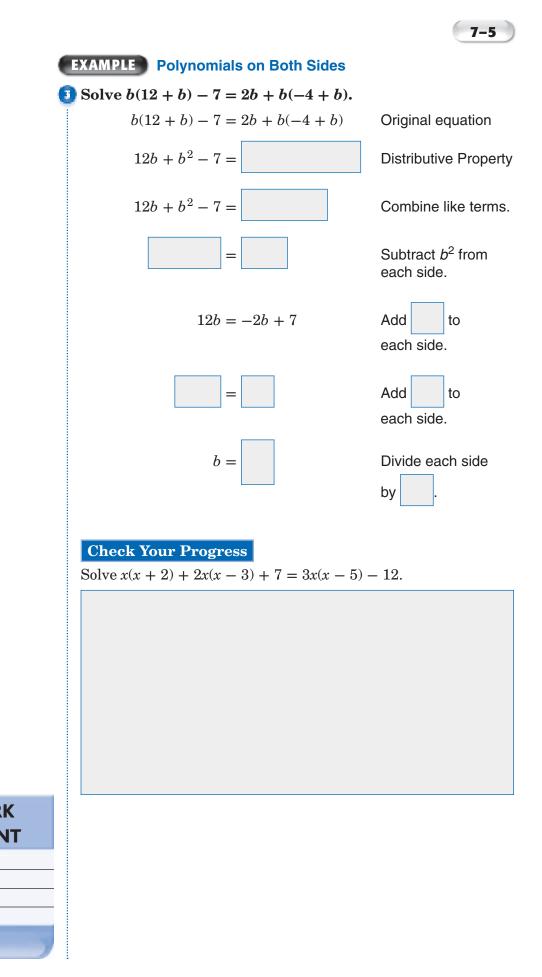
**b.** Find  $(3x^3 + 2x^2 - x^4) - (x^2 + 5x^3 - 2x^4)$ .



# **Multiplying a Polynomial by a Monomial**



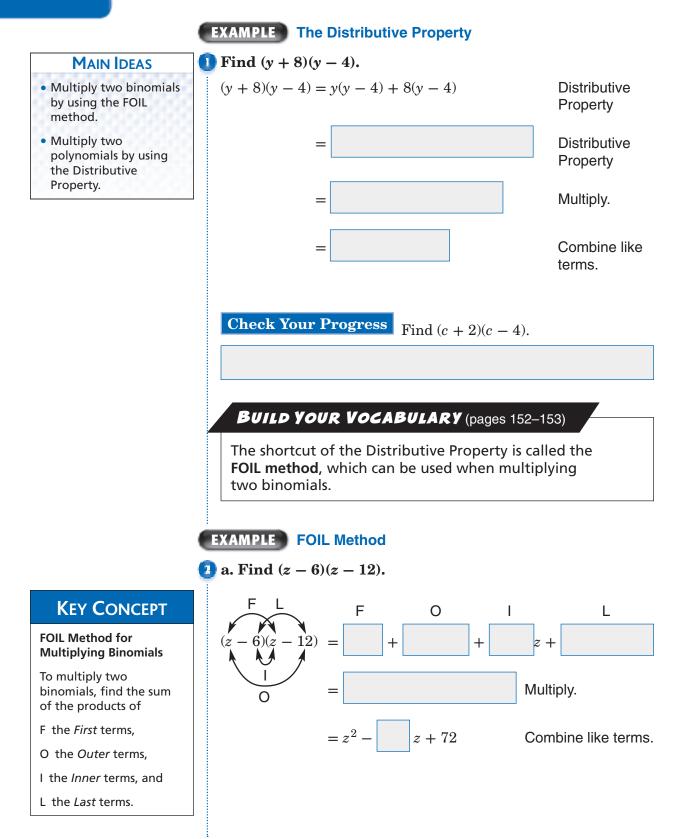
7-5

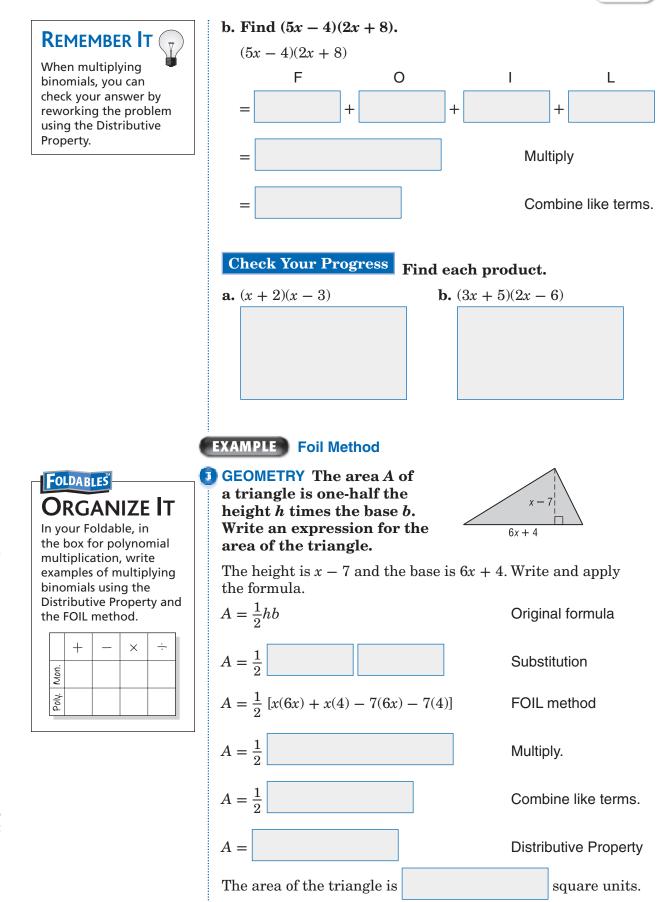


HOMEWORK **ASSIGNMENT** Page(s): Exercises:

# **Multiplying Polynomials**

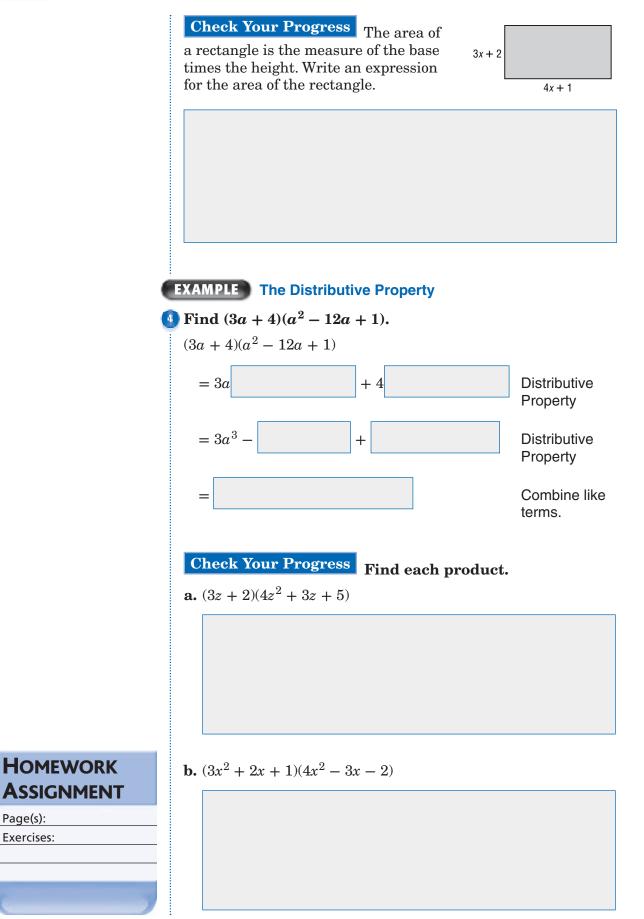
7-6





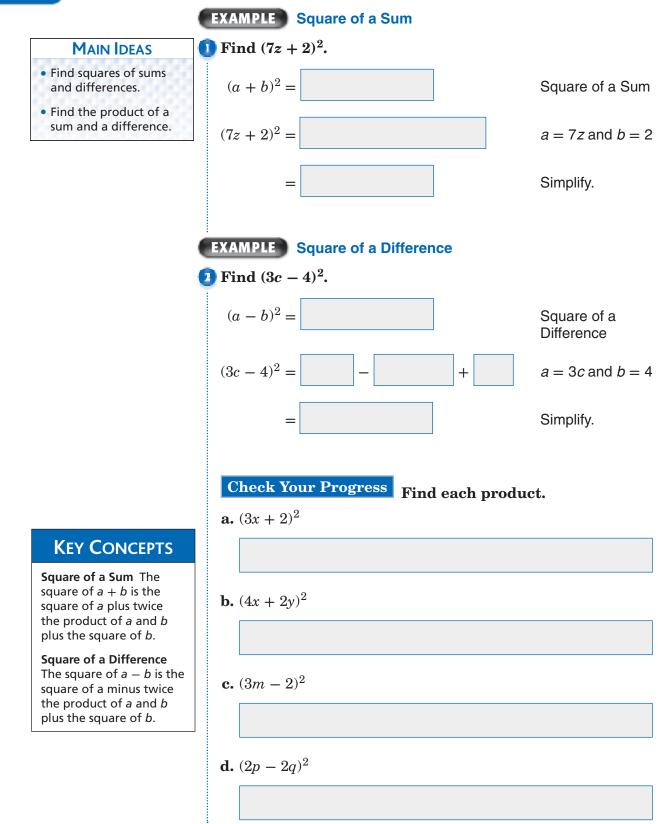
7-6





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# **7–7** Special Products

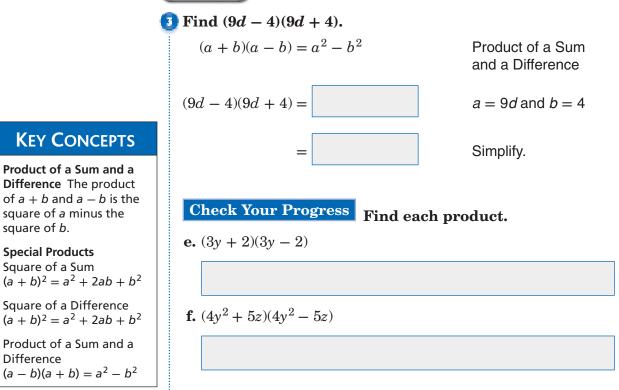


7-7

square of b.

Difference

### **EXAMPLE** Product of a Sum and a Difference





Page(s):

Exercises:



# **BRINGING IT ALL TOGETHER**

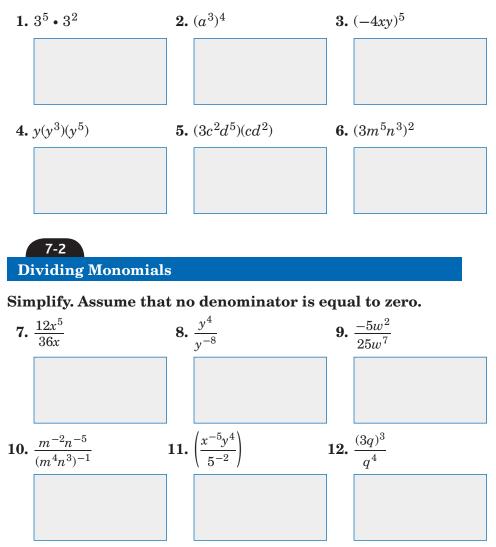
# STUDY GUIDE

FOLDABLES	Vocabulary Puzzlemaker	Build your Vocabulary
Use your <b>Chapter 7 Foldable</b> to help you study for your chapter test.	To make a crossword puzzle, word search, or jumble puzzle of the vocabulary words in Chapter 7, go to: glencoe.com	You can use your completed <b>Vocabulary Builder</b> ( <i>pages 152–153</i> ) to help you solve the puzzle.

### 7-1

**Multiplying Monomials** 

### Simplify.







**13.** Complete the table.

	monomial	binomial	trinomial	polynomial with more than three terms
Example	$3r^2t$	$2x^2 + 3x$	$5x^2 + 3x + 2$	$7s^2 + s^4 + 2s^3 - s + 5$
Number of Terms				

14. What is the degree of the polynomial  $4x^4 + 2x^3y^3 + y^2 + 14$ ? Explain how you found your answer.

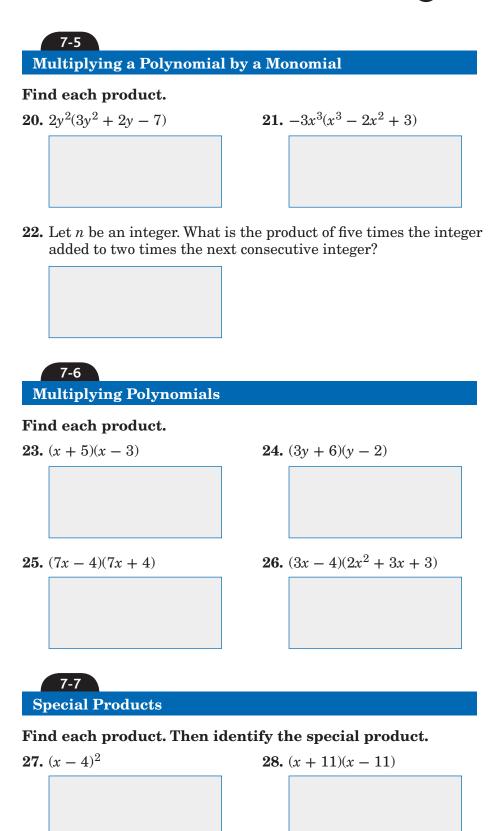
**15.** Use a dictionary to find the meaning of the terms *ascending* and *descending*. Write their meanings and then describe a situation in your everyday life that relates to them.

7-4 Adding and Subtracting Polynomials

#### Find each sum or difference.

**16.** 
$$(3k - 8) + (7k + 12)$$
  
**17.**  $(w^2 + w - 4) + (7w^2 - 4w + 10)$   
**18.**  $(7h^2 + 4h - 8) - (3h^2 - 2h + 10)$   
**19.**  $(17n^4 + 2n^3) - (10n^4 + n^3)$ 

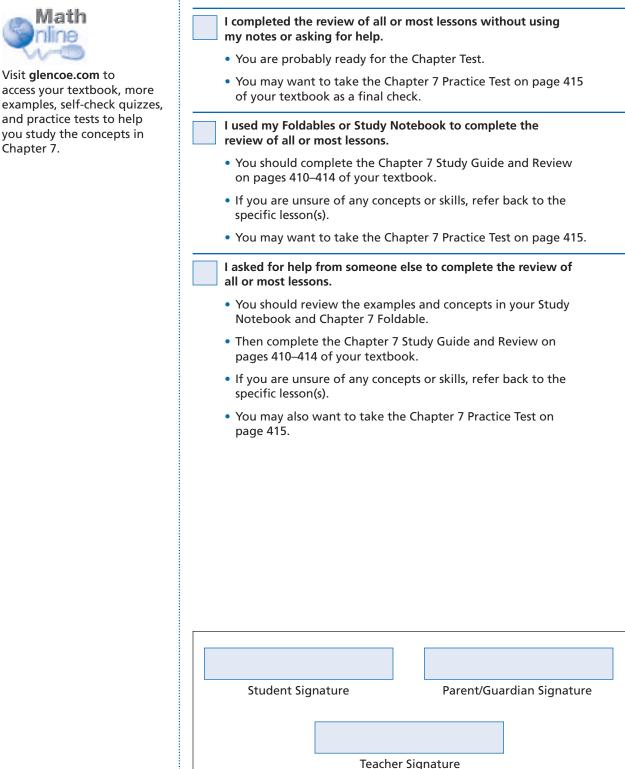
8)





# ARE YOU READY FOR THE CHAPTER TEST?

Check the one that applies. Suggestions to help you study are given with each item.

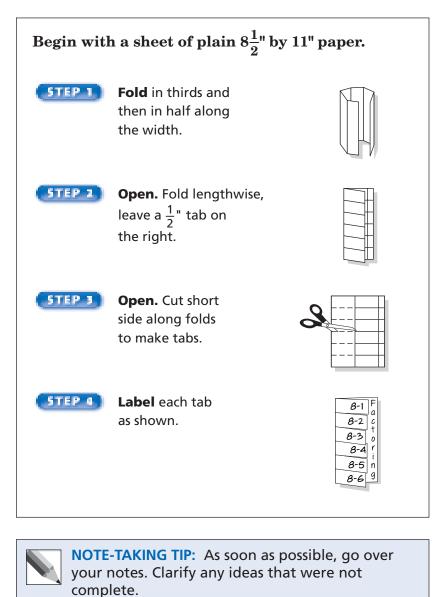




# **Factoring**



Use the instructions below to make a Foldable to help you organize your note as you study the chapter. You will see Foldable reminders in the margin of this Interactive Study Notebook to help you in taking notes.





## BUILD YOUR VOCABULARY

This is an alphabetical list of new vocabulary terms you will learn in Chapter 8. As you complete the study notes for the chapter, you will see Build Your Vocabulary reminders to complete each term's definition or description on these pages. Remember to add the textbook page number in the second column for reference when you study.

Found on Page	Definition	Description or Example

Vocabulary Term	Found on Page	Definition	Description or Example
perfect square <u>trinomial</u> try·NOH·mee·uhl			
prime_factorization FAK·tuh·ruh·ZAY·shuhn			
prime number			
prime polynomial			
roots			
Zero Products Property			



# **Monomials and Factoring**

#### MAIN IDEAS

- Find prime factorizations of integers and monomials.
- Find the greatest common factors of integers and monomials.

## KEY CONCEPT

Prime and Composite Numbers A whole number greater than 1 whose only factors are 1 and itself is called a prime number.

A whole number, greater than 1 that has more than two factors is called a **composite number**.

## BUILD YOUR VOCABULARY (pages 176-177)

When a whole number is expressed as a product of

that are all

is called the **prime factorization** of the number.

A monomial is in **factored form** when it is expressed as the

numbers, the expression

and no

variable has an exponent greater than 1.

## **EXAMPLE** Prime Factorization of a Monomial

1 Factor  $18x^3y^3$  completely.

 $18x^{3}y^{3} = 2 \cdot 9 \cdot x \cdot x \cdot y \cdot y \cdot y$   $18 = 2 \cdot 9, x^{3} = x \cdot x \cdot x,$ and  $y^{3} = y \cdot y \cdot y$   $= 2 \cdot x \cdot x \cdot x \cdot y \cdot y \cdot y$ in factored form is  $2 \cdot 3 \cdot 3 \cdot x \cdot x \cdot y \cdot y \cdot y$ .
Check Your Progress
Factor each monomial

completely.

**a.**  $15a^{3}b^{2}$ 

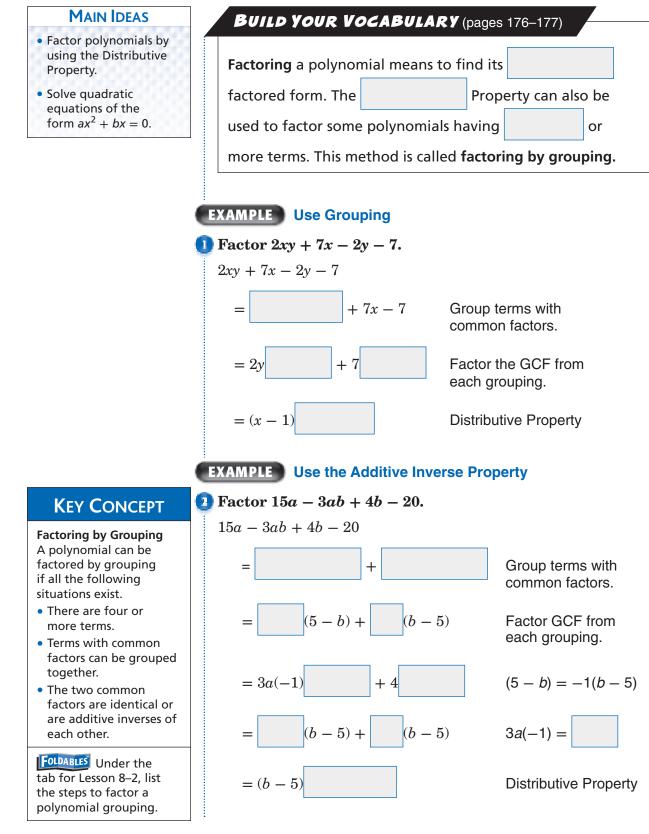
**b.**  $-45xy^2$ 

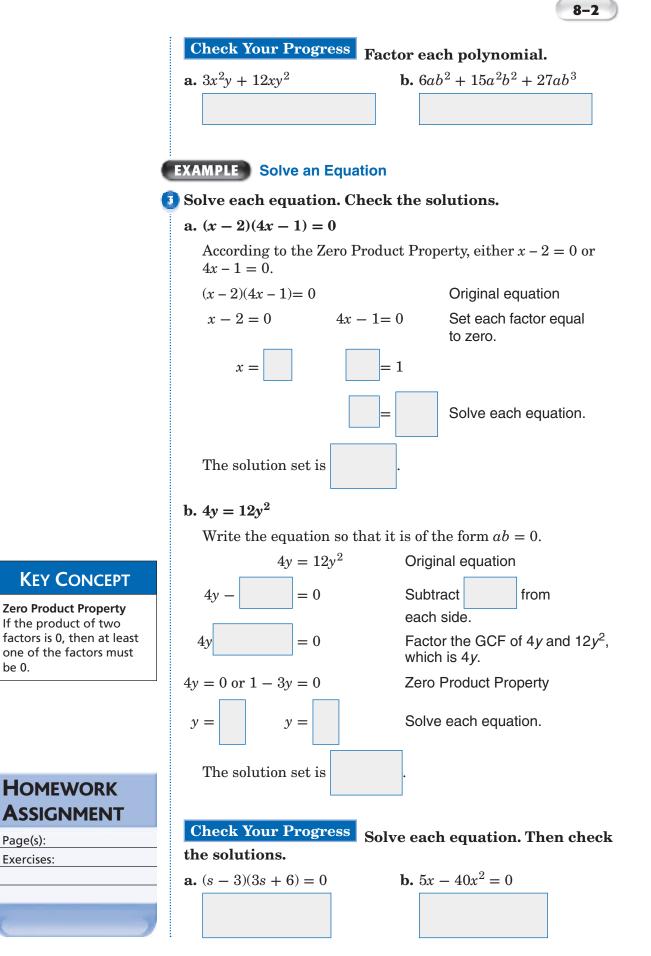
KEY CONCEPT	BUILD YOUR VOCABULARY (pages 176	–177)			
Greatest Common Factor (GCF)	The greatest common factor ( ) of	two or more			
<ul> <li>The GCF of two or more monomials is the product of their</li> </ul>	integers is the product of the	common			
common factors when each monomial is in factored form.	the integers.				
<ul> <li>If two or more integers or monomials have</li> <li>CCE of 1 than the</li> </ul>	EXAMPLE Finding GCF				
a GCF of 1, then the integers or monomials are said to be <i>relatively</i>	<b>2</b> GEOMETRY The sides of a trianlge are $12wz^2$ , $8wz$ , and $16w^2z$ . Find the GCF of the three sides.				
prime.	Find the factors of $12wz^2$ , $8wz$ , and $16w^2z$ . The factors of $12wz^2$ , are				
	The factors of 8 <i>wz</i> are	 ]•			
	The factors of $16w^2z$ are	].			
	So, the GCF is				
Foldables	<b>EXAMPLE</b> GCF of a set of Monomials				
ORGANIZE IT	<b>[]</b> Find the GCF of $27a^2b$ and $15ab^2c$ .				
Under the tab for Lesson 8–1, write a	$27a^2b = \textcircled{0} \cdot 3 \cdot 3 \cdot 2 \cdot a \cdot b$ Factor each numb				
monomial that can be factored. Then factor	$15ab^2c = \textcircled{0} \cdot 5 \cdot \textcircled{0} \cdot \cancel{b} \cdot b \cdot c$ Circle the commo	n prime factors			
the monomial.	The GCF of $27a^2b$ and $15ab^2c$ is				
$\begin{array}{c} \mathbf{B}^{-1} \\ \mathbf{B}^{-2} \\ \mathbf{B}^{-3} \\ \mathbf{B}^{-3} \end{array}$	Check Your Progress Find the GCF of				
8-4 r 8-5 n	<b>Check Your Progress</b> Find the GCF of a monomials.	each set of			
8-6 9	<b>a.</b> 15 and 35 <b>b.</b> $39x^2y^3$ and	$26xy^4$			
HOMEWORK					
ASSIGNMENT					
Page(s): Exercises:					

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## 8-2

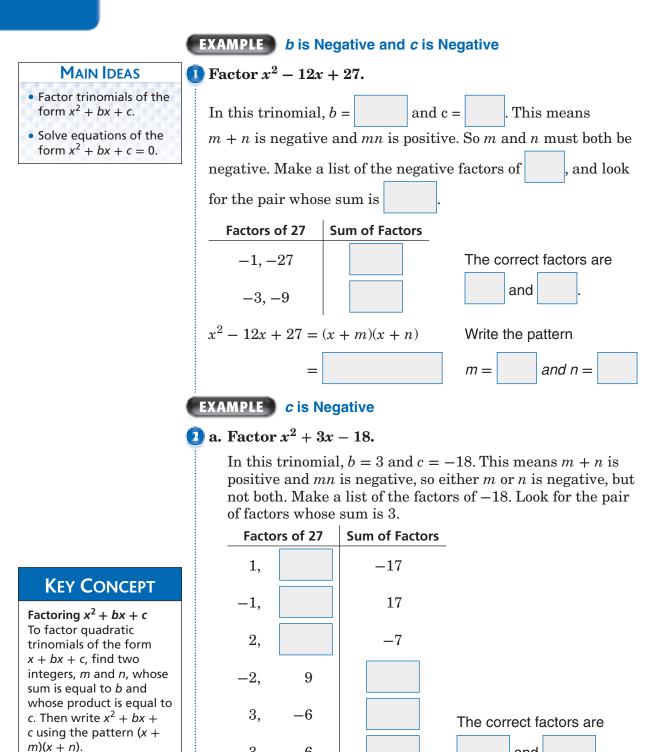
# **Factoring Using the Distributive Property**





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# Factoring Trinomials: $x^2 + bx + c$



-3,

6

 $x^2 + 3x - 18 = (x + m)(x + n)$ 

=



and

and n =

Write the pattern.

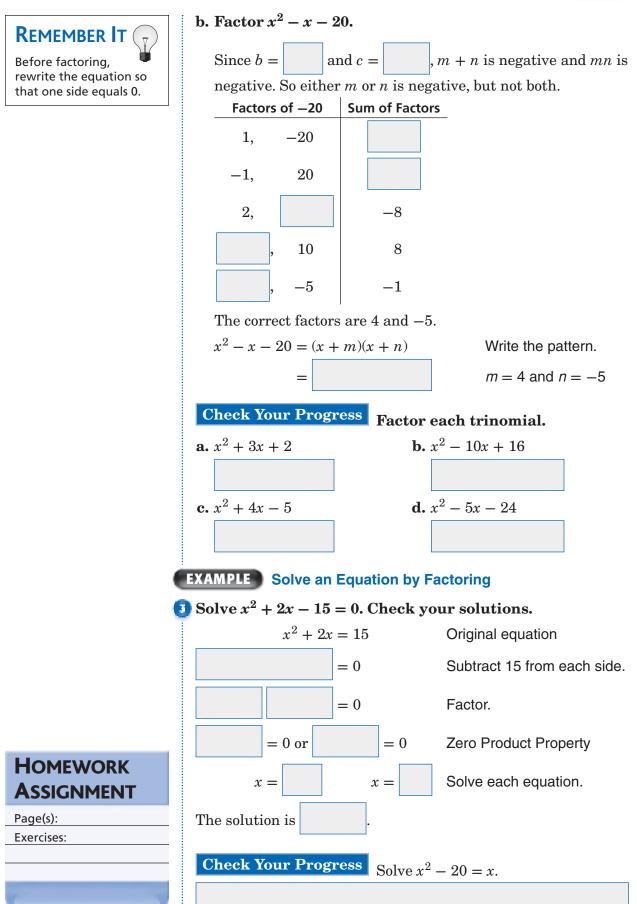
m =

FOLDABLES Take notes explaining how to factor

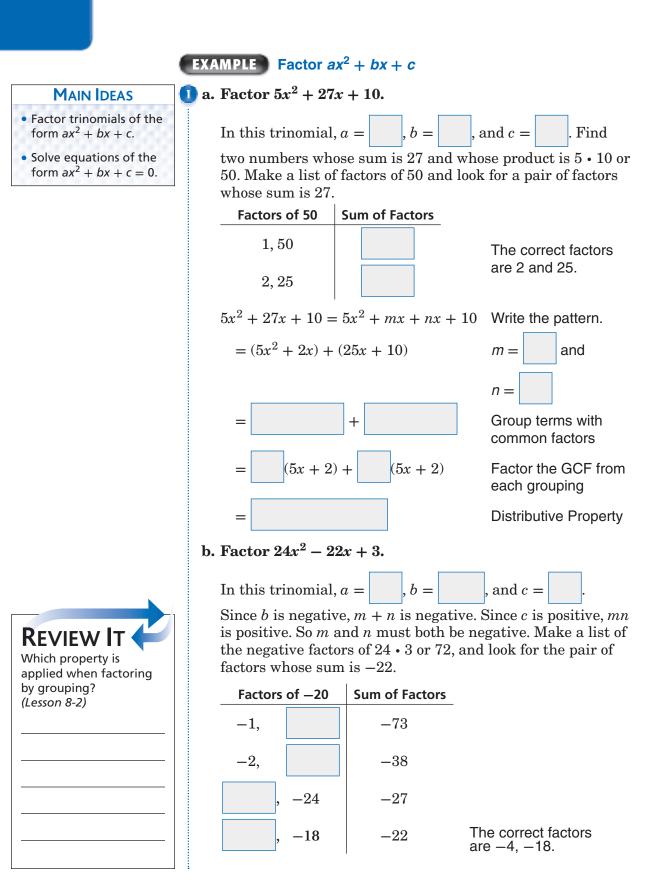
trinomials in the form  $x^2 + bx + c$ . Include

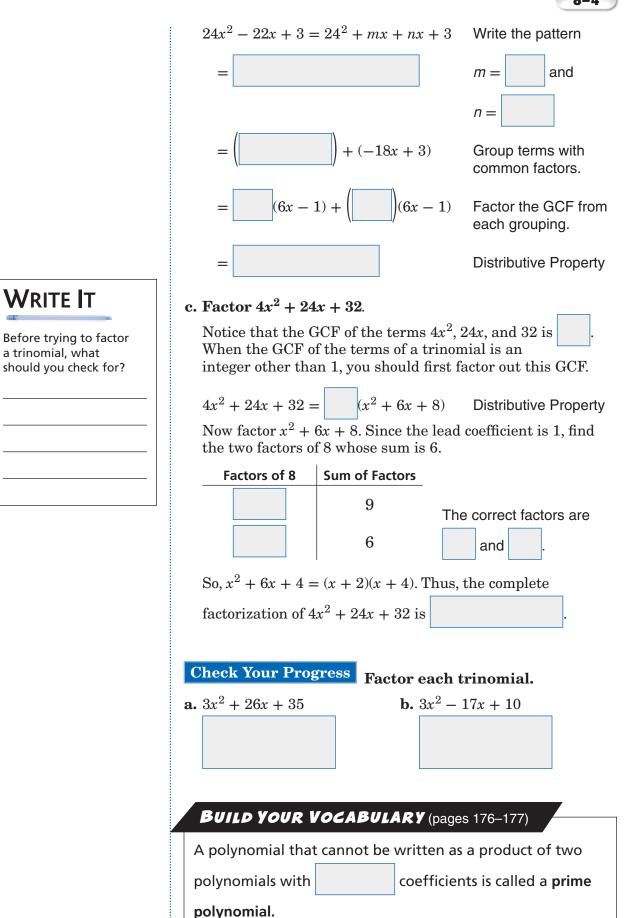
examples.





# **Factoring Trinomials:** $ax^2 + bx + c$





8 - 4

FOLDABLES

Under the tab for Lesson 8-4, list the steps you use to solve equations by factoring.

Organize It

8-1 8-2

8-3 8-4

8-5 8-6

#### **EXAMPLE** Determine Whether a Polynomial is Prime

#### **P** Factor $3x^2 + 7x - 5$ .

In this trinomial, a = 3, b = 7, and c = -5. Since b is positive, m + n is positive. Since c is negative, mn is negative, so either *m* or *n* is negative, but not both. Make a list of all the factors of 3(-5) or -15. Look for the pair of factors whose sum is 7.

Factors of -15	Sum of Factors	Factors of -15	Sum of Factors			
-1, 15		-3, 5				
1, -15		3, -5				
There are no integral factors whose sum is 7. Therefore						

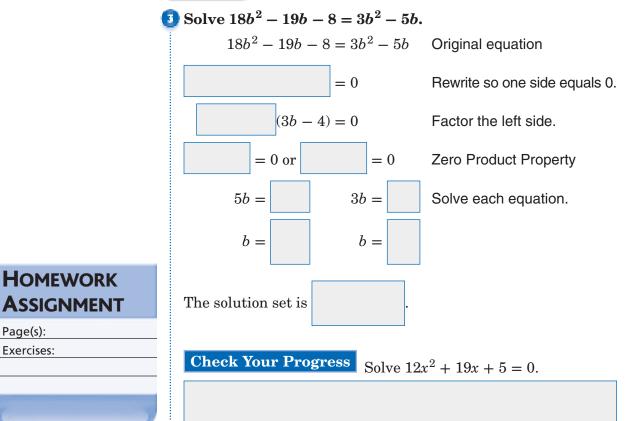
al factors whose sum is 7. Therei

 $3x^2 + 7x - 5$  is a

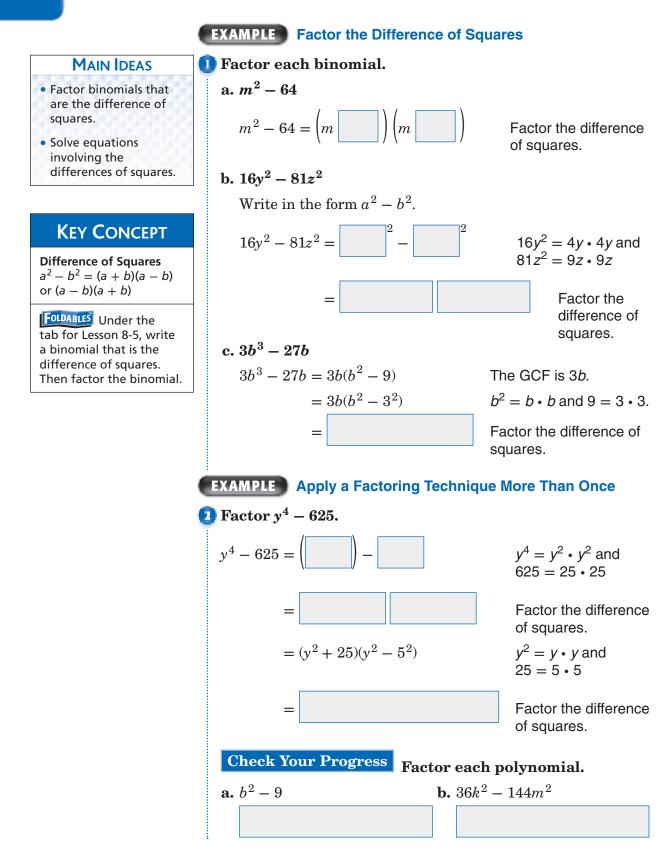
## Check Your Progress Factor each trinomial. If the trinomial cannot be factored using integers, write prime.



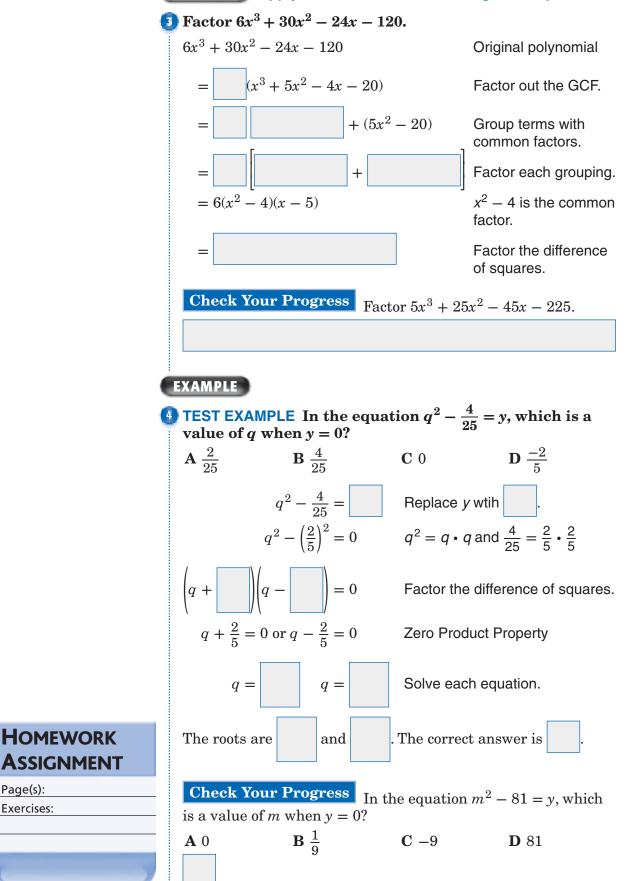
#### **EXAMPLE** Solve Equations by Factoring



# **Factoring Differences of Squares**



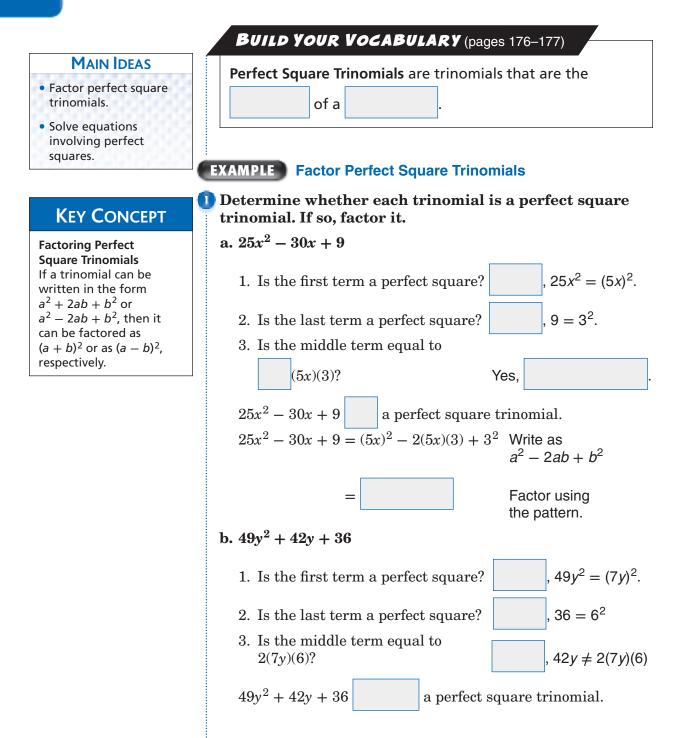
#### EXAMPLE Apply Several Different Factoring Techniques



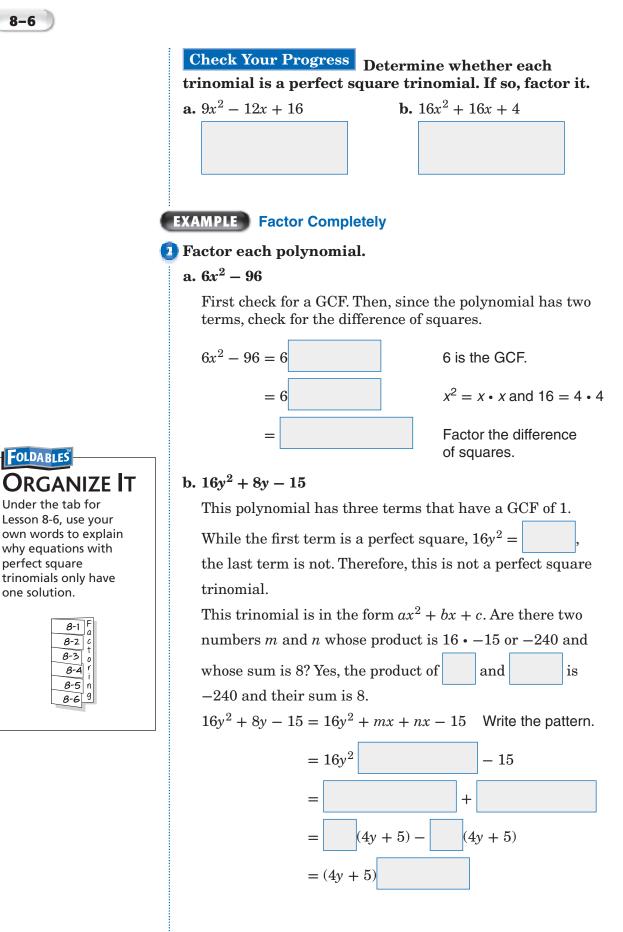
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# **Perfect Squares and Factoring**



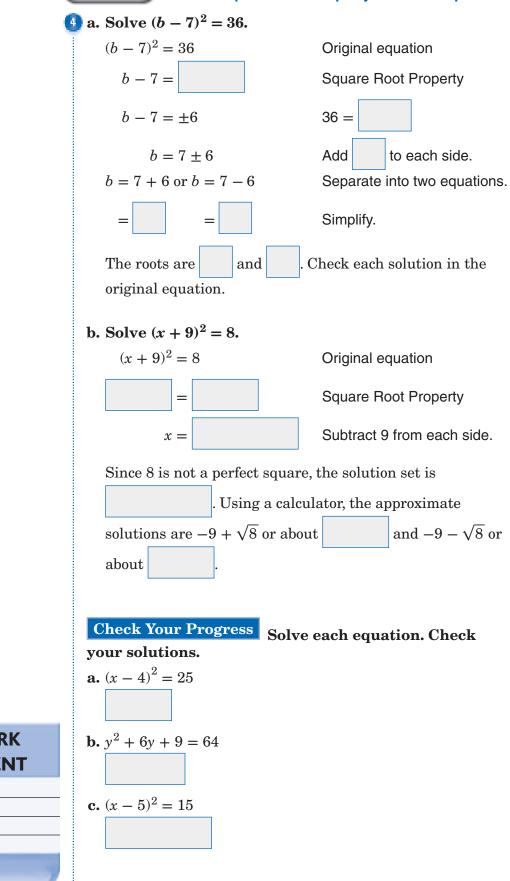
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Check Your Progress Factor eac	h polynomial.
<b>a.</b> $3x^2 - 3$ <b>b.</b> $4x^2$	+ 10x + 6
EXAMPLE Solve Equations with Repo	eated Factors
Solve $4x^2 + 36x + 81 = 0$ . $4x^2 + 36x + 81 = 0$	Original equation
$\left( \begin{array}{c} \\ \end{array} \right)^2 + 2 \begin{array}{c} \\ \end{array} + \begin{array}{c} \\ \end{array}^2 = 0$	Recognize $4x^2 + 36x + 81$ as a perfect square trinomial.
= 0	Factor the perfect square trinomial.
= 0	Set the repeated factor equal to zero
x =	Solve for <i>x</i> .
Thus, the solution set is	
<b>Check Your Progress</b> Solve $9x^2 -$	30x + 25 = 0.
Build Your Vocabulary (pa	ages 176–177)
The square root property states that	
if $x^2 = n$ , then $x = \sqrt{n}$ .	

#### EXAMPLE Use the Square Root Property To Solve Equations



Homework Assignment

Page(s): Exercises:



# **BRINGING IT ALL TOGETHER**

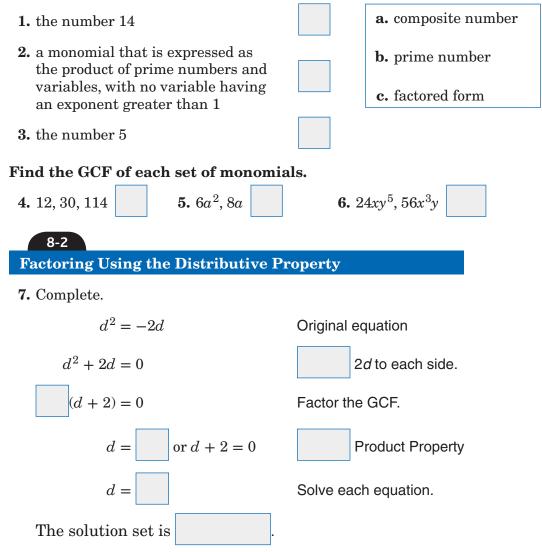
## STUDY GUIDE

<b>FOLDABLES</b>	Vocabulary Puzzlemaker	Build your Vocabulary
Use your <b>Chapter 8 Foldable</b> to help you study for your chapter test.	To make a crossword puzzle, word search, or jumble puzzle of the vocabulary words in Chapter 8, go to: glencoe.com	You can use your completed <b>Vocabulary Builder</b> ( <i>pages 176–177</i> ) to help you solve the puzzle.

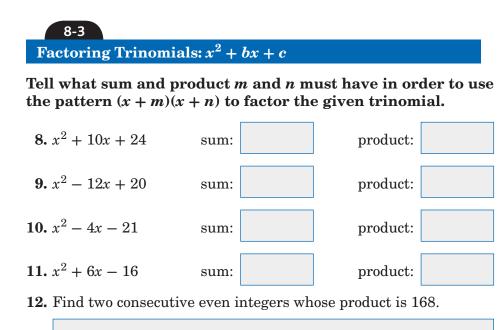
8-1

#### **Factors and Greatest Common Factors**

#### Choose the letter of the term that best matches each phrase.



## Chapter 8 BRINGING IT ALL TOGETHER



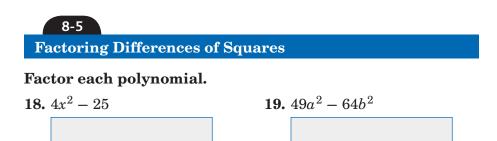


Factor each trinomial, if possible. If the trinomial cannot be factored using integers, write *prime*.

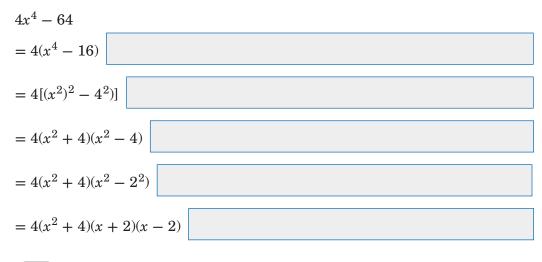
- 13.  $2b^2 + 10b + 12$  14.  $4y^2 + 4y 3$  

   15.  $12x^2 4y 5$  16.  $10x^2 9x + 6$
- **17.** Explain how you know that the trinomial  $2x^2 7x + 4$  is a prime polynomial.





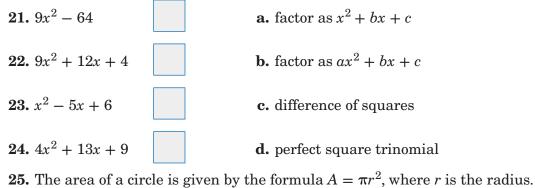
**20.** Explain what is done in each step to factor  $4x^4 - 64$ .



#### 8-6

**Perfect Squares and Factoring** 

Match each polynomial from the first column with a factoring technique in the second column. Some of the techniqes may be used more than once. If none of the techniques can be used to factor the polynomial, write *none*.

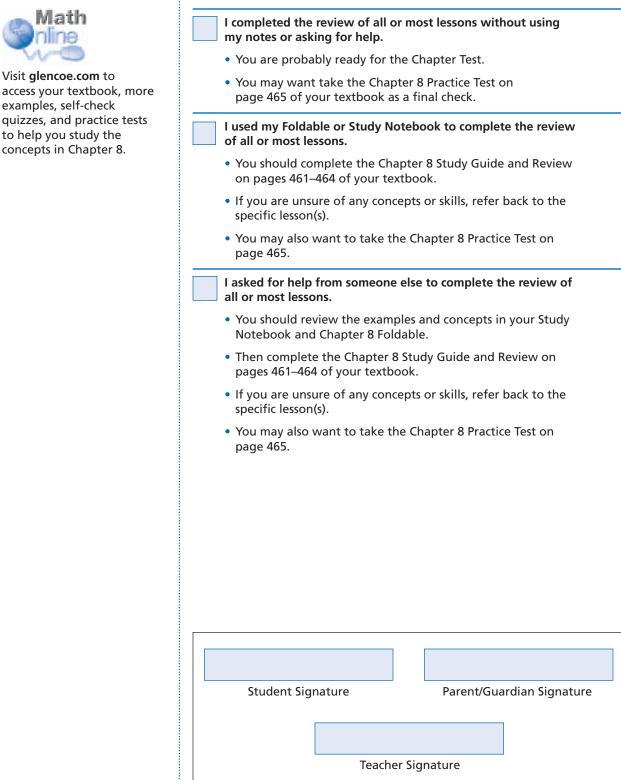


**25.** The area of a circle is given by the formula  $A = \pi r^2$ , where *r* is the radius. If increasing the radius of a circle by 3 inches gives the resulting circle an area of  $81\pi$  square inches, what is the radius of the original circle?



# ARE YOU READY FOR THE CHAPTER TEST?

Check the one that applies. Suggestions to help you study are given with each item.

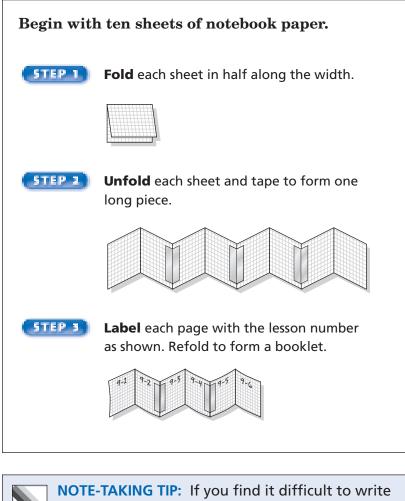




# **Quadratic and Exponential Functions**



Use the instructions below to make a Foldable to help you organize your notes as you study the chapter. You will see Foldable reminders in the margin of this Interactive Study Notebook to help you in taking notes.



**NOTE-TAKING TIP:** If you find it difficult to write and pay attention at the same time, ask your instructor if you may record the classes with a tape recorder.



## BUILD YOUR VOCABULARY

This is an alphabetical list of new vocabulary terms you will learn in Chapter 9. As you complete the study notes for the chapter, you will see Build Your Vocabulary reminders to complete each term's definition or description on these pages. Remember to add the textbook page number in the second column for reference when you study.

Vocabulary Term	Found on Page	Definition	Description or Example
axis of <u>symmetry</u> [SIH·muh·tree]			
completing the square			
compound interest			
discriminant			
double root			
exponential decay [EHK·spuh·NEHN·chul]			
exponential function			
exponential growth			

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Vocabulary Term	Found on Page	Definition	Description or Example
maximum			
minimum			
parabola [puh·RA·buh·luh]			
<u>quadratic</u> equation [kwah·dra·tihk]			
Quadratic Formula			
quadratic function			
roots			
symmetry			
vertex			
zeros			



**MAIN IDEAS** 

 Graph quadratic functions.

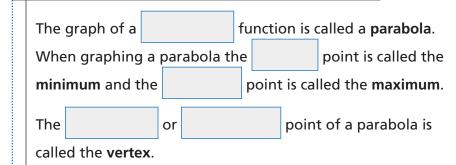
parabola.

Find the equation of

the axis of symmetry and the coordinates of the vertex of a

# **Graphing Quadratic Functions**

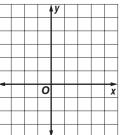
## BUILD YOUR VOCABULARY (pages 198–199)



## EXAMPLE Graph Opens Upward

# **1** a. Use a table of values to graph $y = x^2 - x - 2$ .

Graph these ordered pairs and connect them with a smooth curve.

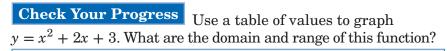


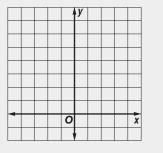
x	У
-2	
-1	0
0	
1	
2	0

b. What are the domain and range of this function?

Domain:

Range:  $\{y \mid$ 





## **KEY CONCEPT**

Quadratic Function A quadratic function can be described by an equation of the form  $y = ax^2 + bx + c$ , where  $a \neq 0$ .

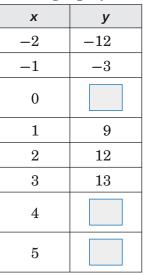
**FOLDABLES** On the page for Lesson 9-1, write an example of a quadratic function that opens upward. Then write an example of a quadratic function that opens downward. Copyright © Glencoe/McGraw-Hill, a division of The McGraw-Hill Companies, Inc



#### **EXAMPLE** Graph Opens Downward

**2** ARCHERY The equation  $y = -x^2 + 6x + 4$  represents the height y of an arrow x seconds after it is shot into the area.

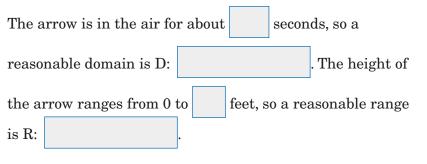
a. Use a table of values to graph  $y = -x^2 + 6x + 4$ .



Graph these ordered pairs and connect them with a smooth curve.

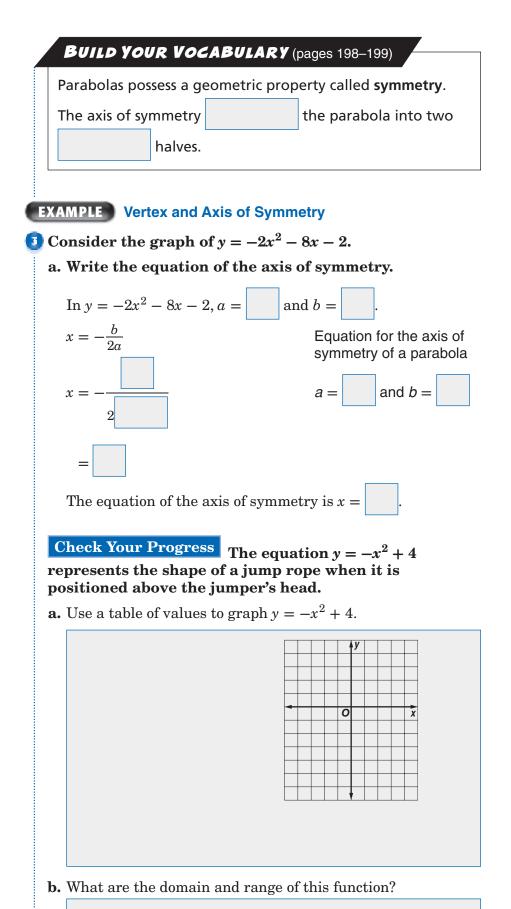
1	V							
14	Ľ.				<u> </u>			
12		-		-		-		
10				1	-			
8								
0								
6								
0								
-4				-				
2		-		-	-	-		
								X
	0		h (	h /		- (		7
0	01	4	Ł,	<b>p</b> 4	5	56	P	
-2								

- b. What are the mathematical domain and range of the function?
  - D:  $\{x | x \text{ is a real number}\}$
  - R:  $\{y | y \le 13\}$
- c. Describe reasonable domain and range values for this situation.



KEY CONCEPT

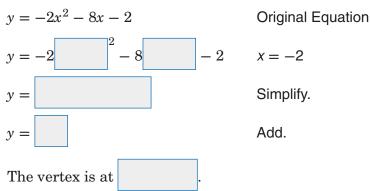
Equation of the Axis of Symmetry of a Parabola The equation of the axis of symmetry for the graph of  $y = ax^2 + bx + c$ , where  $a \neq 0$ , is  $x = -\frac{b}{2a}$ .





#### b. Find the coordinates of the vertex.

Since the equation of the axis of symmetry is x = -2 and the vertex lies on the axis, the *x*-coordinate for the vertex is -2.



c. Identify the vertex as a maximum or minimum.

Since the coeffic	ient	t of the $x^2$ term i	s	2
the parabola opens			a	nd the vertex is a
	poi	nt.		

#### d. Graph the function.

You can use the symmetry of the parabola to help you draw its graph. On a coordinate plane, graph the vertex and the axis of symmetry.

Choose a value for *x* other than -2. For example, choose -1and find the *y*-coordinate that satisfies the equation.

$$y = -2x^{2} - 8x - 2$$
 Original equation  

$$y = -2\left( \boxed{\phantom{x}} \right)^{2} - 8\left( \boxed{\phantom{x}} \right) - 2 \quad x = \boxed{\phantom{x}}$$

$$y = 4$$
 Simplify.

Since the graph is symmetrical about its axis of symmetry

, you can find another x =

point on the other side of the axis of symmetry. The point at

is 1 unit to the right

of the axis. Go 1 unit to the right of the axis. Go 2 unit to the left of the axis and plot the

## point

Repeat this for several other points. Then sketch the parabola.

Functions can be graphed using the symmetry of the parabola. See page 467

of your textbook.

**REMEMBER IT** 

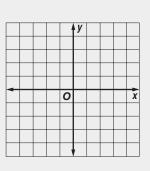
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0

X

**Check Your Progress** Consider the graph of  $y = 3x^2 - 6x + 1$ .

- **a.** Write the equation of the axis of symmetry.
- **b.** Find the coordinates of the vertex.
- c. Identify the vertex as a maximum or minimum.
- **d.** Graph the function.





Page(s):

Exercises:

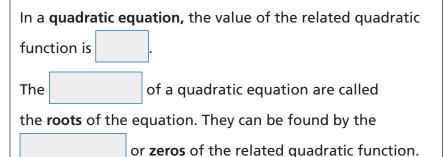


# **Solving Quadratic Equations by Graphing**

#### MAIN IDEAS

- Solve quadratic equations by graphing.
- Estimate solutions of quadratic equations by graphing.

## BUILD YOUR VOCABULARY (pages 198–199)



## EXAMPLE Two Roots

#### **1** Solve $x^2 - 3x - 10 = 0$ by graphing.

Graph the related function  $f(x) = x^2 - 3x - 10$ .

The equation of the axis of symmetry is  $x = -\frac{-3}{2(1)}$  or  $x = \frac{3}{2}$ .

When 
$$x = \frac{3}{2}$$
,  $f(x)$  equals  $(\frac{3}{2})^2 - 3(\frac{3}{2}) - 10$  or . So the

coordinates of the vertex are

Make a table of values to find other points to sketch the graph.

		8	y				
		4					
-	- <u>2</u>	0		Ź	4	6	x
		-4-					
		— —4- — —8-					

x	У
-3	8
-1	
0	-10
1	-12
2	
3	-10
4	
6	

To solve  $x^2 - 3x - 10 = 0$ , you need

to know where the value of f(x) is This occurs at the *x*-intercepts. The *x*-intercepts of the parabola

and

appear to be

9-2

#### EXAMPLE A Double Root

## **2** Solve $x^2 + 8x = -16$ by graphing.

First rewrite the equation so one side is equal to zero.

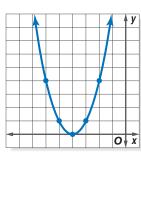
$$x^{2} + 8x = -16$$
$$x^{2} + 8x = -16$$
$$x^{2} + 8x = -16$$
$$x^{2} + 8x + 16 = -16$$

Add to each side. Simplify.

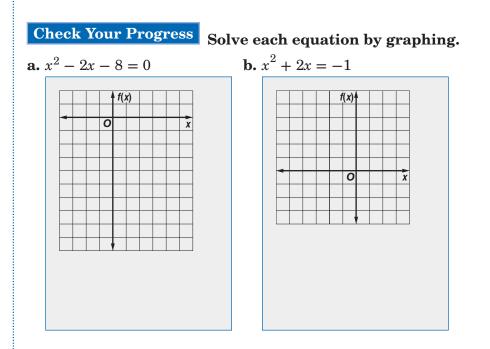
**Original equation** 

Graph the related function  $f(x) = x^2 + 8x + 16$ .

x	f(x)
-2	4
-3	
-4	
-5	
-6	



Notice that the vertex of the parabola is the *x*-intercept. Thus, one solution is \_\_\_\_\_. What is the other solution?

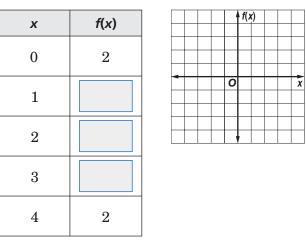


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#### **EXAMPLE** Rational Roots

Solve  $x^2 - 4x + 2 = 0$  by graphing. If integral roots cannot be found, estimate the roots by stating the consecutive integers between which the roots lie.

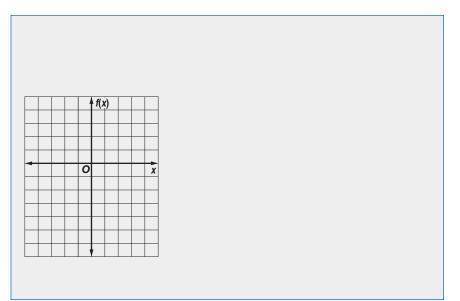
Graph the related function  $f(x) = x^2 - 4x + 2$ .

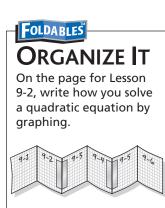


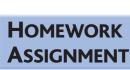
The *x*-intercepts of the graph are between 0 and 1 and between

3 and 4. One root is between and , and the other root is between and .

**Check Your Progress** Solve  $x^2 - 2x - 5$  by graphing. If integral roots cannot be found, estimate the roots by stating the consecutive integers between which the roots lie.





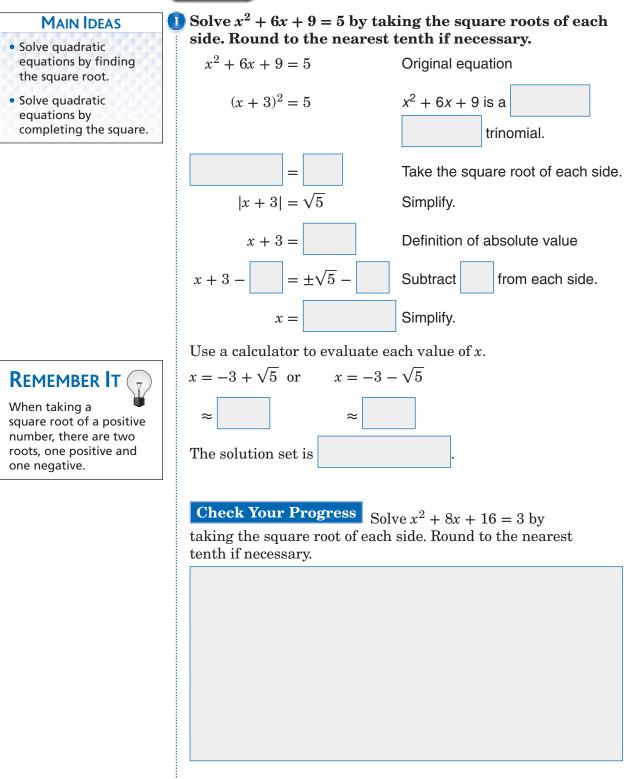


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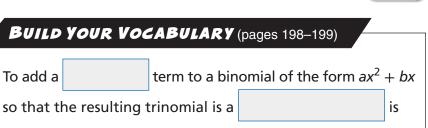
Exercises:

# Solving Quadratic Equations by Completing the Square

#### EXAMPLE Irrational Roots



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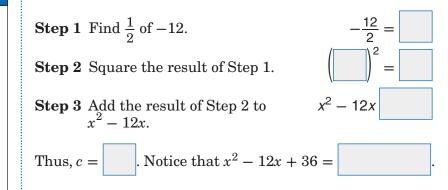


referred to as completing the square.

## EXAMPLE Complete the Square

**2** Find the value of c that makes  $x^2 - 12x + c$  a perfect square.

Complete the square.



**Check Your Progress** Find the value of *c* that makes  $x^2 + 14x + c$  a perfect square.

# **EXAMPLE** Solve an Equation by Completing the Square

# **(1)** Solve $x^2 - 18x + 5 = -12$ by completing the square.

**Step 1** Isolate the  $x^2$  and x terms.





 $x^2 - 18x =$ 

Subtract.

Simplify.

# KEY CONCEPT

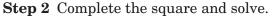
**Completing the Square** To complete the square for a quadratic expression of the form  $x^2 + bx$ , you can follow the steps below.

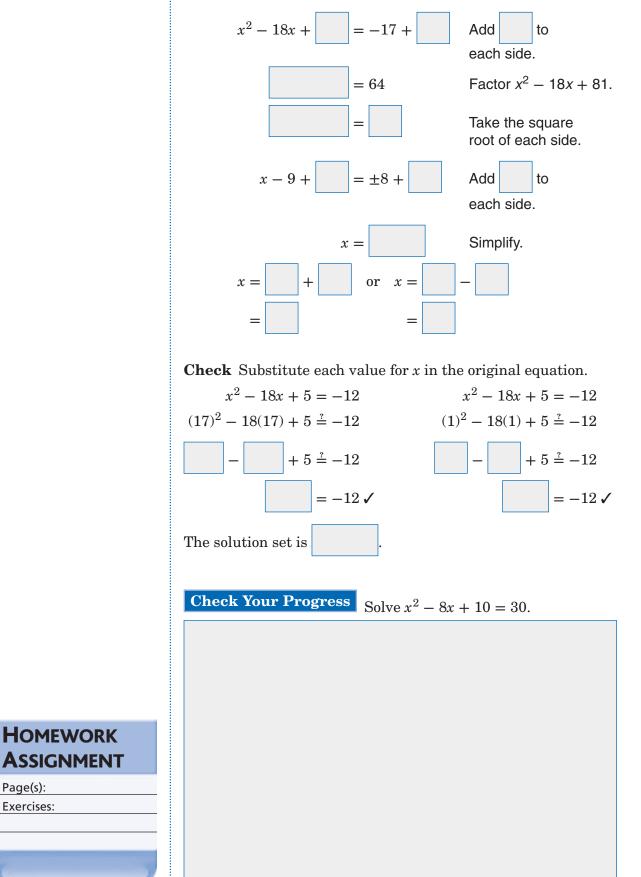
Step 1 Find  $\frac{1}{2}$  of *b*, the coefficient of *x*.

Step 2 Square the result of Step 1.

Step 3 Add the result of Step 2 to  $x^2 + bx$ , the original expression.

**FOLDABLES** On the page for Lesson 9-3, write the steps for completing the square.





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Page(s): Exercises:

# **Solving Quadratic Equations** by Using the Quadratic Formula

# **BUILD YOUR VOCABULARY** (pages 198–199) When solving the standard form of the equation for the result produces the Quadratic

Formula.

# **EXAMPLE** Solve Quadratic Equations

Solve each equation. Round to the nearest tenth if necessary.

## **KEY CONCEPT**

**MAIN IDEAS** 

equations by using the

determine the number of solutions for a guadratic equation.

Quadratic Formula. • Use the discriminant to

Solve quadratic

The Quadratic Formula The solutions of a quadratic equation in the form  $ax^2 + bx + c = 0$ , where  $a \pm 0$ , are given by the Quadratic Formula.  $-b \pm \sqrt{b^2 - 4ac}$ X =2a

FOLDABLES Write this formula in your Foldable. Be sure to explain the formula.

a. 
$$x^2 - 2x - 35 = 0$$

For this equation, a = 1, b = -2, and c = -35.

$$x = \frac{-b \pm \sqrt{b^2 - 4ac}}{2a}$$
Quadratic Formula  

$$= \frac{-(-2) \pm \sqrt{(-2)^2 - 4(1)(-35)}}{2(1)}$$
$$a = 1, b = -2, and c = -35$$
  

$$= \frac{2 \pm \sqrt{2}}{2}$$
Multiply.  

$$= \frac{2 \pm \sqrt{2}}{2}$$
Add.  

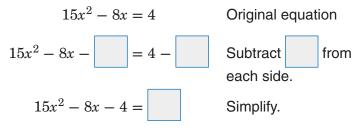
$$= \frac{2 \pm \sqrt{2}}{2}$$
Simplify.  

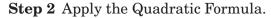
$$x = \boxed{2 \pm 2}$$
The solution set is  $\boxed{2}$ .

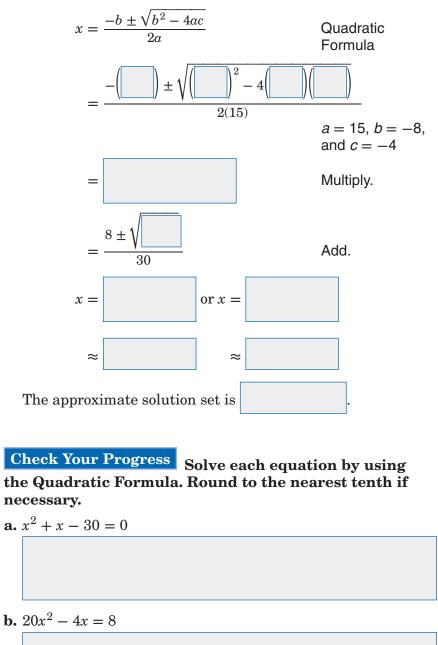
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## b. $15x^2 - 8x = 4$

Step 1 Rewrite the equation in standard form.

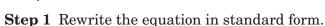


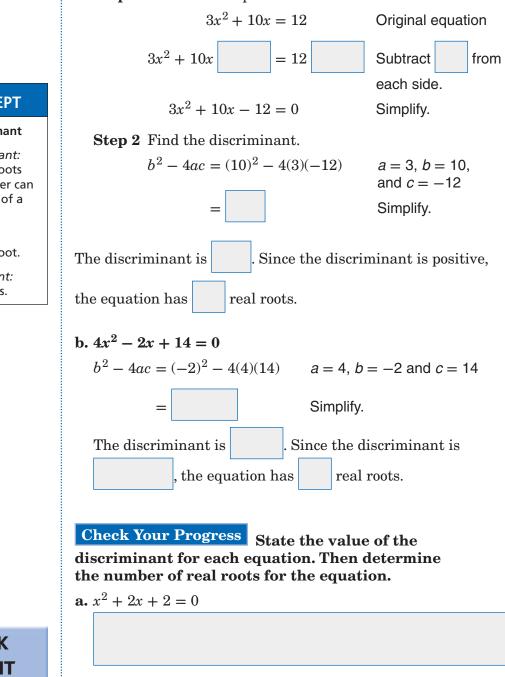




# **EXAMPLE** Use the Discriminant

State the value of the discriminant. Then determine the number of real roots of the equation.
 a. 3x<sup>2</sup> + 10x = 12





# KEY CONCEPT

Using the Discriminant

Negative Discriminant: There are no real roots since no real number can be the square root of a negative number.

Zero Discriminant: There is a double root.

*Positive Discriminant:* There are two roots.

Homework Assignment

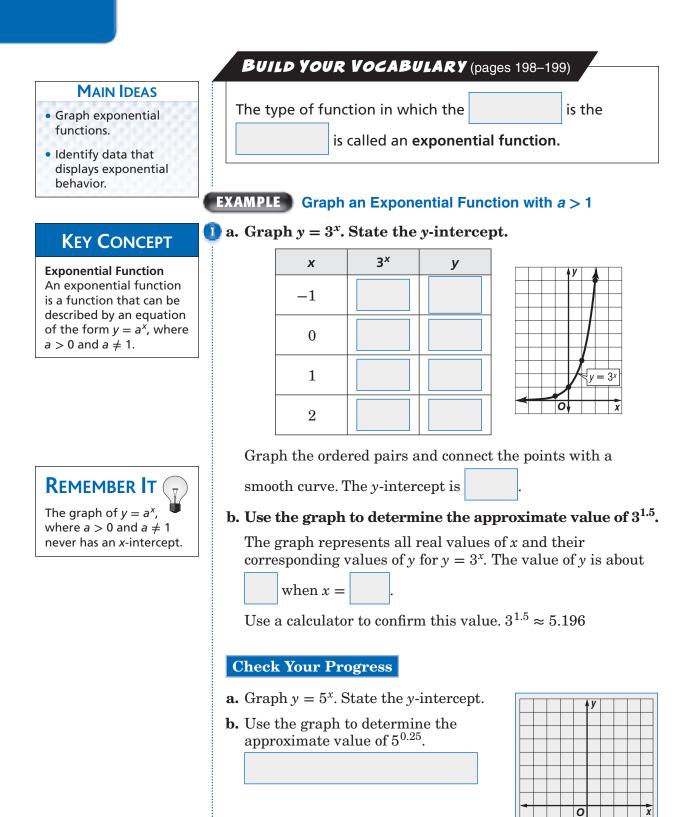
Page(s):

Exercises:

**b.**  $-5x^2 + 10x = -1$ 

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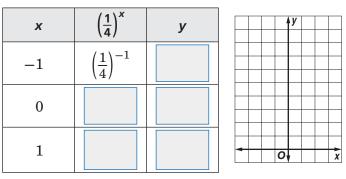
# **Exponential Functions**

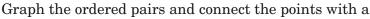


x

# **EXAMPLE** Graph Exponential Functions with 0 < a < 1

**2** a. Graph  $y = \left(\frac{1}{4}\right)^x$ . State the y-intercept.





smooth curve. The *y*-intercept is

b. Use the graph to determine the approximate value of  $\left(\frac{1}{4}\right)^{-1.5}$ .

when x =

The value of *y* is about

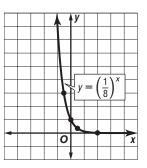
 $(1)^{-1.5}$ 

Use a calculator to confirm this value.  $\left(\frac{1}{4}\right)^{-1.5} = 8$ 

## **Check Your Progress**

**a.** Graph 
$$y = \left(\frac{1}{8}\right)^x$$
. State the y-intercept

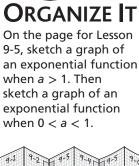
**b.** Use the graph to determine the approximate value of  $\left(\frac{1}{8}\right)^{-0.5}$ .



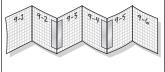
# EXAMPLE Use Exponential Functions to Solve Problems

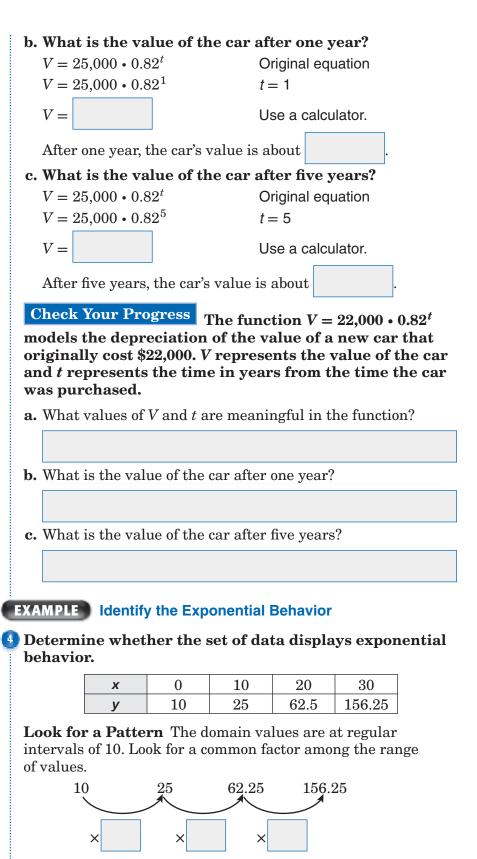
- The function  $V = 25,000 \cdot 0.82^t$  models the depreciation of the value of a new car that originally cost \$25,000. V represents the value of the car and t represents the time in years from the time the car was purchased.
  - a. What values of V and t are meaningful in the function?
    - Only the values of  $V \leq$  and  $t \leq$  are

meaningful in the context of the problem.



FOLDABLES





ASSIGNMENT Page(s):

HOMEWORK

Exercises:

Since the domain values are at regular intervals and the range values have a common factor, the data are probably

exponential. The equation for the data may involve



# **Growth and Decay**

### MAIN IDEAS

 Solve problems involving exponential growth.

 Solve problems involving exponential decay.

### **KEY CONCEPT**

**General Equation for Exponential Growth** The general equation for exponential growth is  $y = C(1 + r)^t$  where y represents the final amount, C represents the initial amount. r represents the rate of change expressed as a decimal, and t represents time.

## **EXAMPLE** Exponential Growth

- **D** POPULATION In 2005, the town of Flat Creek had a population of about 280,000 and a growth rate of 0.85% per year.
  - a. Write an equation to represent the population of Flat Creek since 2005.

The rate 0.85% can be written as 0.0085.

$y = C(1+r)^t$	General equation for exponential growth			
$y = 280,000(1 + 0.0085)^t$	C = 280,000 and $r = 0.0085$			
$y = 280,000(1.0085)^t$	Simplify.			
An equation to represent th	ne population of Flat Creek is			
	, where is the population			
and is the number of years since 2005.				
b. According to the equation population of Flat Creek	-			
In 2015, <i>t</i> will equal 2015 –	- 2005 or 10.			
$y = 280,000(1.0085)^t$	Equation for population of Flat Creek			
y = 280,000(1.0085)	<i>t</i> =			

 $\gamma \approx 304,731$ 

In 2015, there will be about

Use a calculator.

people in Flat Creek.

**Check Your Progress** In 2005, Scioto School District had a student population of about 4500 students, and a growth rate of about 0.15% per year.

- **a.** Write an equation to represent the student population of the Scioto School District since the year 2005.
- **b.** According to the equation, what will be the student population of the Scioto School District in the year 2011?

### **BUILD YOUR VOCABULARY** (pages 196–197)

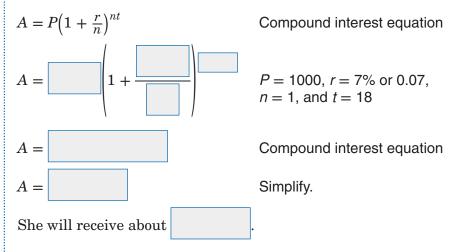
The equation  $A = P(1 + \frac{r}{n})^{nt}$  is used to find **compound** 

interest which is an application of

growth.

## EXAMPLE Compound Interest

**2** COLLEGE When Jing May was born, her grandparents invested \$1000 in a fixed rate savings account at a rate of 7% compounded annually. The money will go to Jing May when she turns 18 to help with her college expenses. What amount of money will Jing May receive from the investment?



**Check Your Progress** 

When Lucy was 10 years old, her father invested \$2500 in a fixed rate savings account at a rate of 8% compounded semiannually. When Lucy turns 18, the money will help to buy her a car. What amount of money will Lucy receive from the investment?

KEY CONCEPT	EXAMPLE Exponential Decay	
General Equation for Exponential Decay The general equation for exponential decay is $y = C(1 - r)^t$ where y represents the final amount, C represents the initial amount, r	<ul> <li>CHARITY During an economic organization found that its d 1.1% per year. Before the receivere \$390,000.</li> <li>a. Write an equation to repredonations since the beginn</li> </ul>	onations dropped by ession, its donations esent the charity's
represents the rate of decay expressed as a decimal, and t represents time.	$y = C(1 - r)^{t}$ $y = \boxed{\left(1 - \boxed{\right)}}$ $y = $	General equation for exponential decay C = 390,000 and r = 1.1% or 0.011 Simplify.
	b. Estimate the amount of the the start of the recession.	e donations 5 years after
	$y = 390,000(0.989)^{t}$ $y = 390,000(0.989)^{\Box}$ $y = $ The amount of donations show Check Your Progress A chat that the value of its clothing 2.5% per year. Before this dow organization received clothin a. Write an equation to represent clothing donations since the b	writable organization found donations dropped by wnturn in donations, the ng valued at \$24,000. At the value of the charity's
HOMEWORK ASSIGNMENT Page(s):	<b>b.</b> Estimate the value of the cloth the start of the downturn.	hing donations 3 years after
Exercises:		

9-6



# **BRINGING IT ALL TOGETHER**

# STUDY GUIDE

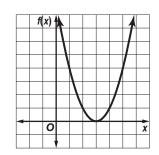
FOLDABLES	Vocabulary Puzzlemaker	Build your Vocabulary
Use your <b>Chapter 9 Foldable</b> to help you study for your chapter test.	To make a crossword puzzle, word search, or jumble puzzle of the vocabulary words in Chapter 9, go to: glencoe.com	You can use your completed <b>Vocabulary Builder</b> ( <i>pages 198–199</i> ) to help you solve the puzzle.



The graphs of two quadratic functions are shown below. Complete each statement about the graphs.

<b>1.</b> Each graph is a curve called a
2. The highest point of graph A is located at
<b>3.</b> The lowest point of graph B is located at
4. The maximum or minimum point of a parabola is called the
of the parabola.
9-2
Solving Quadratic Equations by Graphing
Refer to the graph shown at the right to answer the questions about the related equation $f(x) = x^2 - 6x + 9$ .
5. The related quadratic equation is

**6.** How many real number solutions are there?



7. Name one solution.



**8.** Draw a line under each quadratic equation that you could solve by taking the square root of each side.

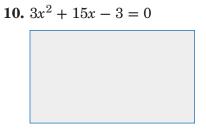
$x^2 + 6x + 9 = 100$	$x^2 - 14x + 40 = 25$	$x^2 - 16x + 64 = 26$
$x^2 - 20x + 80 = 16$	$x^2 + 10x + 36 = 49$	$x^2 - 12x + 36 = 6$

Solving Quadratic Equations by Using the Quadratic Formula

## Solve each equation by completing the square.

**9.**  $x^2 + 18x + 50 = 9$ 

9-4



**11.** What is the quadratic formula?

Solve each equation by using the quadratic formula. Round to the nearest tenth if necessary.

**12.**  $2a^2 - 3a = -1$ 

**13.**  $3w^2 - 1 = 8w$ 

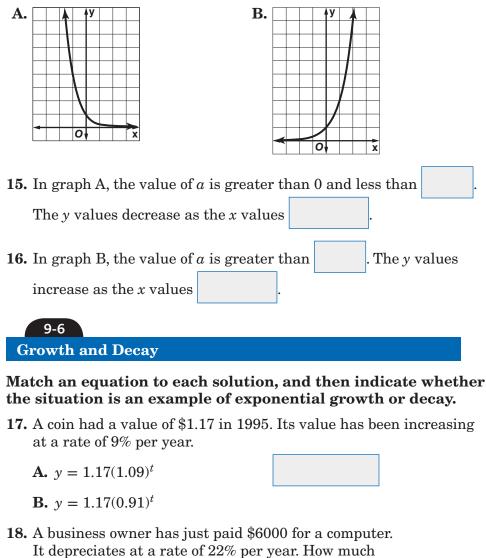


**14.** You can use the discriminant to determine the number of real roots for a quadratic equation. What is the discriminant?



9-5 Exponential Functions

The graphs of two exponential functions of the form  $y = a^x$  are shown below.



will it be worth in 5 years?

**A.**  $A = 6000(1.22)^5$ 

**B.**  $A = 6000(0.78)^5$ 



# ARE YOU READY FOR THE CHAPTER TEST?



Visit **glencoe.com** to access your textbook, more examples, self-check quizzes, and practice tests to help you study the concepts in Chapter 9.

Check the one that applies. Suggestions to help you study are given with each item.
-------------------------------------------------------------------------------------

I completed the review of all or most lessons without using my notes or asking for help.

- You are probably ready for the Chapter Test.
- You may want take the Chapter 9 Practice Test on page 521 of your textbook as a final check.

I used my Foldable or Study Notebook to complete the review of all or most lessons.

- You should complete the Chapter 9 Study Guide and Review on pages 517–520 of your textbook.
- If you are unsure of any concepts or skills, refer back to the specific lesson(s).
- You may also want to take the Chapter 9 Practice Test on page 521.

I asked for help from someone else to complete the review of all or most lessons.

- You should review the examples and concepts in your Study Notebook and Chapter 9 Foldable.
- Then complete the Chapter 9 Study Guide and Review on pages 517–520 of your textbook.
- If you are unsure of any concepts or skills, refer back to the specific lesson(s).
- You may also want to take the Chapter 9 Practice Test on page 521.

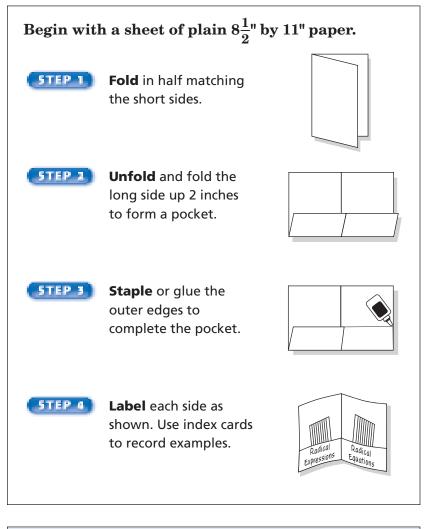
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Teacher	Signature



# **Radical Expressions and Triangles**



Use the instructions below to make a Foldable to help you organize your notes as you study the chapter. You will see Foldable reminders in the margin this Interactive Study Notebook to help you in taking notes.



**NOTE-TAKING TIP:** Remember to study your notes daily. Reviewing small amounts at a time will help you retain the information.

Chapter 10



# BUILD YOUR VOCABULARY

This is an alphabetical list of new vocabulary terms you will learn in Chapter 10. As you complete the study notes for the chapter, you will see Build Your Vocabulary reminders to complete each term's definition or description on these pages. Remember to add the textbook page number in the second column for reference when you study.

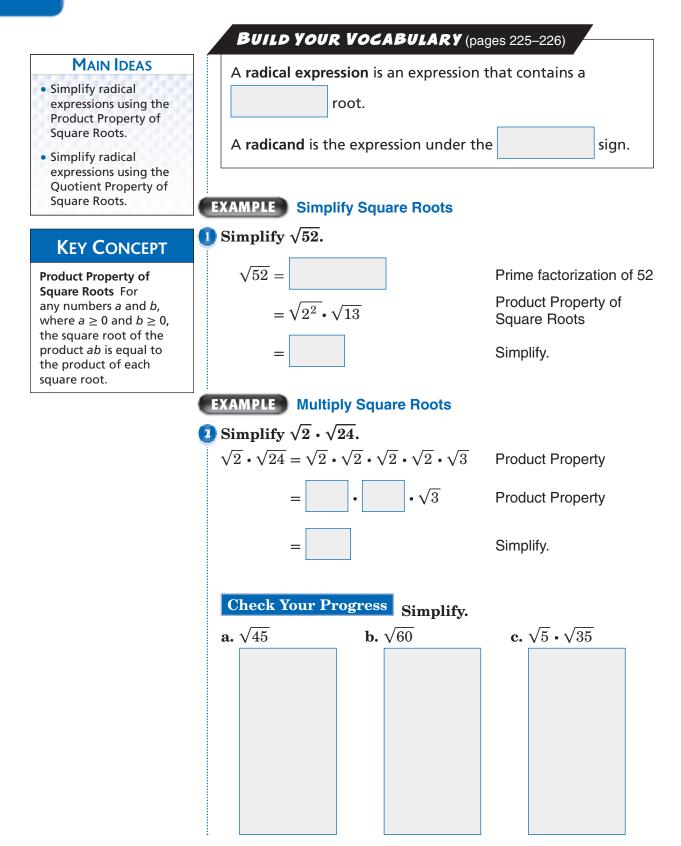
Vocabulary Term	Found on Page	Definition	Description or Example
conjugate [KAHN·jih·guht]			
converse			
Distance Formula			
extraneous solution [ehk·STRAY·nee·uhs]			
hypotenuse [hy·PAH·tn·OOS]			
legs			

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(continued on the next page)

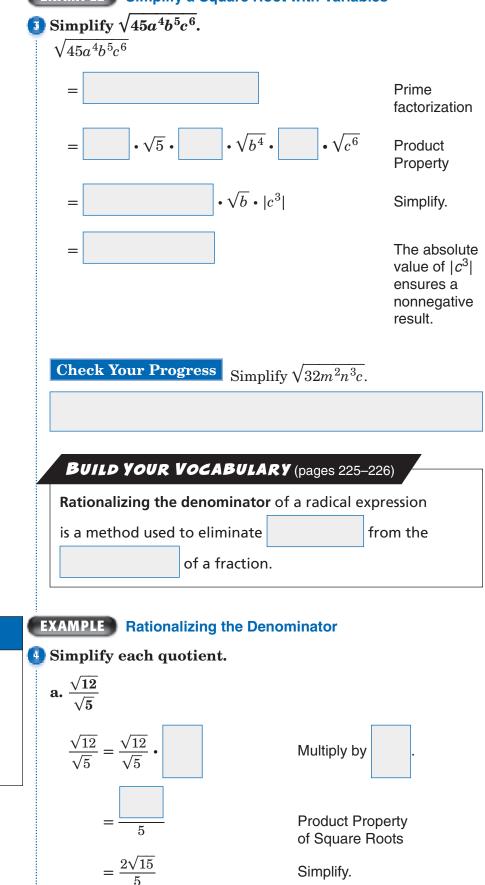
Vocabulary Term	Found on Page	Definition	Description or Example
<u>Pythagorean</u> triple			
puh·THA·guh·REE·uhn			
radical equation			
radical expression			
<u>radicand</u> RA·duh·KAND			
rationalizing the denominator			
similar triangles			

# **Simplifying Radical Expressions**









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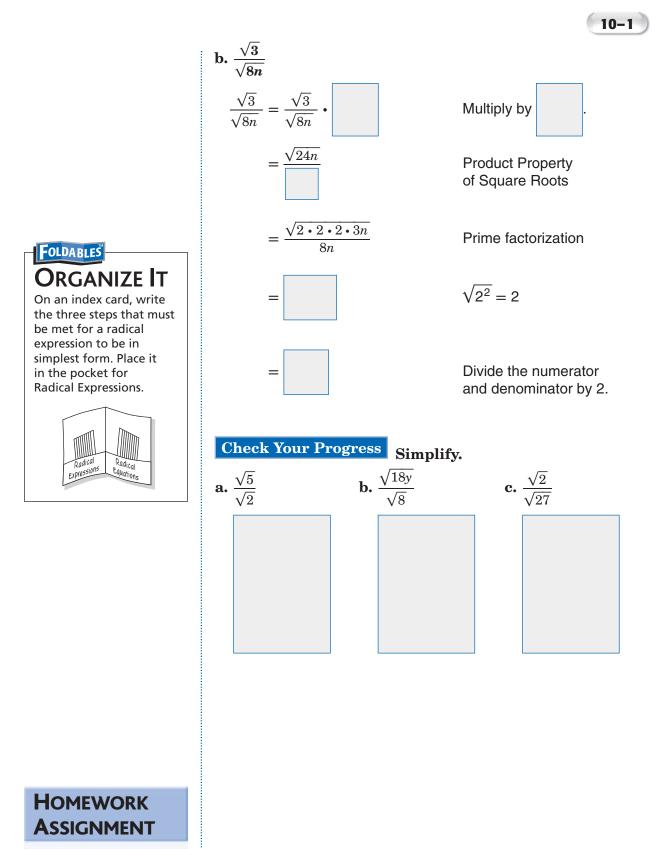
**KEY CONCEPT** 

Quotient Property of Square Roots For

any numbers *a* and *b*, where  $a \ge 0$  and b > 0, the square root of the quotient  $\frac{a}{b}$  is equal to

the quotient of each

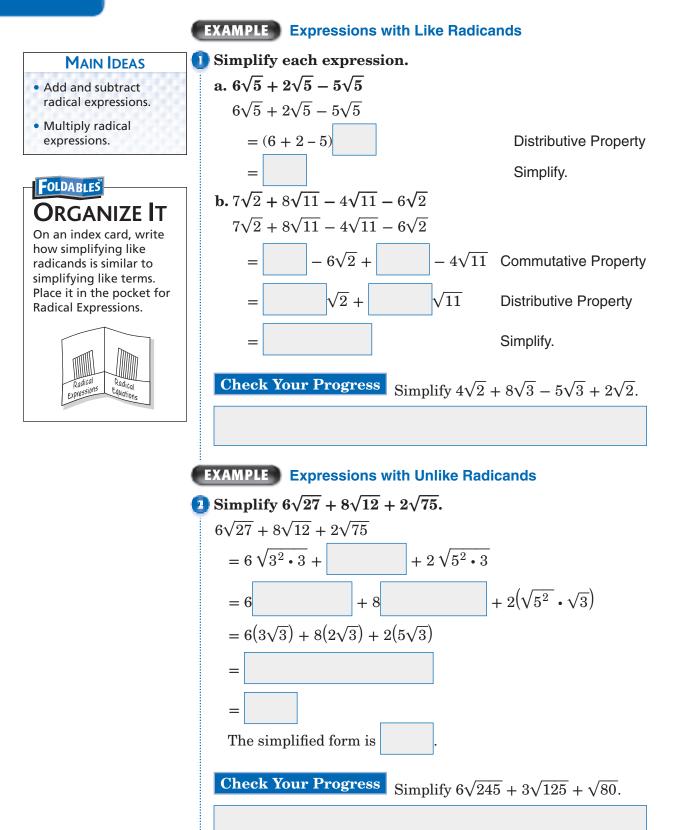
square root.



Page(s):

Exercises:

**Operations with Radical Expressions** 



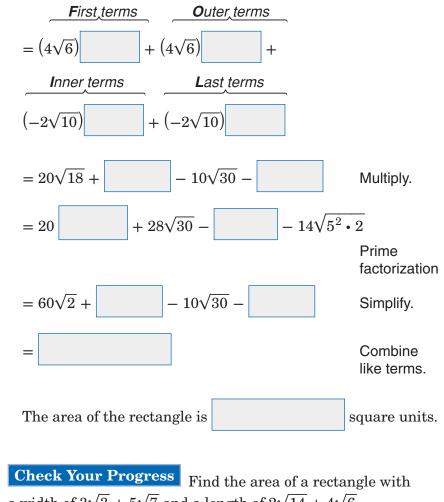
10-2

# **EXAMPLE** Multiply Radical Expressions

## **3** GEOMETRY Find the area of a rectangle in simplest form with a width of $4\sqrt{6} - 2\sqrt{10}$ and a length of $5\sqrt{3} + 7\sqrt{5}$ .

To find the area of the rectangle multiply the measures of the length and width.

 $(4\sqrt{6} - 2\sqrt{10})(5\sqrt{3} + 7\sqrt{5})$ 



a width of  $3\sqrt{3} + 5\sqrt{7}$  and a length of  $2\sqrt{14} + 4\sqrt{6}$ .

HOMEWORK ASSIGNMENT Page(s): Exercises:



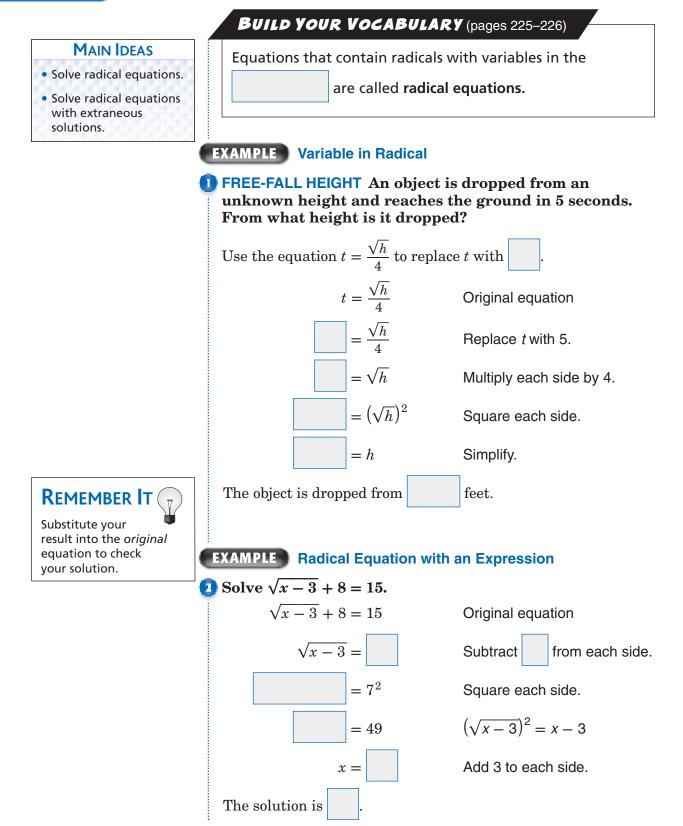
**REVIEW IT** 

Give an example of two

binomials. Then explain

how you multiply them using FOIL method. (Lesson 7-6)

# **10–3** Radical Equations





	Check Your Progress	
<b>REVIEW IT</b> Explain the Zero Product Property in your own words. ( <i>Lesson 8–2</i> )	<b>a.</b> Refer to Example 1. If an unknown in 7 seconds, from what height is it	
	<b>b.</b> Solve $\sqrt{x+4} + 6 = 14$ .	
	Build Your Vocabulary (pa	ages 225–226)
	An <b>extraneous solution</b> is a solution	
	equation that is a solution of t	he equation.
•	EXAMPLE Variable on Each Side	
	Solve $\sqrt{2-y} = y$ .	
	$\sqrt{2-y} = y$	Original equation
	$\left(\sqrt{2-y}\right)^2 = y^2$	
		Simplify.
	$0 = y^2 + y - 2$	Subtract and add
		to each side.
	0 =	Factor.
	= 0  or  = 0	Zero Product Property
	y = $y =$	Solve.
	<b>Check</b> $\sqrt{2-y} = y$	$\sqrt{2-y} = y$
	$\frac{\sqrt{2 - (-2)}}{\sqrt{4}} \stackrel{?}{=} -2$	$\frac{\sqrt{2-1} \stackrel{?}{=} 1}{\sqrt{1} \stackrel{?}{=} 1}$
	$\sqrt{4} = -2$ $2 \neq -2 \times$	$\begin{array}{c} \sqrt{1} = 1 \\ 1 = 1 \end{array} \checkmark$
HOMEWORK Assignment	Since does not satisfy the origina	al equation, is
Page(s):	the only solution.	
Exercises:	Check Your Progress Solve each	
		-
	<b>a.</b> $\sqrt{x+3} - 1 = 8$ <b>b.</b> $y =$	$\sqrt{2y+3}$

Glencoe Algebra 1 233



# The Pythagorean Theorem

### MAIN IDEAS

- Solve problems by using the Pythagorean Theorem.
- Determine whether a triangle is a right triangle.

# **KEY CONCEPT**

#### The Pythagorean

**Theorem** If *a* and *b* are the lengths of the legs of a right triangle and *c* is the length of the hypotenuse, then the square of the length of the hypotenuse is equal to the sum of the squares of the lengths of the legs.

# BUILD YOUR VOCABULARY (pages 225-226)

In a right triangle, the side opposite the

angle is called the hypotenuse. The other two

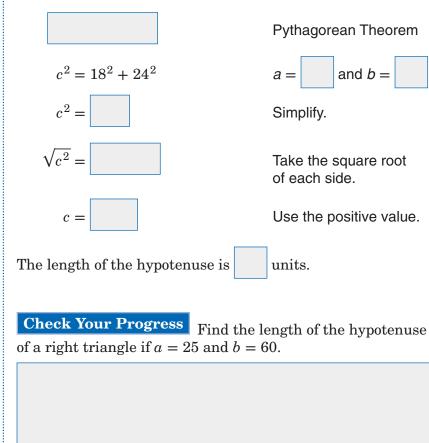
are called the **legs** of the triangle.

Whole numbers that satisfy the

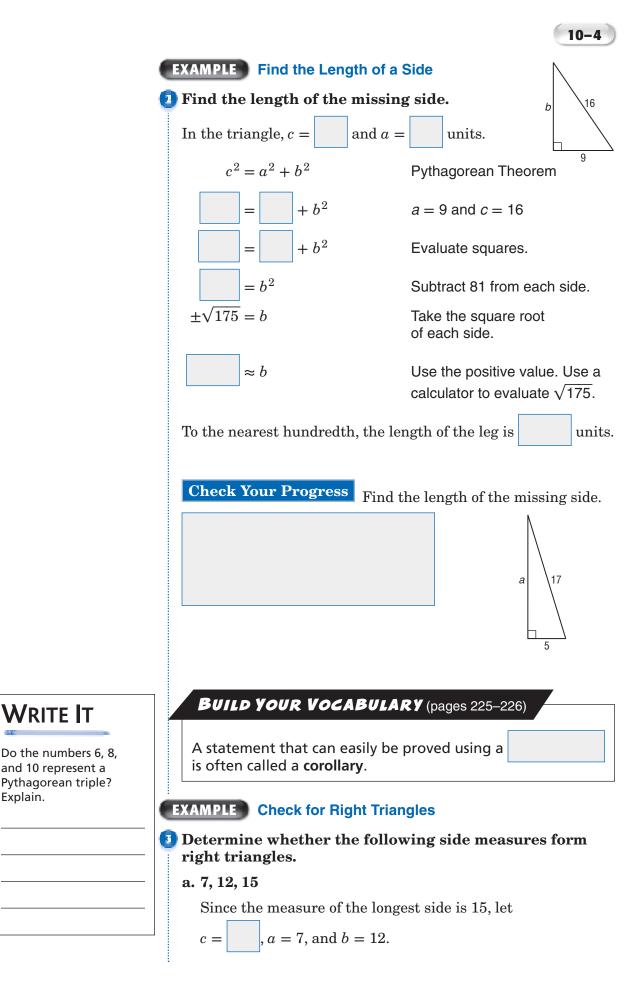
are called Pythagorean triples.

# EXAMPLE Find the Length of the Hypotenuse

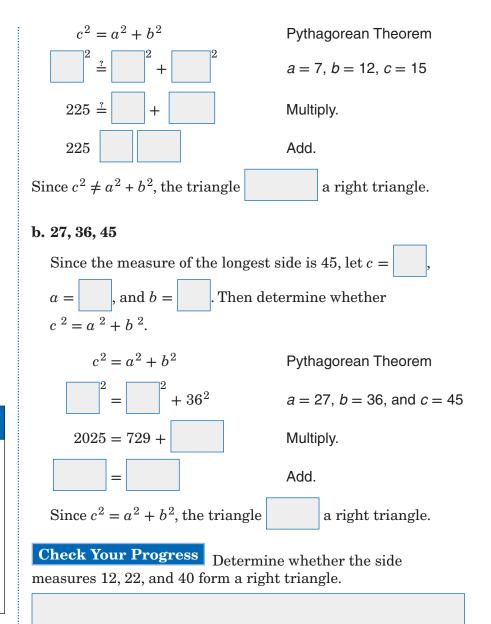
# **1** Find the length of the hypotenuse of a right triangle if a = 18 and b = 24.



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Explain.



**Corollary to the Pythagorean Theorem** If *a* and *b* are measures of the shorter sides of a triangle, *c* is the measure of the longest side, and  $c^2 = a^2 + b^2$ , then the triangle is a right triangle. If  $c^2 \neq a^2 + b^2$ , then the triangle is not a right triangle.

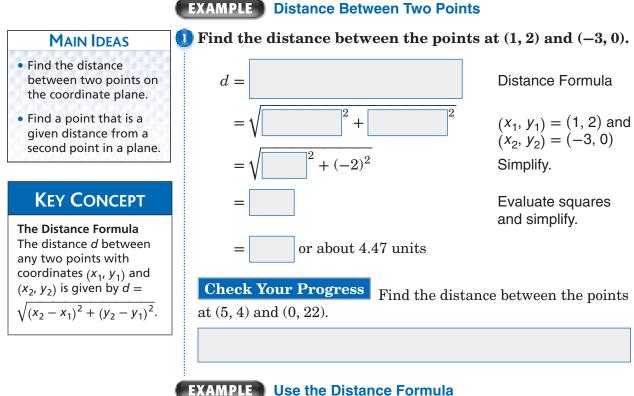
**KEY CONCEPT** 

HOMEWORK Assignment

Page(s): Exercises:

: es:

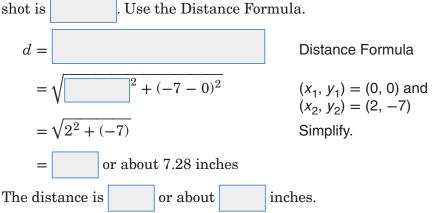
#### **The Distance Formula** 10-5



### EXAMPLE Use the Distance Formula

BIATHLON Julianne is sighting her rifle for an upcoming biathlon competition. Her first shot is 2 inches to the right and 7 inches below the bull's-eye. What is the distance between the bull's-eye and where her first shot hit the target?

If the bull's-eye is at (0, 0), then the location of the first





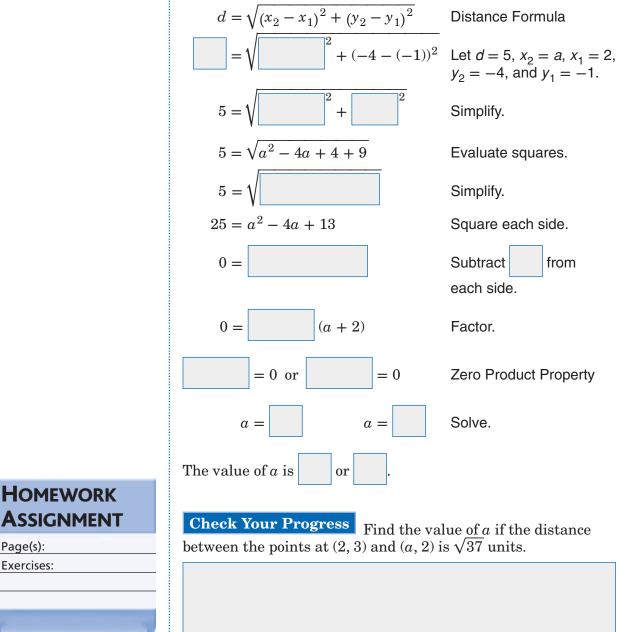


You can choose either point to be  $(x_1, y_1)$  when using the Distance Formula.

**Check Your Progress** Marcy is pitching a horseshoe in her local park. Her first pitch is 9 inches to the left and 3 inches below the pin. What is the distance between the horseshoe and the pin?

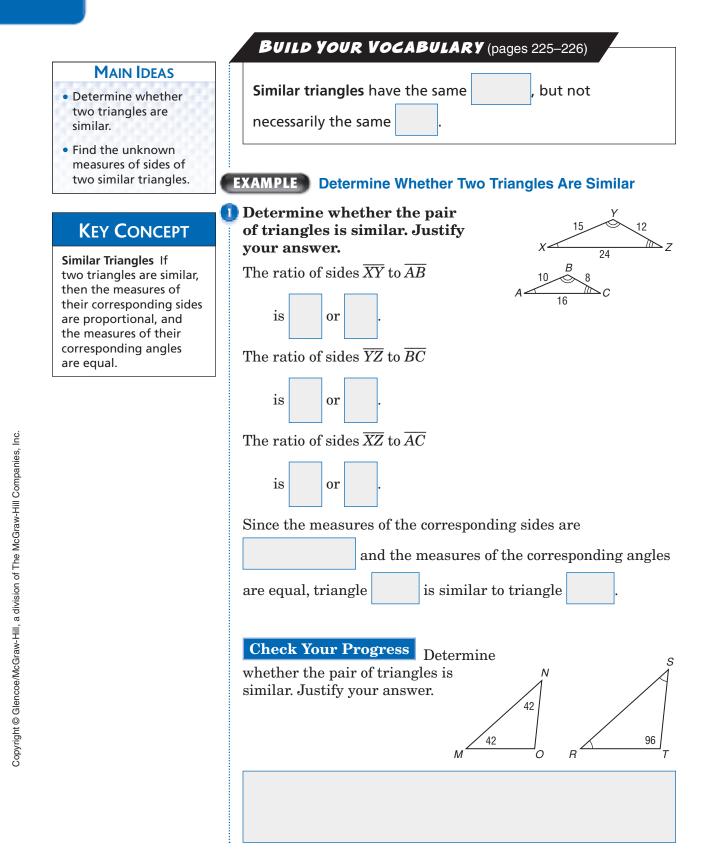
## **EXAMPLE** Find a Missing Coordinate

Find the value of a if the distance between the points at (2, -1) and (a, -4) is 5 units.



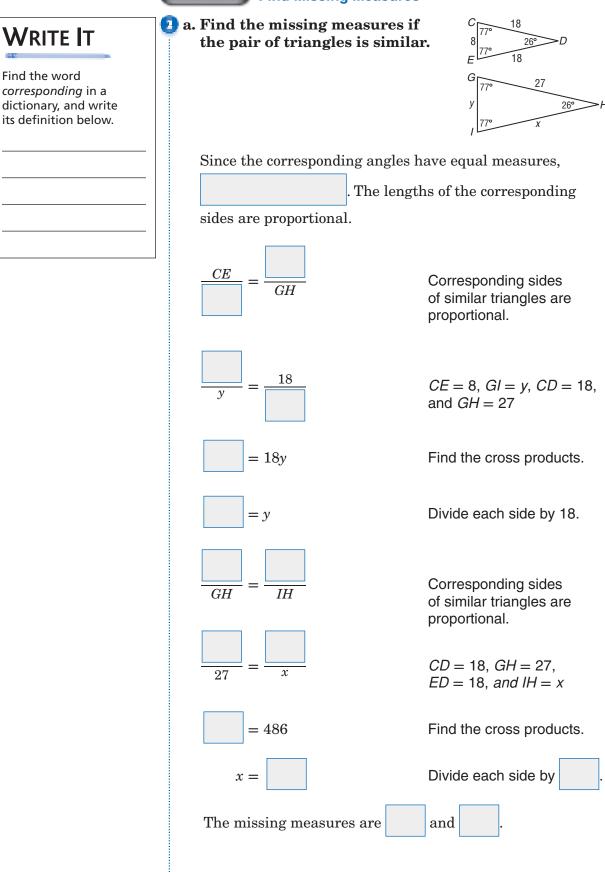
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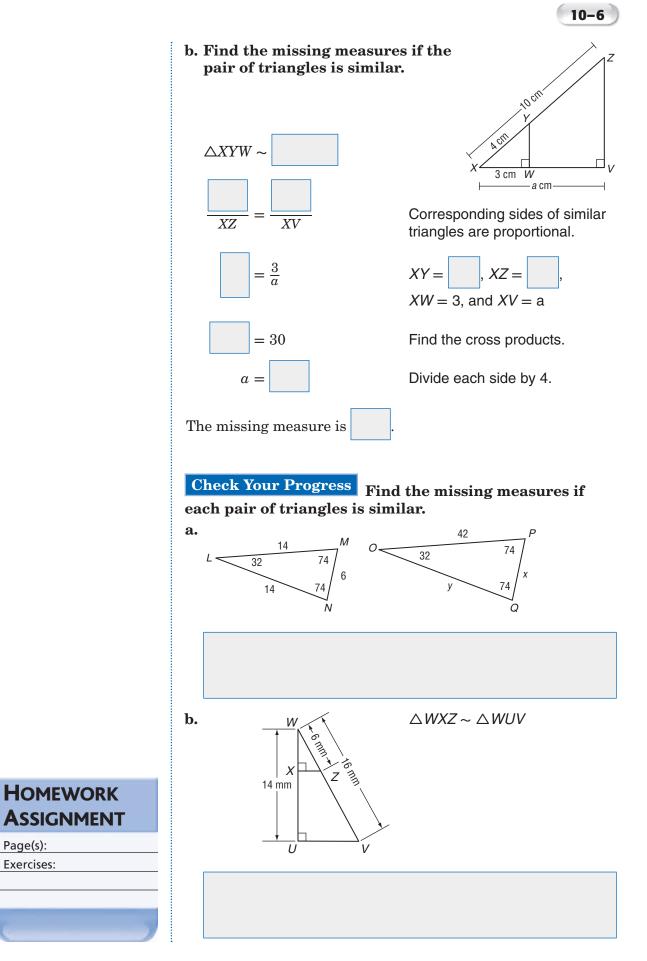
# **10–6** Similar Triangles





## EXAMPLE Find Missing Measures





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Page(s):

Exercises:



# **BRINGING IT ALL TOGETHER**

# STUDY GUIDE

FOLDABLES	Vocabulary Puzzlemaker	Build your Vocabulary
Use your <b>Chapter 10 Foldable</b> to help you study for your chapter test.	To make a crossword puzzle, word search, or jumble puzzle of the vocabulary words in Chapter 10, go to: glencoe.com	You can use your completed <b>Vocabulary Builder</b> ( <i>pages 225–226</i> ) to help you solve the puzzle.

### 10-1 Simplifying Radical Expressions

### Simplify.

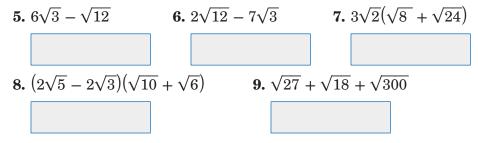
- **1.**  $\sqrt{28x^2y^4}$  **2.**  $\sqrt{\frac{5}{32}}$  **3.**  $\frac{8}{3+\sqrt{3}}$
- **4.** What should you remember to check for when you want to determine if a radical expression is in simplest form?

Check radicands for		and	,
and check fractions for	in	n the	

## 10-2

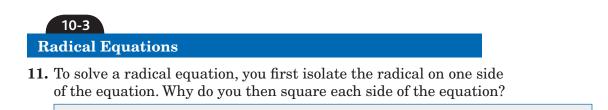
### **Operations with Radical Expressions**

## Simplify each expression.

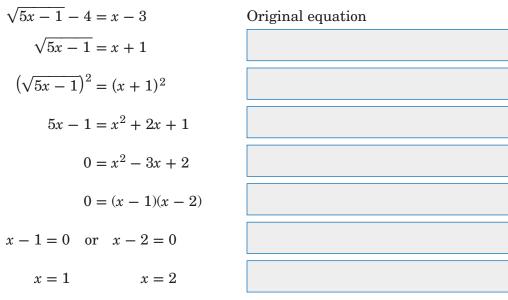


10. Below the words First terms, Outer terms, Inner terms, and Last terms, write the products you would use to simplify the expression  $(2\sqrt{15} + 3\sqrt{15})(6\sqrt{3} - 5\sqrt{2})$ .

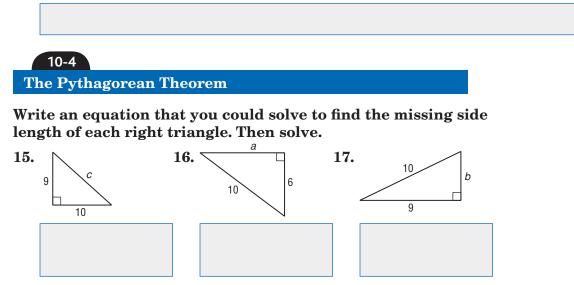
$\mathbf{F}$ irst terms		Outer terms		Inner terms		Last terms
	+		+		+	



**12.** Provide the reason for each step in the solution of the given radical equation.



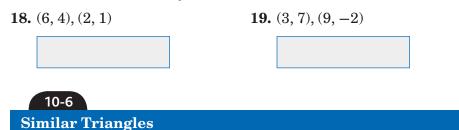
- **13.** To be sure that 1 and 2 are the correct solutions, into which equation should you substitute to check?
- 14. A computer screen measures 12 inches high and 17 inches wide. What is the length of the screen's diagonal? Round your answer to the nearest whole number.



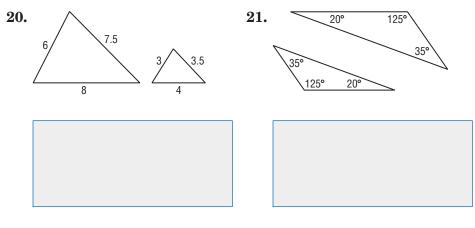




Find the distance between each pair of points whose coordinates are given. Express answers in simplest radical form and as decimal approximations rounded to the nearest hundredth if necessary.



Determine whether each pair of triangles is similar. Explain how you would know that your answer is correct.





## ARE YOU READY FOR THE CHAPTER TEST?



Visit glencoe.com to access your textbook, more examples, self-check quizzes, and practice tests to help you study the concepts in Chapter 10.

Check the one that applies. Suggestions to help you study	y are
given with each item.	

I completed the review of all or most lessons without using my notes or asking for help.

- You are probably ready for the Chapter Test.
- You may want to take the Chapter 10 Practice Test on page 571 of your textbook as a final check.

I used my Foldable or Study Notebook to complete the review of all or most lessons.

- You should complete the Chapter 10 Study Guide and Review on pages 567–570 of your textbook.
- If you are unsure of any concepts or skills, refer back to the specific lesson(s).
- You may also want to take the Chapter 10 Practice Test on page 571.

I asked for help from someone else to complete the review of all or most lessons.

- You should review the examples and concepts in your Study Notebook and Chapter 10 Foldable.
- Then complete the Chapter 10 Study Guide and Review on pages 567–570 of your textbook.
- If you are unsure of any concepts or skills, refer back to the specific lesson(s).
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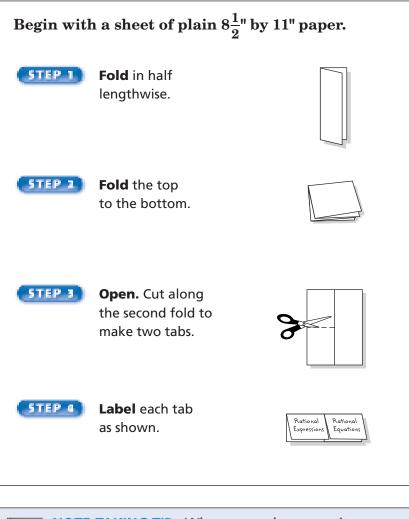
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# **Rational Expressions and Equations**



Use the instructions below to make a Foldable to help you organize your notes as you study the chapter. You will see Foldable reminders in the margin of this Interactive Study Notebook to help you in taking notes.



**NOTE-TAKING TIP:** When you take notes, it may be helpful to sit as close as possible to the front of the class. There are fewer distractions and it is easier to hear.



#### BUILD YOUR VOCABULARY

This is an alphabetical list of new vocabulary terms you will learn in Chapter 11. As you complete the study notes for the chapter, you will see Build Your Vocabulary reminders to complete each term's definition or description on these pages. Remember to add the textbook page number in the second column for reference when you study.

Vocabulary Term	Found on Page	Definition	Description or Example
complex fraction			
excluded values			
extraneous solutions [ehk·STRAY·nee·uhs]			
inverse variation [ihn·VUHRS]			
least common multiple			
least common denominator			

(continued on the next page)

Chapter 11

Vocabulary Term	Found on Page	Definition	Description or Example
mixed expression			
product rule			
rate problems			
rational equations			
rational expression			
work problems			

## 11–1 Inverse Variation

#### **MAIN IDEAS**

- Graph inverse variations.
- Solve problems involving inverse variations.

#### **KEY CONCEPT**

**Inverse Variation** y varies inversely as x if there is some nonzero constant k such that xy = k.

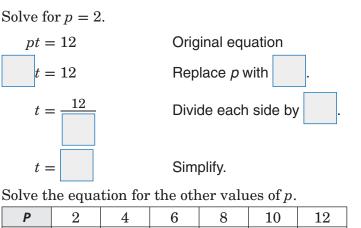
#### **BUILD YOUR VOCABULARY** (pages 247-248)

When the product of two values remains relationship forms an inverse variation.

the

#### **EXAMPLE** Graph an Inverse Variation

**MANUFACTURING** The time *t* in hours that it takes to build a particular model of computer varies inversely with the number of people *p* working on the computer. The equation pt = 12 can be used to represent the people building a computer. Draw a graph of the relation.

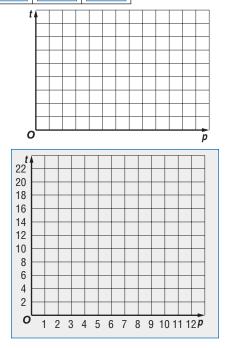


Graph the ordered pairs. As the number of people *p* increases, the time *t* it takes to build a computer decreases.

t

#### **Check Your Progress**

The time *t* in hours that it takes to prepare packages for delivery varies inversely with the number of people *p* that are preparing them. The equation pt = 36 can be used to represent the people preparing the packages. Draw a graph of the relation.



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#### BUILD YOUR VOCABULARY (pages 247-248)

The equation  $x_1y_1 = x_2y_2$  is called the **product rule** for

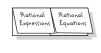
**2** If y varies inversely as x and y = 5 when x = 12, find x

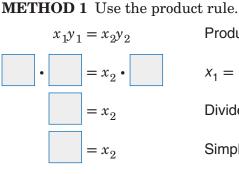
variations.

Let  $x_1 = 12$ ,  $y_1 = 5$ , and  $y_2 = 15$ . Solve for  $x_2$ .

#### Foldables ORGANIZE IT

Under the tab for Rational Expressions, write the general form for inverse variation. Then give an example of an inverse variation equation.





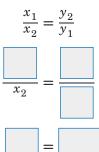
EXAMPLE Solve for x

when y = 15.

 $x_1 = 12, y_1 = 5, y_2 = 15$ Divide each side by Simplify.

Product rule for inverse variations

**METHOD 2** Use a proportion.



 $= x_2$ 

Proportion rule for inverse variations

 $x_1 = 12, y_1 = 5, y_2 = 15$ 

Cross multiply.

Divide each side by 15.

Both methods show that x =

```
when y =
```

#### **Check Your Progress**

- **a.** If *y* varies inversely as *x* and y = 6 when x = 40, find *x* when y = 30.
- **b.** If *y* varies inversely as *x* and y = -5 when x = 15, find *y* when x = 3.

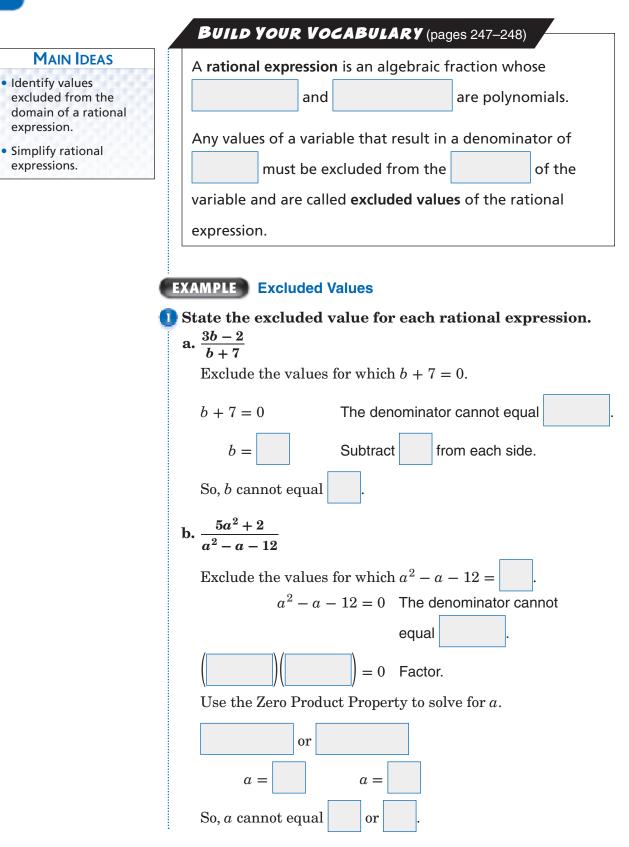
HOMEWORK ASSIGNMENT

#### Page(s):

Exercises:

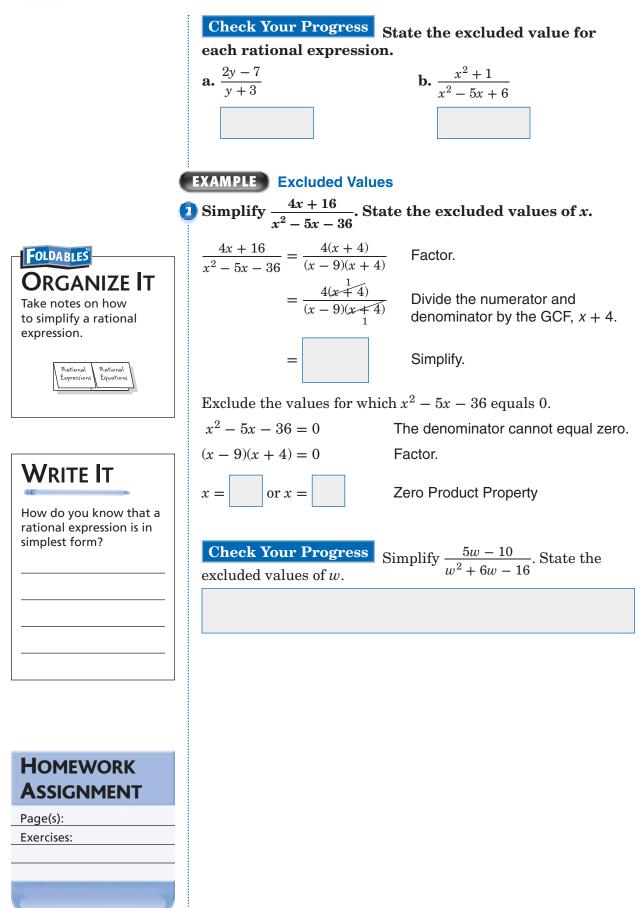
## 11-2

# **Rational Expressions**



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**11–3** Multiplying Rational Expressions

#### MAIN IDEAS

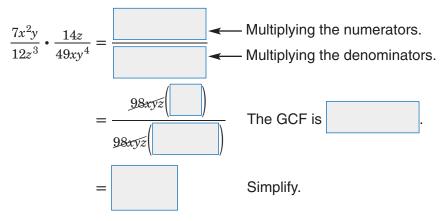
- Multiply rational expressions.
- Use dimensional analysis with
- multiplication.

EXAMPLE Expressions Involving Monomials

# $\bigcirc \text{ Find } \frac{7x^2y}{12z^3} \cdot \frac{14z}{49xy^4}.$

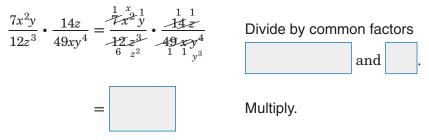
#### METHOD 1

Divide by the greatest common factor after multiplying.



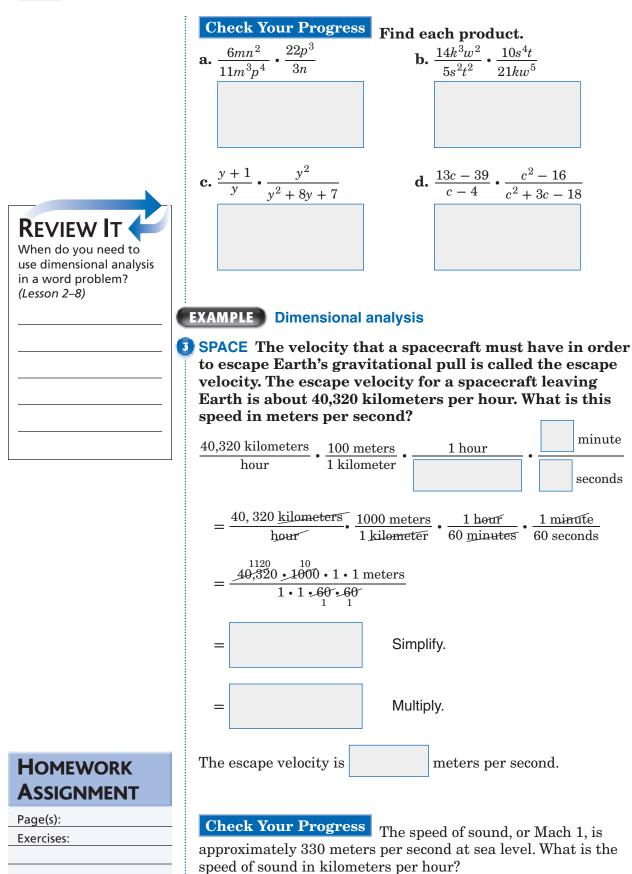
#### **METHOD 2**

Divide the common factors before multiplying.

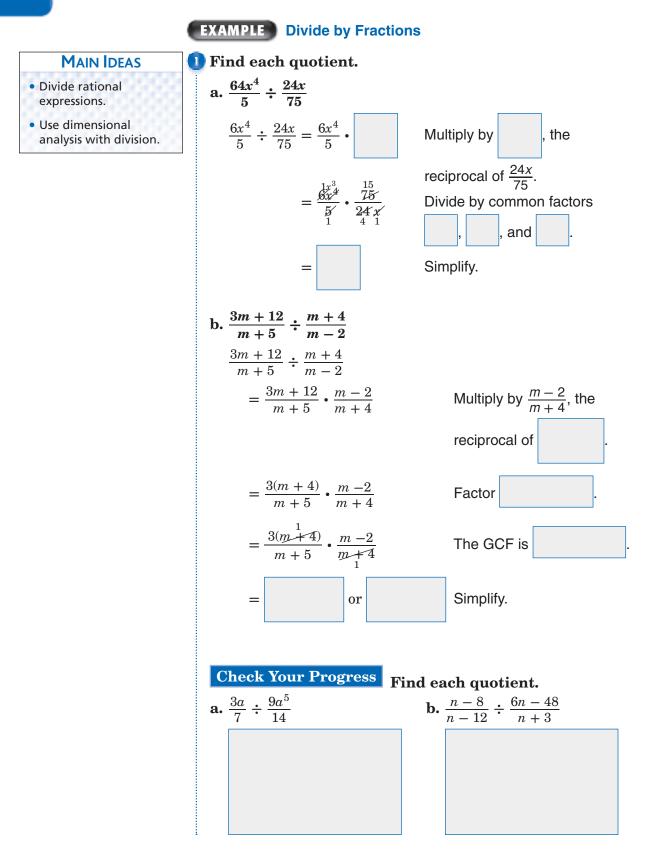


#### EXAMPLE Expressions Involving Polynomials

2 Find  $\frac{b+3}{4b-12} \cdot \frac{b^2-4b+3}{b^2-7b-30}$ .  $\frac{b+3}{4b-12} \cdot \frac{b^2-4b+3}{b^2-7b-30} = \frac{b+3}{4(b-3)} \cdot \frac{(b-3)(b-1)}{(b-10)(b+3)}$  Factor.  $= \frac{(b+3)(b-3)(b-1)}{4(b-3)(b-10)(b+3)}$  The GCF is (b+3)(b-3).  $= \frac{b-1}{4(b-10)}$  Multiply. = Simplify.



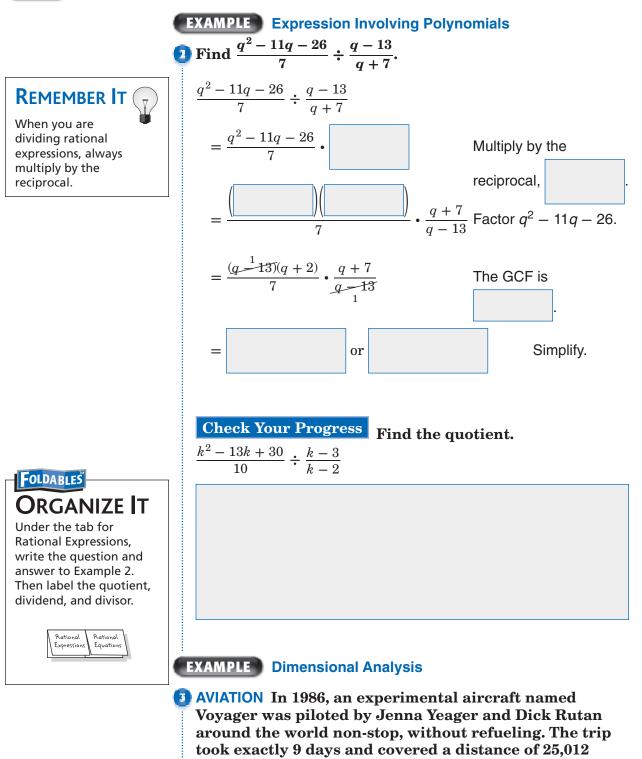
**Dividing Rational Expressions** 



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11-4

11-4

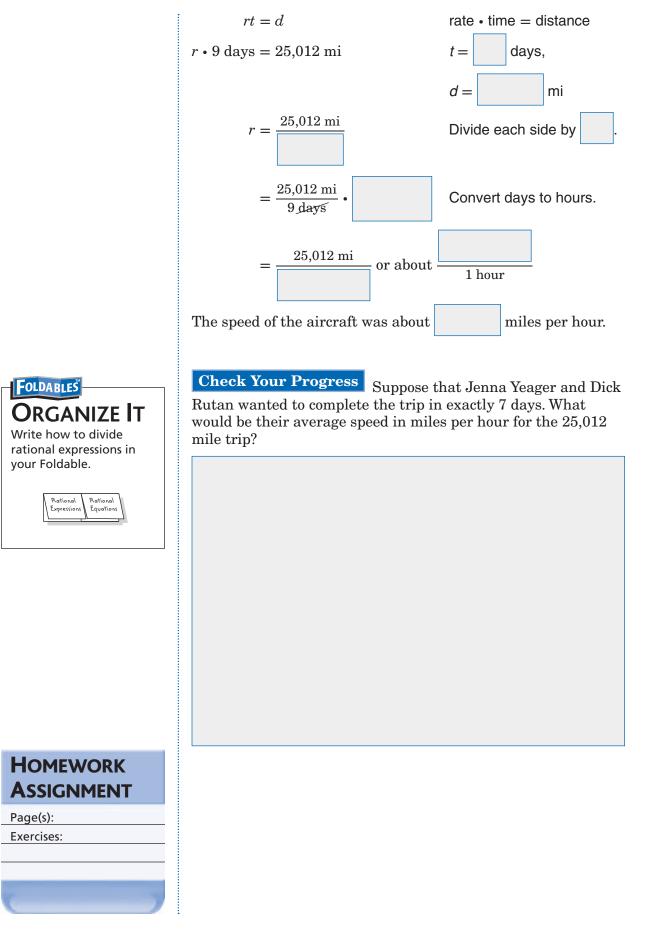


Use the formula for rate, time, and distance.

hour? Round to the nearest miles per hour.

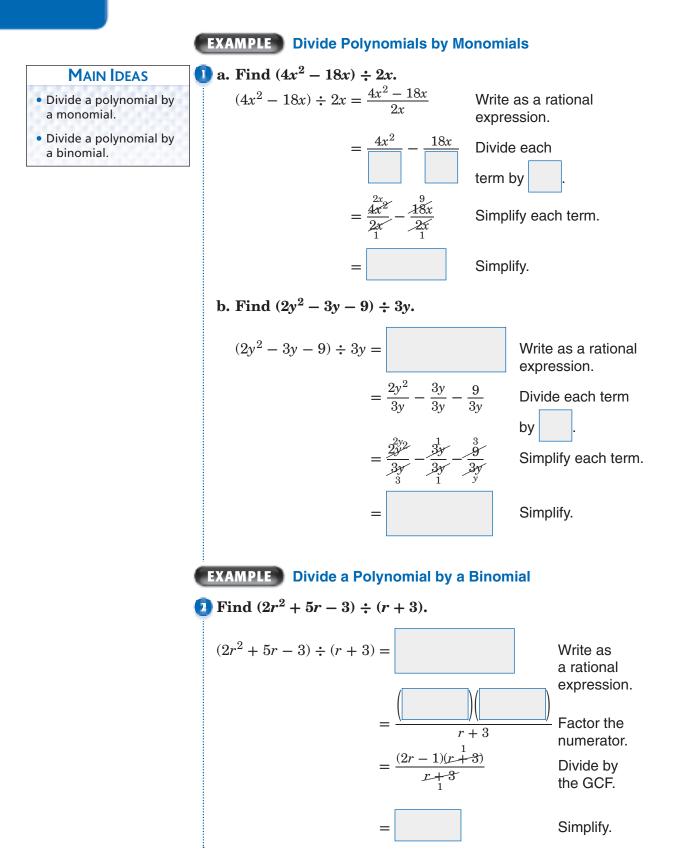
miles. What was the speed of the aircraft in miles per

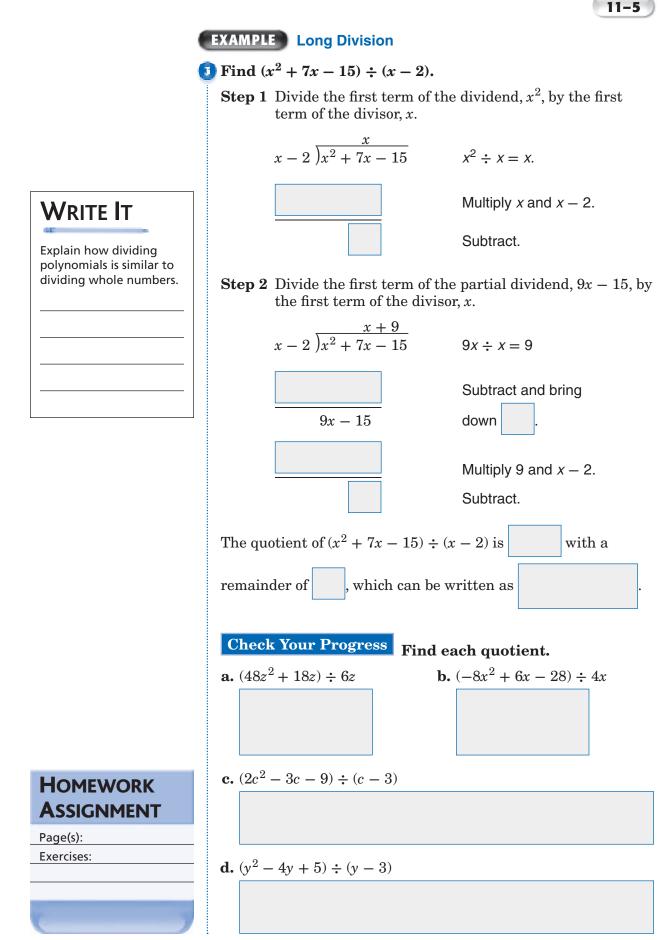




Glencoe Algebra 1 257

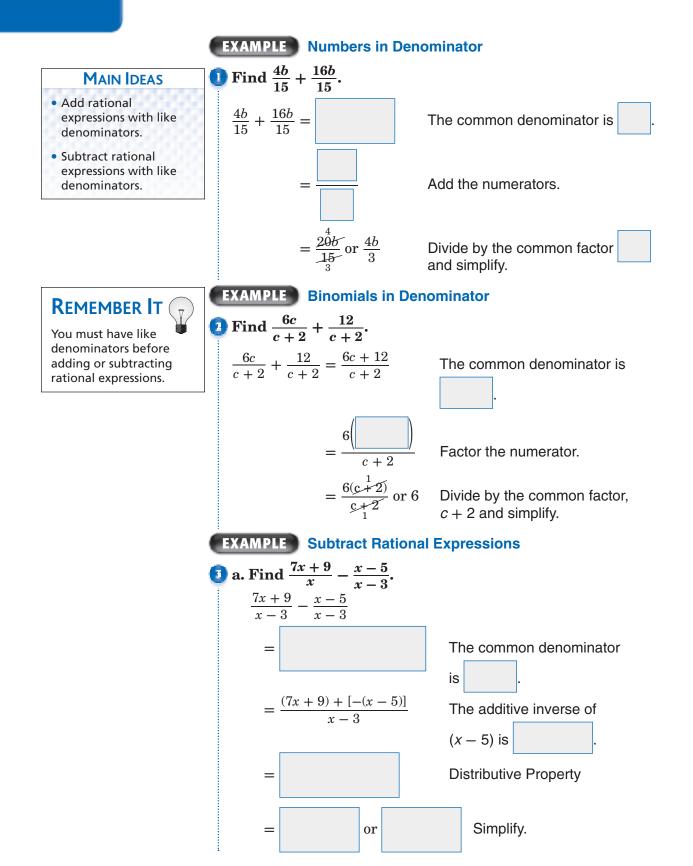
## **11–5** Dividing Polynomials

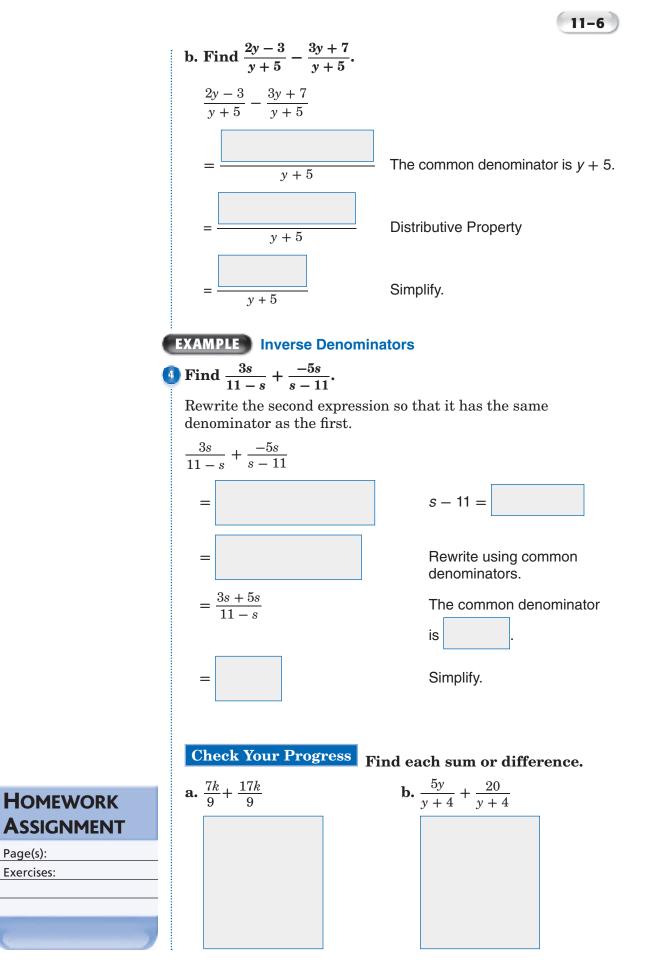




Glencoe Algebra 1 259

**11–6** Rational Expressions with Like Denominators





## 11-7

# **Rational Expressions with Unlike Denominators**

#### MAIN IDEAS

- Add rational expressions with unlike denominators.
- Subtract rational expressions with unlike denominators.

#### **KEY CONCEPT**

Add Rational Expressions Use the following steps to add rational expressions with unlike denominators.

Step 1 Find the LCD.

**Step 2** Change each rational expression into an equivalent expression with the LCD as the denominator.

**Step 3** Add just as with rational expressions with like denominators.

Step 4 Simplify if necessary.

#### BUILD YOUR VOCABULARY (pages 247-248)

The least common mult	i <b>ple</b> is the	number that is	
a multiple of two or more numbers.			
The least common multiple of the of			
two or more is known as the <b>least common</b>			
denominator.			

#### EXAMPLE LCM of Polynomials

#### 🕕 Find the LCM of each pair of polynomials.

#### a. $12b^4c^5$ and $32bc^2$

Find the prime factors of each coefficient and variable expression.

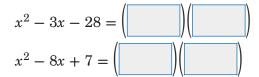
$12b^4c^5 =$	
$32bc^{2} =$	

Use each prime factor the greatest number of times it appears in any of the factorizations.

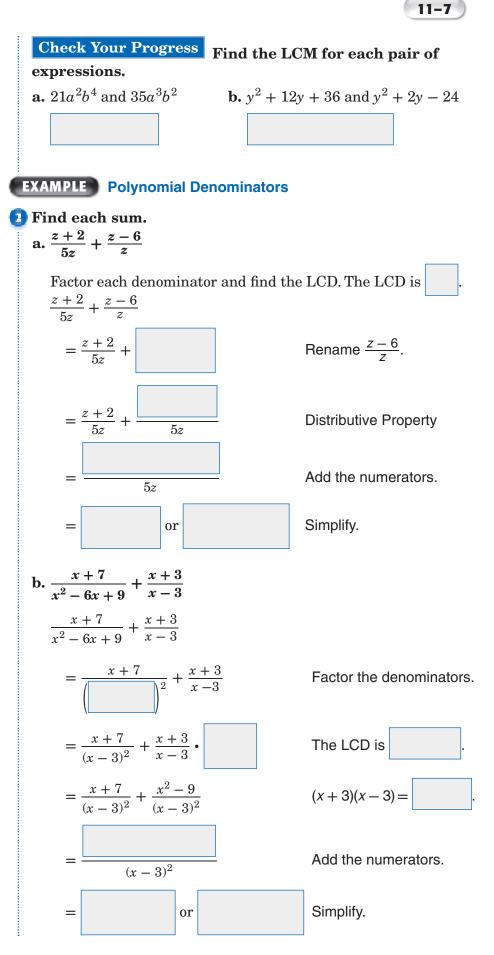
LCM =

b.  $x^2 - 3x - 28$  and  $x^2 - 8x + 7$ 

Express each polynomial in factored form.

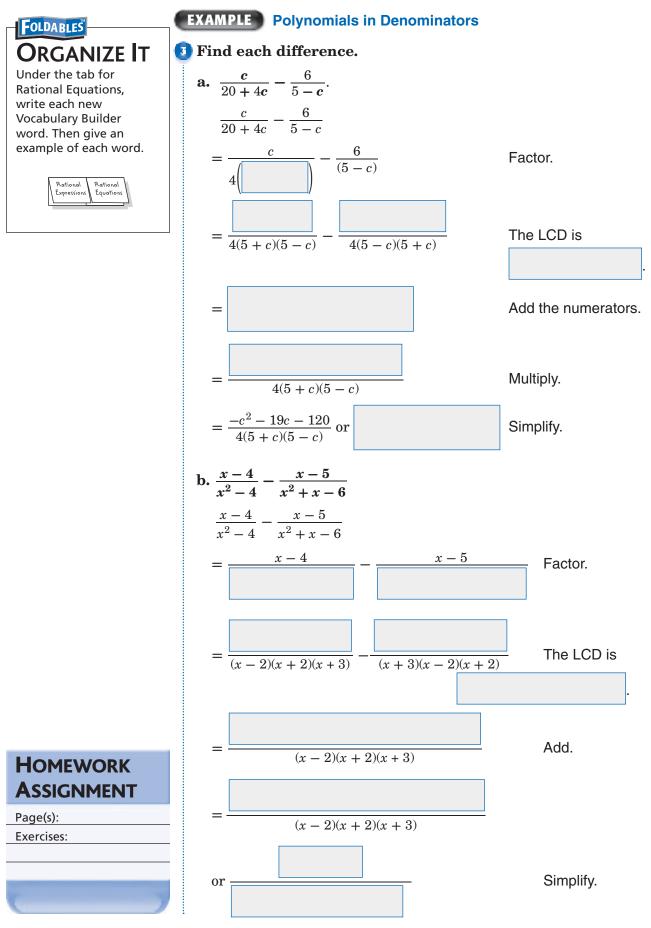


Use each factor the greatest number of times it appears.



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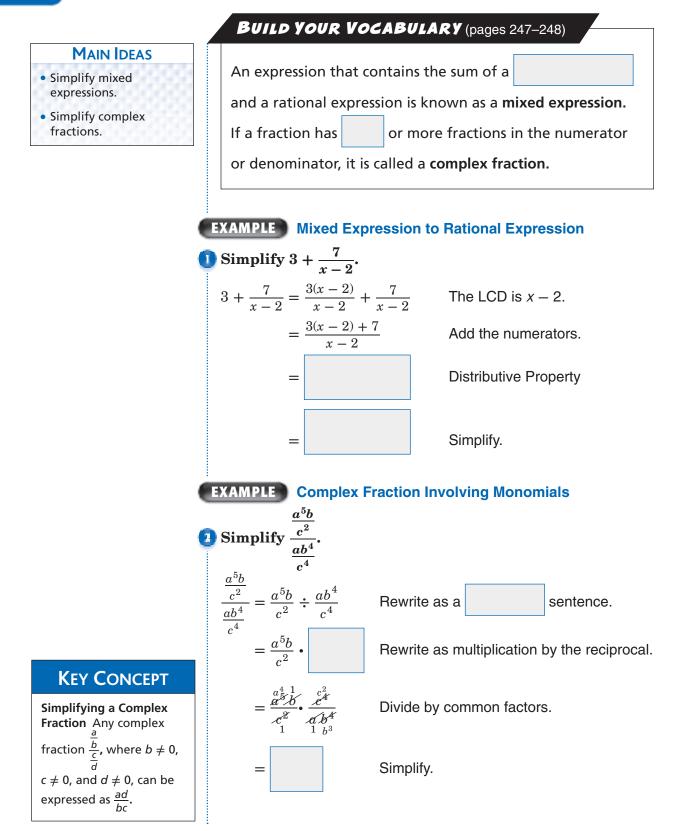




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## **Mixed Expressions and Complex Fractions**

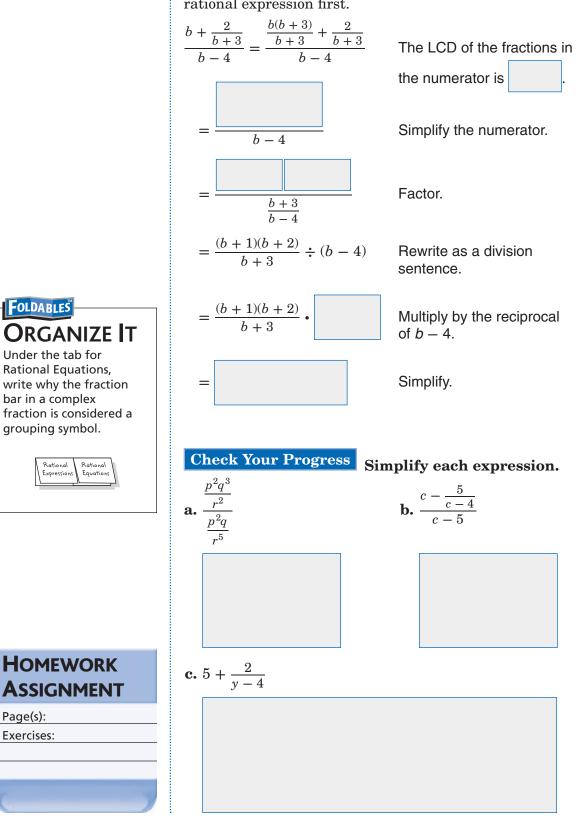


11-8



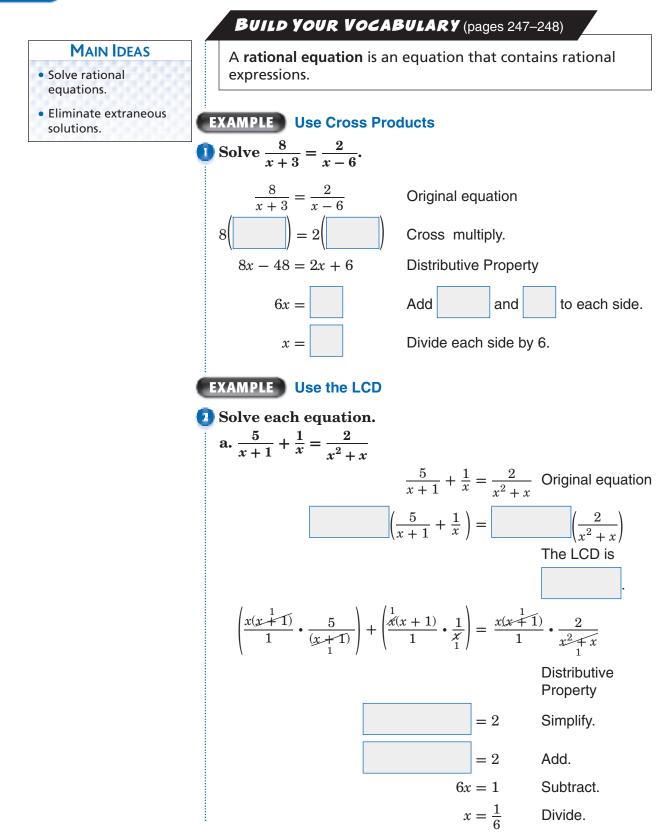
$$3 \text{ Simplify } \frac{b + \frac{2}{b+3}}{b-4}.$$

The numerator contains a mixed expression. Rewrite it as a rational expression first.

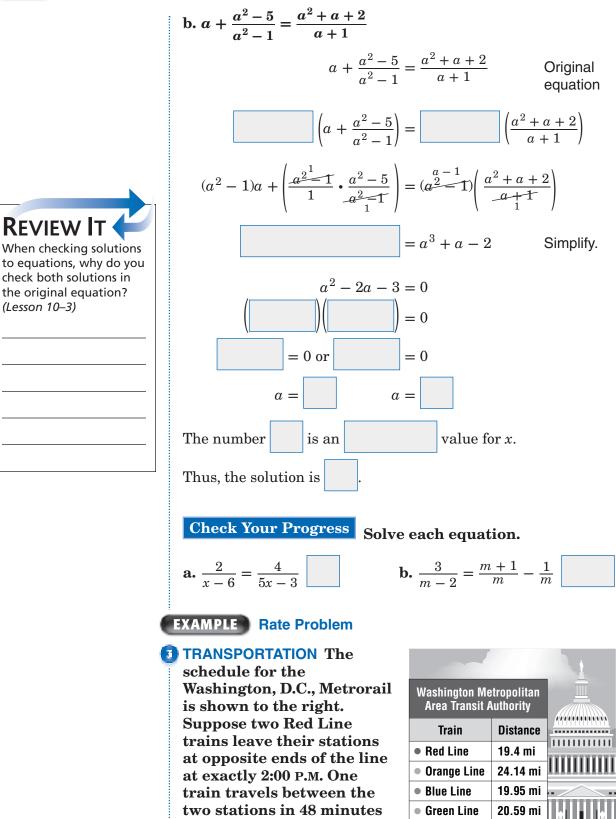


11-9

## **Solving Rational Equations**







and the other train takes

54 minutes. At what time do the two trains pass

each other?

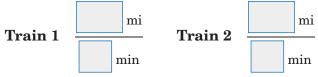
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9.46 mi

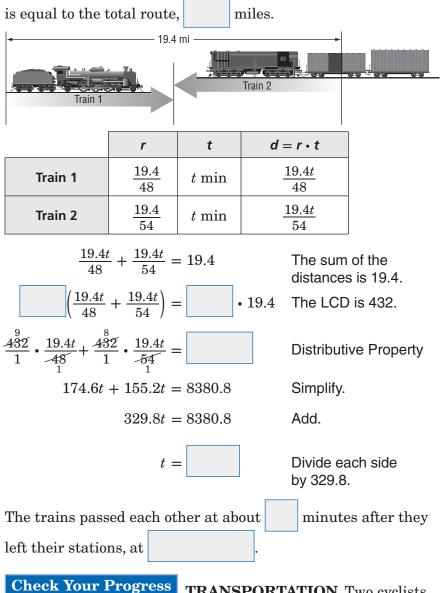
Yellow Line



Determine the rates of both trains. The total distance is 19.4 miles.

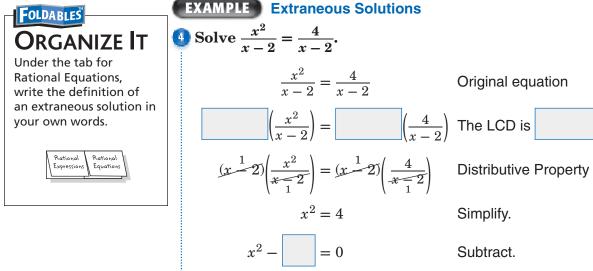


Next, since both trains left at the same time, the time both have traveled when they pass will be the same. And since they started at opposite ends of the route, the sum of their distances



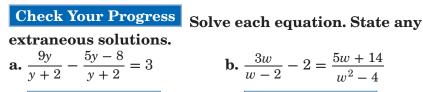
**Check Your Progress TRANSPORTATION** Two cyclists are riding on a 5-mile circular bike trail. They both leave the bike trail entrance at 3:00 P.M. traveling in opposite directions. It usually takes the first cyclist one hour to complete the trail and it takes the second cyclist 50 minutes. At what time will they pass each other?





(x-2)(x+2) = 0Factor. x - 2 = 0 or x + 2 = 0Zero Product Property x =x =

The number 2 is an extraneous solution, since 2 is an excluded value for x. Thus, -2 is the solution of the equation.



b.	$\frac{3w}{w-2}$	- 2 =	$\frac{5w+14}{w^2-4}$

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Page(s):

Exercises:



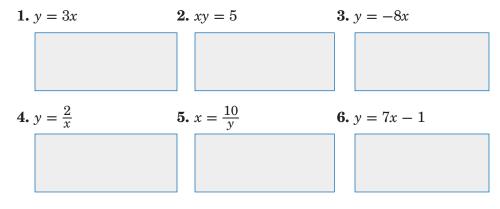
# **BRINGING IT ALL TOGETHER**

## STUDY GUIDE

ZZLEMAKER	Vocabulary
l search, or jumble puzzle e vocabulary words in	You can use your completed <b>Vocabulary Builder</b> (pages 247–248) to help you solve the puzzle.
	ZZLEMAKER ake a crossword puzzle, d search, or jumble puzzle e vocabulary words in oter 11, go to: coe.com

#### 11-1 Inverse Variation

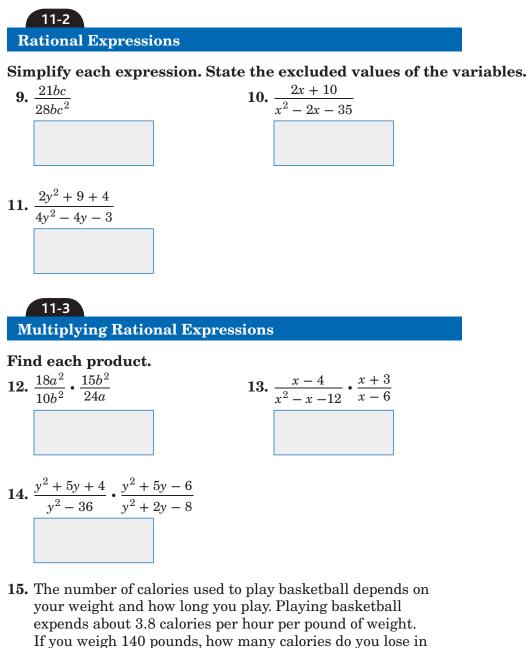
Write *direct variation, inverse variation,* or *neither* to describe the relationship between x and y described by each equation.



For each problem, assume that y varies inversely as x. Use the Product Rule to write an equation you could use to solve the problem. Then write a proportion and solve the problem.

	Problem	Product Rule	Proportion	Solve
7.	If $y = 8$ when x = 12, find $ywhen x = 4.$			
8.	If $x = 50$ when y = 6, find $xwhen y = 30$			

## Chapter BRINGING IT ALL TOGETHER



1.25 hours?

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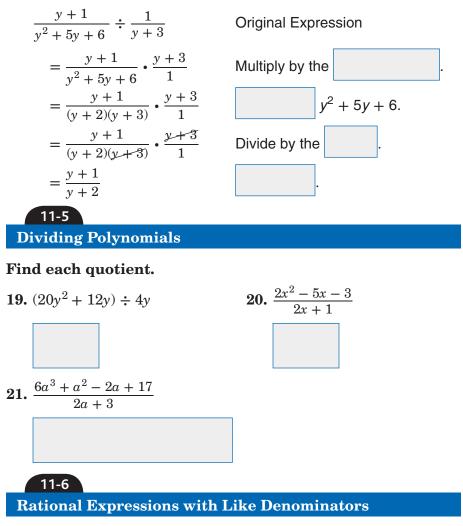


#### 11-4 Dividing Rational Equations

State the reciprocal of the divisor in each of the following.

**16.** 
$$\frac{3b+15}{b+1} \div (b-2)$$
 **17.**  $\frac{2c^2}{d} \div \frac{c}{3d}$ 

18. Supply the reason for the steps below.



For each addition or subtraction problem, write the needed expression in each box on the right side of the equation.

22. 
$$\frac{5n}{7} + \frac{8}{7} = \frac{5n + 1}{7}$$
  
23.  $\frac{d-c}{c+2d} - \frac{c-d}{c+2d} = \frac{1-(c-d)}{c+2d}$   
24.  $\frac{8}{6x-1} + \frac{9}{1-6x} = \frac{8+(1)}{6x-1}$ 

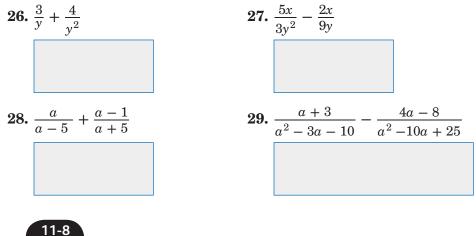
### Chapter BRINGING IT ALL TOGETHER

11-7

**Rational Expressions with Unlike Denominators** 

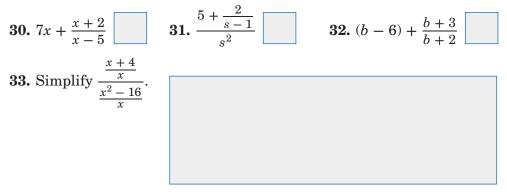
**25.** What is the LCM of  $49k^2n^2$  and  $21kn^5$ ?

#### Find each sum or difference.



**Mixed Expressions and Complex Fractions** 

Tell whether each expression is a mixed expression or complex fraction. Write M for mixed expression and C for complex fraction.

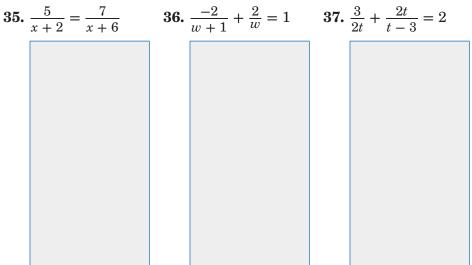


Chapter 11 BRINGING IT ALL TOGETHER

#### 11-9 Solving Rational Equations

**34.** Is  $\frac{\sqrt{x-3}}{4} = \frac{3}{x}$  a rational equation? Explain.

Solve each equation. State any extraneous solutions.



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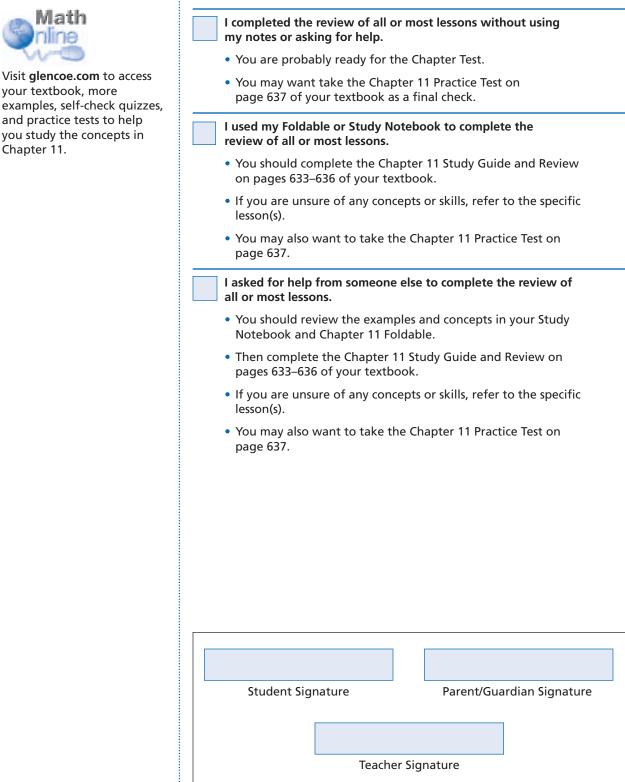


your textbook, more

Chapter 11.

## ARE YOU READY FOR THE CHAPTER TEST?

Check the one that applies. Suggestions to help you study are given with each item.

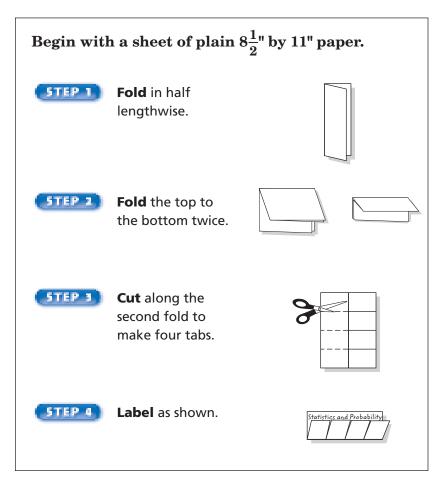




# **Statistics and Probability**



Use the instructions below to make a Foldable to help you organize your notes as you study the chapter. You will see Foldable reminders in the margin of this Interactive Study Notebook to help you in taking notes.



NOTE-TAKING TIP: If your instructor points out definitions or procedures from your text, write a reference page in your notes. You can then write these referenced items in their proper place in your notes after class.



#### BUILD YOUR VOCABULARY

This is an alphabetical list of new vocabulary terms you will learn in Chapter 12. As you complete the study notes for the chapter, you will see Build Your Vocabulary reminders to complete each term's definition or description on these pages. Remember to add the textbook page number in the second column for reference when you study.

Vocabulary Term	Found on Page	Definition	Description or Example
biased sample			
combination			
complements			
compound event			
convenience sample			
kuhn·VEEN·yuhn(t)s			
dependent events			
empirical study			
event			
experimental probability			
factorial			

Vocabulary Term	Found on Page	Definition	Description or Example
inclusive			
independent events			
population			
random sample			
sample			
simple random sample			
stratified random sample			
systematic random sample SIHS·tuh·MA·tihk			
voluntary response sample			



## **Sampling and Bias**

#### MAIN IDEAS

- Identify various sampling techniques.
- Recognize a biased sample.

#### **KEY CONCEPTS**

Simple Random Sample: A sample that is as likely to be chosen as any other from the population.

Stratified Random Sample In a stratified random sample, the population is first divided into similar, nonoverlapping groups. A simple random sample is then selected from each group.

Systematic Random Sample In a systematic random sample, the items are selected according to a specified time or item interval.

#### BUILD YOUR VOCABULARY (pages 278–279)

A sample is some portion of a

group, called

the population, selected to represent that group. If all of

within a population are included, it is called

#### a **census**.

the

In a biased sample, one or more parts of a population are

over others.

#### EXAMPLE Classify a Random Sample

a. RETAIL Each day, a department store chain selects one male and one female shopper randomly from each of their 57 stores, and asks them survey questions about their shopping habits.

Identify the sample and suggest a population from which it was selected.

The sample is	male and	female shoppers. The
population is		

#### b. Classify the sample as *simple*, *stratified*, or *systematic*.

The population is divided into similar, nonoverlapping

groups. This is a

sample.

# **Check Your Progress** At an automobile factory, every tenth item is checked for quality controls.

**a.** Identify the sample and suggest a population from which it was selected.

**b.** Classify the sample as *simple*, *stratified*, or *systematic*.







**KEY CONCEPTS** 

A convenience sample includes members of a

A voluntary response

sample involves only those who want to

HOMEWORK

ASSIGNMENT

participate in the sampling.

population that are easily

**Biased Samples** 

accessed.

Page(s): Exercises:

### EXAMPLE Identify Sample as Biased or Unbiased

STUDENT COUNCIL The student council surveys the students in one classroom to decide the theme for the spring dance. Identify the sample as biased or unbiased. Explain your reasoning.

The sample includes only students in one classroom.

The sample is

#### **Check Your Progress**

Identify the sample as *biased* or unbiased. Explain your reasoning.

A local news station interviews one person on every street in Los Angeles to give their opinion on their mayor.

### EXAMPLE Identify and Classify a Biased Sample

**1** a. COMMUNITY The residents of a neighborhood are to be surveyed to find out when to hold a neighborhood clean up day. The neighborhood chairperson decides to ask her immediate neighbors and the neighbors in the houses directly across the street from her house.

Identify the sample, and suggest a population from which it was selected.

The sample is the

and the neighbors across the street. The

is the residents of the neighborhood.

b. Classify the sample as a *convenience sample*, or a voluntary response sample.

This is a sample because the chairperson

asked only her closest neighbors.

**Check Your Progress** Mark wanted to find out what the average student in the United States does on the weekend. He decides to interview people in his dorm. Identify the sample, and suggest a population from which it was selected. Then classify the sample as a *convenience sample*, or a *voluntary* response sample.

# **Counting Outcomes**

### MAIN IDEAS

- Count outcomes using a tree diagram.
- Count outcomes using the Fundamental Counting Principle.

BUILD YOUR VOCABULARY (pages 278–279)

One method used for counting the number of possible

is to draw a **tree diagram**.

The list of all possible

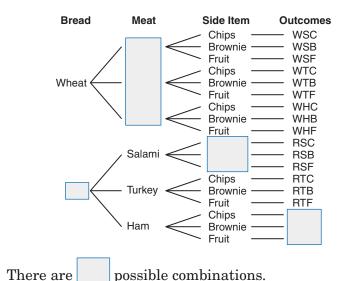
is called the sample

space. An event is any collection of one or more outcomes

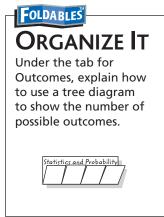
in the sample space.

### EXAMPLE Tree Diagram

At football games, a concession stand sells sandwiches on either wheat or rye bread. The sandwiches come with salami, turkey, or ham, and either chips, a brownie, or fruit. Use a tree diagram to determine the number of possible sandwich combinations.



**Check Your Progress** A buffet offers a combination of a meat, a vegetable, and a drink. The choices of meat are chicken or pork; the choices of vegetable are carrots, broccoli, green beans, or potatoes; and the choices of drink are milk, lemonade, or a soft drink. Use a tree diagram to determine the number of possible combinations.



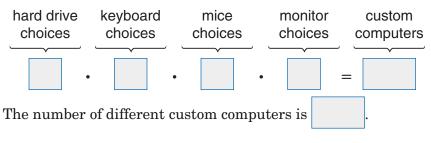
### **KEY CONCEPT**

Fundamental Counting Principle If an event Mcan occur in m ways and is followed by an event N that can occur in nways, then the event Mfollowed by event N can occur in  $m \cdot n$  ways.

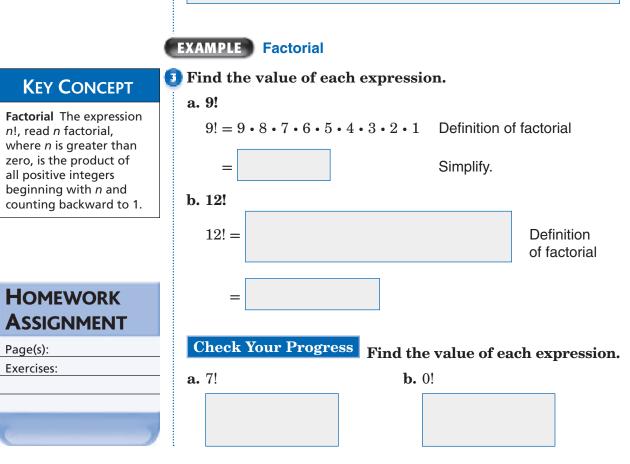
### EXAMPLE Fundamental Counting Principle

2 The Best Deal computer company sells custom made personal computers. Customers have a choice of 11 different hard drives, 6 different keyboards, 4 different mice, and 4 different monitors. How many different custom computers can you order?

Multiply to find the number of custom computers.



**Check Your Progress** A baseball team is organizing their draft. In the first five rounds, they want a pitcher, a catcher, a first baseman, a third baseman, and an outfielder. They are considering 7 pitchers, 9 catchers, 3 first baseman, 4 third baseman, and 12 outfielders. How many top picks are there to choose from?





# **Permutations and Combinations**

#### MAIN IDEAS

- Determine probabilities using permutations.
- Determine probabilities using combinations.

### BUILD YOUR VOCABULARY (pages 278-279)

An arrangement or listing in which order or placement is important is called a **permutation**.

An arrangement or listing in which order is not important is called a **combination**.

### EXAMPLE Permutation and Probability

### **KEY CONCEPT**

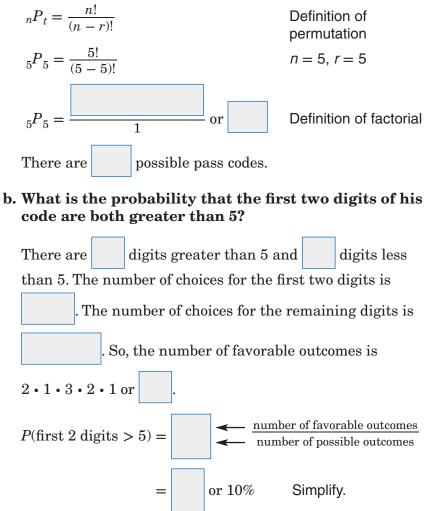
**Permutation** The number of permutations of *n* objects taken *r* at a time is the quotient of *n*! and (n - r)!.

**FOLDABLES** Under the permutation tab, record this definition in words and in symbols.

 Shaquille has a 5-digit code to access his e-mail account. The code is made up of the even digits 2, 4, 6, 8, and 0. Each digit can be used only once.

a. How many different pass codes could Shaquille have?

This situation is a permutation of 5 digits taken 5 at a time.



**Check Your Progress** Bridget and Brittany are trying to find a house, but they cannot remember the address. They can remember only that the digits used are 1, 2, 5, and 8, and that no digit is used twice. Find the number of possible addresses. Then find the probability that the first two numbers are odd.

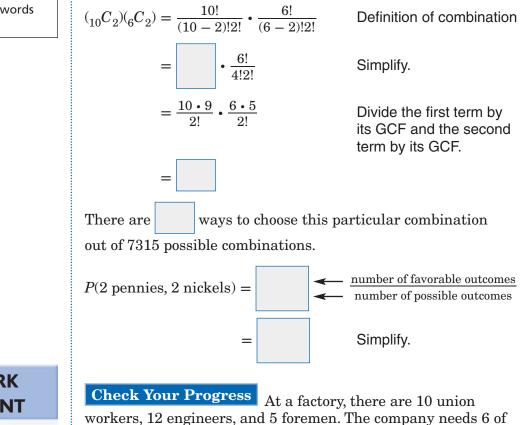
### **EXAMPLE** Combinations and Probability

2 MONEY Diane has a bag full of coins. There are 10 pennies, 6 nickels, 4 dimes, and 2 quarters in the bag. What is the probability that she will pull two pennies and two nickels out of the bag?

The number of combinations of 22 coins taken 4 at a time is

$$_{22}C_4 = \frac{22!}{(22-4)!4!}$$
 or

Using the Fundamental Counting Principle, the answer can be determined with the product of the two combinations.



workers, 12 engineers, and 5 foremen. The company needs 6 of these workers to attend a national conference. If the workers are chosen randomly, what is the probability that 3 union workers, 2 engineers, and 1 foreman are selected?

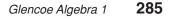
### KEY CONCEPT

**Combination** The number of combinations of *n* objects taken *r* at a time is the quotient of *n*! and (n - r!)r!.

**FOLDABLES** Under the combination tab, record this definition in words and in symbols.

Page(s):

Exercises:



# **Probability of Compound Events**

### MAIN IDEAS

- Find the probability of two independent events or dependent events.
- Find the probability of two mutually exclusive events or inclusive events.

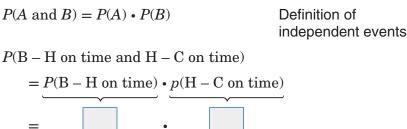
### BUILD YOUR VOCABULARY (pages 278–279)

A compound event is made up of or more					
events.					
Independent events are events in which the outcome of					
one event does not the outcome of the other.					
When the outcome of one event the outcome					
of another event, the events are dependent events.					

### EXAMPLE Independent Events

or 45%

Rae is flying from Birmingham to Chicago. She has to fly from Birmingham to Houston on the first leg of her trip. In Houston she changes planes and heads to Chicago. The airline reports that the flight from Birmingham to Houston has a 90% on time record, and the flight from Houston to Chicago has a 50% on time record. What is the probability that both flights will be on time?



# KEY CONCEPTS

**Probability of Independent Events** If two events, *A* and *B*, are independent, then the probability of both events occuring is the product of the probability of *A* and the probability of *B*.

### Probability of

**Dependent Events** If two events, *A* and *B*, are dependent, then the probability of both events occuring is the product of the probability of *A* and the probability of *B* after *A* occurs.

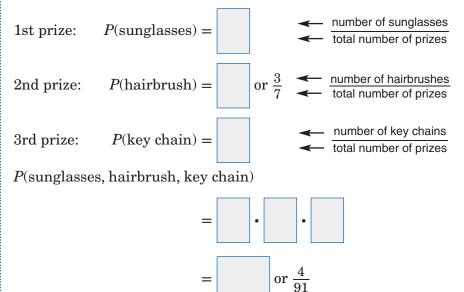
**Check Your Progress** Two cities, Fairfield and Madison, lie on different faults. There is a 60% chance that Fairfield will experience an earthquake by the year 2010 and a 40% chance that Madison will experience an earthquake by 2010. Find the probability that both cities will experience an earthquake by 2010.

Multiply.

### **EXAMPLE** Dependent Events

2 At the school carnival, winners in the ring-toss game are randomly given a prize from a bag that contains 4 sunglasses, 6 hairbrushes, and 5 key chains. Three prizes are randomly drawn from the bag and not replaced. Find *P*(sunglasses, hairbrush, key chain).

The selection of the first prize affects the selection of the next prize since there is one less prize from which to choose. So, the events are dependent.



**Check Your Progress** A gumball machine contains 16 red gumballs, 10 blue gumballs, and 18 green gumballs. Once a gumball is removed from the machine, it is not replaced. Find each probability if the gumballs are removed in the order indicated.

**a.** *P*(red, green, blue)

**b.** *P*(green, blue, not red)

## BUILD YOUR VOCABULARY (pages 278–279)

The events for drawing a marble that is green and for

drawing a marble that is

green are called **complements**.

time are called

Events that cannot occur at the **mutually exclusive.** 

Two events that occur at the same time are called **inclusive events**.



### **KEY CONCEPTS**

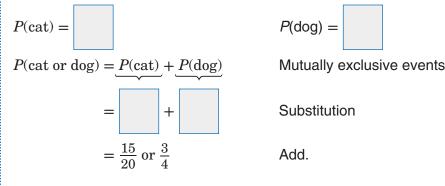
Mutually Exclusive Events If two events, A and B, are mutually exlcusive, then the probability that either A or B occurs is the sum of their probabilities.

**Probability of Inclusive Events** If two events, *A* and *B*, are inclusive, then the probability that either *A* or *B* occurs is the sum of their probabilities decreased by the probability of both occuring.

**FOLDABLES** Take notes on how to find the probability of compound events.

### **EXAMPLE** Mutually Exclusive Events

3 Alfred is going to the Lakeshore Animal Shelter to pick a new pet. Today, the shelter has 8 dogs, 7 cats, and 5 rabbits available for adoption. If Alfred randomly picks an animal to adopt, what is the probability that the animal would be a cat or a dog?



#### EXAMPLE Inclusive Events

• A dog has just given birth to a litter of 9 puppies. There are 3 brown females, 2 brown males, 1 mixed-color female, and 3 mixed-color males. If you choose a puppy at random from the litter, what is the probability that the puppy will be male or mixed-color?

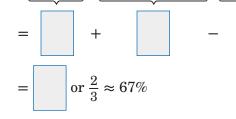
**A** 
$$\frac{2}{9}$$
 **B**  $\frac{1}{3}$  **C**  $\frac{5}{9}$  **D**  $\frac{2}{3}$ 

These events are inclusive.

*P*(male or mixed-color)

$$= P(male) + P(mixed-color) - P(male and mixed-color)$$

Simplify.



The answer is D.

## Homework Assignment

Page(s):

Exercises:

#### **Check Your Progress**

In Mrs. Kline's class, 7 boys have brown eyes and 5 boys have blue eyes. Out of the girls, 6 have brown eyes and 8 have blue eyes. If a student is chosen at random from the class, what is the probability that the student will be a boy or have brown eyes?

## **Probability Distributions**

### MAIN IDEAS

- Use random variables to compute probability.
- Use probability distributions to solve real-world predictions.

### EXAMPLE Random Variable

- The owner of a pet store asked customers how many pets they owned. The results of this survey are shown in the table.
  - a. Find the probability that a randomly chosen customer has at most 2 pets.

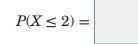
Number of Pets	Number of Customers				
0	3				
1	37				
2	33				
3	18				
4	9				

There are 3 + 37 + 33 or

outcomes in which a customer

owns at most 2 pets. There are

survey results.



b. Find the probability that a randomly chosen customer has 2 or 3 pets.

There are + or

outcomes in which a

customer owns 2 or 3 pets.

$$P(X = 2 \text{ or } 3) =$$

3) = or

or

**Check Your Progress** 

was conducted concerning the number of movies people watch at the theater per month. The results of this survey are shown in the table.

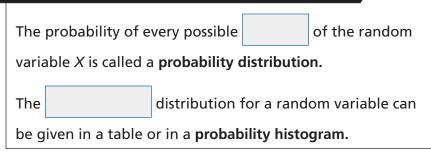
Movies (per month)	Numbers of People
0	7
1	23
2	30
3	29
4	11

**a.** Find the probability that a randomly chosen person watched at most 1 movie per month.

**b.** Find the probability that a randomly chosen person watches 0 or 4 movies per month.

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## BUILD YOUR VOCABULARY (pages 278–279)



### EXAMPLE Probability Distribution

### KEY CONCEPT

Properties of Probability Distributions

- 1. The probability of each value of X is greater than or equal to 0 and less than or equal to 1.
- 2. The probabilities of all the values of *X* add up to 1.

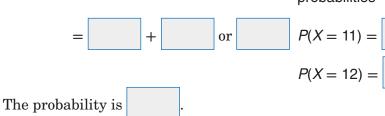
The table shows the probability distribution of the number of students in each grade at Sunnybrook High School. If a student is chosen at random, what is the probability that he or she is in grade 11 or above?

X = grade	P(X)
9	0.29
10	0.26
11	0.25
12	0.2

The probability of a student being in grade 11 or above is the sum of the probability of grade 11 and the probability of grade 12.

$$P(X \ge 11) = P(X = 11) + P(X = 12)$$

Sum of individual probabilities



The table

**Check Your Progress** 

shows the probability distribution of the number of children per family in the city of Maplewood. If a family was chosen at random, what is the probability that they have at least 2 children?

X = Number of Children	P(X)
0	0.11
1	0.23
2	0.32
3	0.26
4	0.08

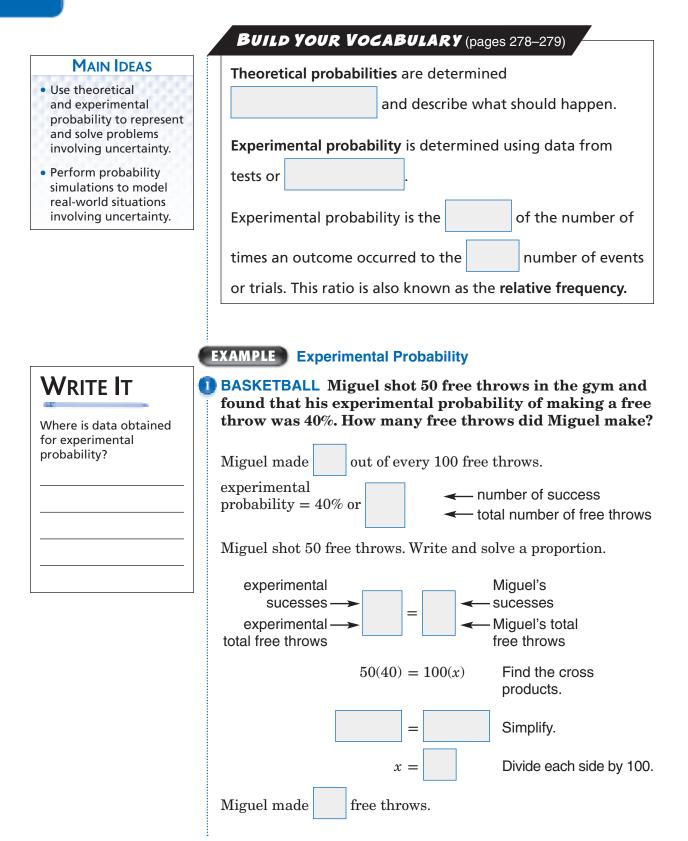
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## HOMEWORK ASSIGNMENT

Page(s):

Exercises:

# **Probability Simulations**





**Check Your Progress** Nancy was testing her serving accuracy in volleyball. She served 80 balls and found that the experimental probability of keeping it in bounds was 60%. How many serves did she keep in bounds?

### BUILD YOUR VOCABULARY (pages 278-279)

When you	an experiment repeatedly,	collect			
and combine the	, and	the			
results, this is known as an <b>empirical study</b> .					
A <b>simulation</b> allows you to use objects to act out an that would be difficult or impractical to perform.					



### EXAMPLE Empirical Study

A pharmaceutical company performs three clinical studies to test the effectiveness of a new medication. Each study involved 100 volunteers. The results of the studies are shown in the table.

Result	Study 1	Study 2	Study 3
Expected Success Rate	70%	70%	70%
Condition Improved	61%	74%	67%
No improvement	39%	25%	33%
Condition Worsened	0%	1%	0%

What is the experimental probability that the drug showed no improvement in patients for all three studies?

The number of outcomes with no improvement for the three

studies was 39 + 25 + 33 or

out of the 300 total patients.

experimental probability =

or about

**Check Your Progress** A new study is being developed to analyze the relationship between heart rate and watching scary movies. A researcher performs three studies, each with 100 volunteers. Based on similar studies, the researcher expects that 80% of the subjects will experience a significant increase in heart rate. The table shows the results of the study. What is the experimental probability that the movie would cause a significant increase in heart rate for all three studies?

Result	Study 1	Study 2	Study 3
Expected Success Rate	80%	80%	80%
Rate increased significantly	83%	75%	78%
Littler or no increase	16%	24%	19%
Rate decreased	1%	0%	0%

### **EXAMPLE** Simulation

- 🚺 In the last 30 school days, Bobbie's older brother has given her a ride to school 5 times.
  - a. What could be used to simulate whether Bobbie's brother will give her a ride to school?

Bobbie got a ride to school  $\frac{3}{50}$  or  $\frac{1}{6}$  days. Since a die has

sides, you could use one side of a die to represent a ride to school.

b. Describe a way to simulate whether Bobbie's brother will give her a ride to school in the next 20 school days.

Choose the side of the die that will be used to represent a ride to school. Let the 1-side of the die equal a ride to school.

Toss the die

times and record each result.



simulate the possible outcomes of the event.

HOMEWORK ASSIGNMENT

Page(s):

Exercises:

**Check Your Progress** In the last 52 days, it has rained 4 times. What could be used to simulate whether it will rain on a given day? Describe a way to simulate whether it will rain in the next 15 days.



# **BRINGING IT ALL TOGETHER**

## STUDY GUIDE

FOLDABLES	Vocabulary Puzzlemaker	Build your Vocabulary
Use your <b>Chapter 12</b> Foldable to help you study for your chapter test.	To make a crossword puzzle, word search, or jumble puzzle of the vocabulary words in Chapter 12, go to: glencoe.com	You can use your completed <b>Vocabulary Builder</b> ( <i>pages 278–279</i> ) to help you solve the puzzle.

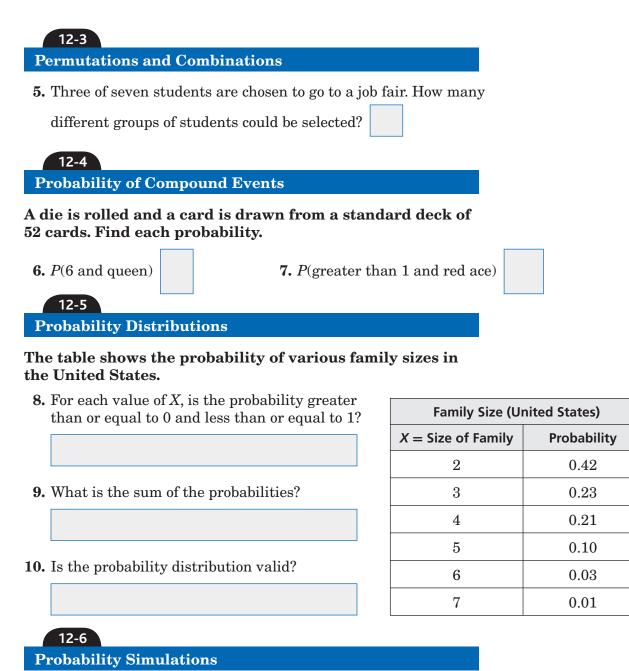


Suppose the principal at a school wants to use Saturdays as make-up days when school is closed due to weather. The principal selects and then polls a group of students to see if the student body supports the idea. Complete the sentences.

<b>1.</b> The student body is the		from which a		
of students is selected to	be polled. If all	the students a	are polled,	
it is called a				
12-2	_			
Counting Outcomes				
Use the tree diagram for	Exercises 2–4.			
2. What is the sample space	ce? C	Game 1 G	iame 2	Game 3
			win	→ win → lose
	v	vin	lose	— win
3. Name two different outo	comes.			- lose
			win 🧹	— win
		ose		— lose
			lose	— win
4. Use the Fundamental C Principle to find the pos	0	hown above.		– lose

	Game 1		Game 2		Game 3		Number of Outcomes
Number of choices		•		•		=	





**11.** Choose the manipulative you would use to simulate the problem. Explain your choice.

Situation	Simulation method
58% of drivers (commercial and private vehicles) have a cell phone in their car. Simulate whether or not the next 10 drivers you meet on the road will have a cell phone.	<ul> <li>die</li> <li>coins</li> <li>marbles</li> <li>spinner</li> </ul>

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to access your textbook,

to help you study the

concepts in Chapter 12.

# ARE YOU READY FOR THE CHAPTER TEST?

Check the one that applies. Suggestions to help you study are given with each item.

