Practice Problem Solutions

1.
$$b = r_{xy} \cdot \frac{S_x}{S_y} = .62 \cdot \frac{1.00}{2.41} = .257$$
 $a = \overline{X} - (b \cdot \overline{Y}) = 5.5 - (.257 \cdot 8.5) = 3.315$

 $\hat{X} = bY + a = .257(6.6) + 3.315 = 5.011$ hours sleep

$$S_{XY} = S_X \cdot \sqrt{1 - r^2} = 1.00 \cdot \sqrt{1 - .62^2} = 1.00 \cdot \sqrt{1 - .384} = .785$$

5.011 \pm .785 hours sleep predicted for someone recalling 6.6 words.

2.
$$\hat{X} = bY + a = .257(8.0) + 3.315 = 5.371$$

$$S_{XY} = S_X \cdot \sqrt{1 - r^2} = 1.00 \cdot \sqrt{1 - .62^2} = 1.00 \cdot \sqrt{1 - .384} = .785$$

5.371 \pm .785 hours sleep predicted for someone recalling 8.0 words.

3.
$$\hat{X} = bY + a = .257(4.2) + 3.315 = 4.394$$

 $S_{XY} = S_X \cdot \sqrt{1 - r^2} = 1.00 \cdot \sqrt{1 - .62^2} = 1.00 \cdot \sqrt{1 - .384} = .785$
4.394 ± .785 hours sleep predicted for someone recalling 4.2 words.

4.
$$b = r_{xy} \cdot \frac{S_Y}{S_X} = .62 \cdot \frac{2.41}{1.00} = 1.494$$
 $a = \overline{Y} - (b \cdot \overline{X}) = 8.5 - (1.494 \cdot 5.5) = .283$

$$\hat{Y} = bX + a = 1.494(6) + .283 = 9.247$$
 words recalled
 $S_{YX} = S_Y \cdot \sqrt{1 - r^2} = 2.41 \cdot \sqrt{1 - .62^2} = 2.41 \cdot \sqrt{1 - .384} = 1.892$

 9.247 ± 1.892 recalled words predicted for someone sleeping 6 hours on weeknights.

5.
$$\hat{Y} = bX + a = 1.494(8) + .283 = 11.952$$
 words recalled
 $S_{YX} = S_Y \cdot \sqrt{1 - r^2} = 2.41 \cdot \sqrt{1 - .62^2} = 2.41 \cdot \sqrt{1 - .384} = 1.892$

11.952 \pm 1.892 recalled words predicted for someone sleeping 8 hours on weeknights.

6.
$$\hat{Y} = bX + a = 1.494(4) + .283 = 5.976$$
 words recalled
 $S_{YX} = S_Y \cdot \sqrt{1 - r^2} = 2.41 \cdot \sqrt{1 - .62^2} = 2.41 \cdot \sqrt{1 - .384} = 1.892$
5.976 ± 1.892 recalled words predicted for someone sleeping 4 hours on weeknights.

7.
$$b = r_{xy} \cdot \frac{S_Y}{S_X} = .64 \cdot \frac{12}{9} = .853$$
 $a = \overline{Y} - (b \cdot \overline{X}) = 63.3 - (.853 \cdot 39.8) = 29.351$

The regression equation for predicting the life satisfaction score from age is:

$$\hat{Y} = bX + a = .853(X) + 29.351$$

8.
$$\hat{Y} = bX + a = .853(50) + 29.351 = 42.65 + 29.351 = 72.00$$

 $S_{YX} = S_Y \cdot \sqrt{1 - r^2} = 12 \cdot \sqrt{1 - .64^2} = 12 \cdot \sqrt{1 - .410} = 9.216$

72.00 \pm 9.216 points is the predicted life satisfaction score for someone 50 years of age.

9. $\hat{Y} = bX + a = .853(30) + 29.351 = 25.59 + 29.351 = 54.941$ $S_{YX} = S_Y \cdot \sqrt{1 - r^2} = 12 \cdot \sqrt{1 - .64^2} = 12 \cdot \sqrt{1 - .410} = 9.216$

54.941 \pm 9.216 points is the predicted life satisfaction score for someone 30 years of age.

10.
$$\hat{Y} = bX + a = .853(60) + 29.351 = 51.18 + 29.351 = 80.531$$

$$S_{YX} = S_Y \cdot \sqrt{1 - r^2} = 12 \cdot \sqrt{1 - .64^2} = 12 \cdot \sqrt{1 - .410} = 9.216$$

 80.531 ± 9.216 points is the predicted life satisfaction score for someone 60 years of age.