

Lesson 6-5

Example 1

Find the solution to the system of equations: $2x - y = 6$, $2x + y = 14$.

Solution

$$\begin{aligned} 2x - y &= 6 \\ y &= 2x - 6 \quad \text{Solve the first equation for } y \text{ in terms of } x. \end{aligned}$$

$$\begin{aligned} 2x + y &= 14 \quad \text{Write the second equation.} \\ 2x + (2x - 6) &= 14 \quad \text{Substitute } (2x - 6) \text{ for } y. \\ 2x + 2x - 6 &= 14 \quad \text{Solve for } x. \\ 4x &= 20 \\ x &= 5 \end{aligned}$$

Choose one of the original equations.

$$\begin{aligned} 2x - y &= 6 \\ 2(5) - y &= 6 \quad \text{Substitute 5 for } x. \\ 10 - y &= 6 \quad \text{Solve for } y. \\ y &= 4 \end{aligned}$$

Check $x = 5$, $y = 4$ in each original equation.

$$\begin{array}{lll} \text{Check } x = 5, y = 4 \text{ in} & 2x - y = 6 & 2x + y = 14 \\ \text{each original equation.} & 2(5) - 4 = 6 & 2(5) + 4 = 14 \\ & 10 - 4 = 6 & 10 + 4 = 14 \\ & 6 = 6 \quad \checkmark & 14 = 14 \quad \checkmark \end{array}$$

The solution is $(5, 4)$.

Example 2

Find the solution to the system of equations: $2x - 3y = 9$, $6y - 4x = 12$.

Solution

$$\begin{aligned} 6y - 4x &= 12 \\ 6y &= 4x + 12 \quad \text{Solve for } y. \\ y &= \frac{2}{3}x + 2 \end{aligned} \qquad \begin{aligned} 2x - 3y &= 9 \\ 2x - 3\left(\frac{2}{3}x + 2\right) + 22 &= 9 \quad \text{Substitute for } y. \\ 2x - 2x - 6 + 22 &= 9 \\ -6 &= 9 \end{aligned}$$

There is no solution. The lines are parallel.

Example 3

Solve the system of equations: $9x - 6y = 18$, $6x - 4y = 12$.

Solution

$$9x - 6y = 18$$

$$y = \frac{3}{2}x - 3 \quad \text{Solve for } y.$$

$$6x - 4y = 12$$

$$6x - 4\left(\frac{3}{2}x - 3\right) = 12 \quad \text{Substitute for } y.$$

$$6x - 6x + 12 = 12$$

$$12 = 12$$

The lines are the same. There is an infinite number of solutions that satisfy the equation $9x - 6y = 18$ and $6x - 4y = 12$.

Example 4

SHIPPING An appliance store delivers large appliances using vans and trucks. When loaded, each van holds 5 appliances and each truck holds 8. If 54 appliances are delivered and 9 vehicles are full, how many vans and trucks are used?

Solution

Define each of the variables.

Write and solve a system of equations relating to the variables.

Let t = number of trucks

v = number of vans

There are 9 vehicles.

$$v + t = 9$$

$$t = 9 - v \quad \text{Solve for } t.$$

54 appliances are delivered; 8 in each truck and 5 in each van.

$$5v + 8t = 54$$

$$5v + 8(9 - v) = 54 \quad \text{Substitute } 9 - v \text{ for } t.$$

$$5v + 72 - 8v = 54$$

$$-3v = -18 \quad \text{Solve for } v.$$

$$v = 6$$

$$v + t = 9$$

$$6 + t = 9 \quad \text{Substitute for } v.$$

$$t = 3 \quad \text{Solve for } t.$$

There are 6 vans and 3 trucks delivering appliances.